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# A New Method to Reconstruct Quantitative Food Webs and Nutrient Flows from Isotope Tracer Addition Experiments

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**ABSTRACT:** Understanding how nutrients flow through food webs is central in ecosystem ecology. Tracer addition experiments are powerful tools to reconstruct nutrient flows by adding an isotopically enriched element into an ecosystem and tracking its fate through time. Historically, the design and analysis of tracer studies have varied widely, ranging from descriptive studies to modeling approaches of varying complexity. Increasingly, isotope tracer data are being used to compare ecosystems and analyze experimental manipulations. Currently, a formal statistical framework for analyzing such experiments is lacking, making it impossible to calculate the estimation errors associated with the model fit, the interdependence of compartments, and the uncertainty in the diet of consumers. In this article we develop a method based on Bayesian hidden Markov models and apply it to the analysis of  $^{15}\text{N-NH}_4^+$  tracer additions in two Trinidadian streams in which light was experimentally manipulated. Through this case study, we illustrate how to estimate N fluxes between ecosystem compartments, turnover rates of N within those compartments, and the associated uncertainty. We also show how the method can be used to compare alternative models of food web structure, calculate the error around derived parameters, and make statistical comparisons between sites or treatments.

**Keywords:** food webs, hidden Markov model (HMM), isotope tracer addition, model selection, nutrient uptake, state-space models.

## Introduction

Food webs are the cornerstone of community and ecosystem ecology because they describe the flow of matter and

energy among organisms, thus defining important properties of an ecosystem, such as stability and productivity (Paine 1980; Newbold et al. 1983; Carpenter et al. 2005; Rooney and McCann 2012). They provide the raw material for many ecological questions, including the study of trophic cascades, nutrient cycling, and ecosystem productivity. Food web studies have been a major theme in ecological research for more than a century, beginning with early work that identified trophic linkages (Elton 1927). More recent studies have attempted to quantitatively track the movement of energy and materials through food web compartments, which remains particularly challenging because of complex methods for both data collection and analysis (Dodds et al. 2014).

While interaction strength has been defined in a variety of ways throughout the literature, ecosystem scientists are often interested in the biomass flux of a given nutrient between two species or compartments (Berlow et al. 2004). Researchers have used a variety of approaches to estimate trophic fluxes in the past, including gut-content analysis (Ledger et al. 2013) and analysis of egested material (such as feces or pellets; Lima et al. 2002; Roslin and Majaneva 2016). These methods, however, are sensitive to sampling effects (Banašek-Richter et al. 2004) and only consider what is ingested, rarely accounting for what is assimilated into tissue, and therefore they may not provide accurate estimates of how matter and energy flows through an ecosystem. Another approach is stable isotope analysis, which uses natural variation in the abundance of stable isotopes (most often  $^{13}\text{C}$ ,  $^{15}\text{N}$ , or  $^2\text{H}$ ) across organisms to infer trophic relations (Peterson and Fry 1987; Boecklen et al. 2011). While these natural abundance isotope webs offer a more integrative picture of diet and directly target assimilated nutrients, they are often descriptive and unable to quantify

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fluxes. Moreover, results are sensitive to the assumptions of diet-mixing models (Post 2002; Bond and Diamond 2011) and often fail to differentiate carbon sources in freshwater ecosystems (Jardine et al. 2014). A powerful alternative is using whole-ecosystem isotope addition experiments to estimate fluxes across trophic compartments and characterize nutrient cycles (Newbold et al. 1983; Kling 1994; Carpenter et al. 2005).

Isotope tracer additions use small amounts of isotopically enriched nutrients to track the movement of nutrient tracers among different ecosystem compartments through time. Depending on the properties of the ecosystem, isotopes are added all at once (pulse design) or at a constant rate over a period of time (press design). The pulse design was used in early additions of radioisotopes to lakes (Hutchinson and Bowen 1950; Rigler 1956), streams (Ball and Hooper 1963; Elwood and Nelson, 1972; Newbold et al. 1983), and meso- and microcosms (Whittaker 1961; Patten and Witkamp 1967). Whittaker (1961) pioneered the use of a linear donor-controlled compartment model to quantify transfers of the tracer through the food web, an approach also applied by Patten and Witkamp (1967) and by Newbold et al. (1983). For their whole-stream addition of  $^{32}\text{P}$ , Newbold et al. (1983) calculated transfer fluxes of the naturally occurring phosphorus from the steady-state solution of the compartment model. In press additions, the tracer accumulates in specific ecosystem compartments until an equilibrium state is achieved or the addition ends. Once the addition stops, the tracer begins to clear from basal compartments (e.g., algae) and, progressively after, from higher trophic levels. This design has been used extensively in stream ecosystems to estimate nutrient uptake and turnover (Dodds et al. 2000; Mulholland et al. 2000).

Complemented with estimates of compartment sizes (biomasses), isotopic additions allow for the estimation of nutrient uptake and turnover rates for all ecosystem compartments as well as quantification of the fluxes between them (Dodds et al. 2000; Mulholland et al. 2000). This tracer addition approach has been used to characterize a variety of systems, including nitrogen ( $^{15}\text{N}$ ) in streams (summarized by Dodds et al. 2014) and forests (Goodale et al. 2015), carbon ( $^{13}\text{C}$ ) in marine and lake ecosystems (Middelburg et al. 2000; Cole et al. 2002; Pace et al. 2004), and deuterium-labeled water ( $^2\text{H}_2\text{O}$ ) in terrestrial ecosystems (Kulmatiski et al. 2010).

Despite the increase in their use, there is no formal statistical framework to analyze whole-ecosystem data from tracer addition experiments. Instead, each trophic linkage is analyzed separately, solving for a mass balance between tracer uptake and turnover under the following assumptions: (1) the source pools from which a consumer obtains nutrients are known; (2) if there is more than one source, the proportional contribution of each source is known;

(3) the added isotope is instantaneously and perfectly mixed within a compartment; and (4) consumers do not prey selectively within a source compartment (i.e., the isotopic signature of the matter taken up reflects the signature of the source; Dodds et al. 2000; Mulholland et al. 2000). Some of these assumptions can be problematic. First, trophic links can be uncertain, and even when every consumer's source compartment is known, estimates of their proportional contribution tend to be crude approximations (Ainsworth et al. 2010). Second, consumers often differentially assimilate components of their diet or selectively feed on specific portions of a sampled compartment. If not accounted for, this can cause seemingly paradoxical results, where consumers are more enriched with the tracer than the resource they feed on (Dodds et al. 2014). Regardless of their assumptions, neither of these approaches allows error in the inferences of parameters at lower trophic levels to propagate into flux estimates at higher trophic levels. Nor can they estimate and incorporate the error associated with uncertainty in trophic relationships or diet proportions. With the increase in the use of isotope tracer additions in comparative studies (Dodds et al. 2014; Norman et al. 2017; Tank et al. 2018) and ecosystem-scale experiments (Whiles et al. 2013; Collins et al. 2016), it has become imperative to develop a statistical framework that allows rigorous comparisons among systems and treatments.

To meet this need, we developed a novel approach to the statistical analysis of isotope tracer data based on Bayesian hidden Markov models (HMMs; Zucchini and MacDonald 2009; King 2014). Our approach allows for simultaneous modeling of nutrient transfers among all measured ecosystem compartments, providing estimations of parameter uncertainty that account for both observation and process error propagating across compartments. For omnivores, our method does not require a priori assumptions on the proportion of different prey constituting the diet but rather estimates the proportion as a model parameter. It also allows the modeling of nonhomogeneous compartments by estimating actively cycling versus refractory proportions, thus accounting for overenriched signatures in consumers. Moreover, when there are doubts in the topology of the food web (e.g., whether a particular predator eats a specific prey or not), model comparison tools can be used to choose between the most parsimonious structure according to the data.

We first present the mathematical and statistical framework, framed as a HMM (Zucchini and MacDonald 2009), and then demonstrate its application with a case study on two Trinidadian montane streams differing in canopy cover (Collins et al. 2016). We illustrate how the approach can be used to (1) estimate model parameters and their uncertainty; (2) calculate derived properties, such as nutrient fluxes and compartment residence times, and their

uncertainty; (3) test alternative food web topologies; and (4) statistically compare experimental treatments.

### Modeling Tracer Dynamics

#### Mathematical Framework

The transfer of nutrients from one compartment to the other can be represented as a Markov chain, a probabilistic model where the state of a given system (i.e., the distribution of nutrients across compartments) at time  $t$  depends only on its previous state at time  $t - 1$  (Iosifescu 1980). In a HMM, dynamic data are modeled as a consequence of two stochastic processes: an unobserved biological pro-

cess (here, nutrient fluxes) and an observation process that is conditional on the biological process (in our case, sampling and measurement of isotopic ratios). Table 1 shows a summary of the parameter notation followed and units of measurement used.

We conceptualize an ecosystem as a population of nutrient atoms flowing between compartments of an ecosystem. These compartments correspond, in HMM terminology, to the possible states a nutrient atom can be in. For a given ecosystem with a set of  $C$  compartments, we can define the distribution of atoms among compartments at time  $t$  as a  $C \times 1$  vector  $\mathbf{x}^{(t)} = \{x_1^{(t)}, x_2^{(t)}, \dots, x_N^{(t)}\}$ , where  $x_i^{(t)}$  indicates the number of nutrient atoms in compartment  $i$  at time  $t$ . We can then define a  $C \times C$  transition matrix  $\Psi$  where each

**Table 1:** Notation

Parameter	Description	Domain	Unit
Observed variables:			
$C$	Number of ecosystem compartments	$\mathbb{N}$	...
$\mathcal{T}$	Set of dissolved inorganic nutrient compartments	...	...
$\mathcal{B}$	Set of basal resources uptaking dissolved nutrients	...	...
$x_{\text{obs},i}^{(s,t)}$	Biomass of compartment $i$ at sampling point $s$ and time $t$	$(0, \infty)$	mgN m <sup>-2</sup>
$z_{\text{obs},i}^{(s,t)}$	Proportion of marked isotope in compartment $i$ at sampling point $s$ and time $t$	$(0, 1)$	1
$SD_i$	Standard deviation of compartment biomasses $x_i$	$(0, 1)$	1
State variables:			
$\mathbf{x}^{(s,t)}$	$C \times 1$ vector of elements $x_i^{(s,t)}$ = nutrient mass in compartment $i$ at sampling point $s$ and time $t$	$(0, \infty)$	mgN m <sup>-2</sup>
$\mathbf{n}^{(s,t)}$	$C \times 1$ vector of elements $n_i^{(s,t)}$ = unmarked nutrient mass in compartment $i$ at sampling point $s$ and time $t$	$(0, \infty)$	mgN m <sup>-2</sup>
$\mathbf{m}^{(s,t)}$	$C \times 1$ vector of elements $m_i^{(s,t)}$ = marked nutrient mass in compartment $i$ at sampling point $s$ and time $t$	$(0, \infty)$	mgN m <sup>-2</sup>
$\mathbf{z}^{(s,t)}$	$C \times 1$ vector of elements $z_i^{(s,t)}$ = proportion of heavy isotope for compartment $i$ at sampling point $s$ and time $t$	$(0, 1)$	1
$\mathbf{y}_n^{(s,t)}$	$C \times 1$ vector of elements $y_{n,i}^{(s,t)}$ = external input of unmarked nutrient into $i$ at sampling point $s$ and time $t$	$(0, \infty)$	mgN m <sup>-2</sup>
$\mathbf{y}_m^{(s,t)}$	$C \times 1$ vector of elements $y_{m,i}^{(s,t)}$ = external input of marked nutrient into $i$ at sampling point $s$ and time $t$	$(0, \infty)$	mgN m <sup>-2</sup>
Estimated parameters:			
$\Psi_h$	Transition matrix of elements $\psi_{i,j}$ = rate of nutrient transition between compartments $j$ and $i$ under model $\mathbf{h}$	$(0, 1)$	day <sup>-1</sup>
$v_{ij}$	Uptake rate from compartment $j$ to $i$	$(0, 1)$	day <sup>-1</sup>
$\lambda_i$	Loss rate of compartment $i$	$(0, 1)$	day <sup>-1</sup>
$k_i$	Turnover rate of compartment $i$	$(0, 1)$	day <sup>-1</sup>
$\pi_i$	Active (i.e., nonrefractory) portion of compartment $i$	$(0, 1)$	1
$\eta$	Coefficient of variation of the isotopic proportions $z_{i,j}$	$(0, 1)$	1
Derived parameters:			
$\hat{X}_i$	Expected steady-state biomass of compartment $i$	$(0, \infty)$	mgN m <sup>-2</sup>
$T_i$	Turnover time of the active portion of compartment $i$	$(0, \infty)$	day
$T'_i$	Apparent turnover time of compartment $i$	$(0, \infty)$	day
$F_{i,j}$	Flux between compartment $j$ and $i$	$(0, \infty)$	mgN m <sup>-2</sup> day <sup>-1</sup>
$F_T$	Total nutrient flux	$(0, \infty)$	mgN m <sup>-2</sup> day <sup>-1</sup>
$P_{ij}^U$	Proportion of compartment $i$ 's total uptake coming from $j$	$(0, 1)$	1
$P_{ij}^K$	Proportion of compartment $j$ 's turnover due to uptake by $i$	$(0, 1)$	1

element  $\psi_{ij}$  defines the probability that an atom of nutrient in compartment  $j$  at time  $t$  finds itself in compartment  $i$  at time  $t + 1$ . Some of the compartments, such as the inorganic nutrient forms, may receive external inputs between  $t$  and  $t + 1$ , which can be defined as nonzero elements in a  $C \times 1$  vector of external inputs  $\mathbf{y}^{(t)} = \{y_1^{(t)}, y_2^{(t)}, \dots, y_N^{(t)}\}$  defined by input functions  $f_i: t \rightarrow y_i^{(t)}$ . Given this, we can project the distribution of nutrients from time  $t$  to  $t + 1$  using the equation

$$\mathbf{x}^{(t+1)} = \Psi \cdot \mathbf{x}^{(t)} + \mathbf{y}^{(t)}. \tag{1}$$

This is a discretized form of the linear donor-controlled compartment model proposed by Mulholland and Keener (1974). The transition probabilities  $\psi_{ij}$  in  $\Psi$  are determined by two processes: nutrient uptake and nutrient loss. Uptake rates determine the probability that a nutrient atom moves from compartment  $j$  to  $i$  in one time step and are defined as  $v_{ij} > 0$  for every pair of compartments, where compartment  $i$  uses compartment  $j$  as a source of nutrient. Loss rates  $\lambda_j$  represent the probability that a nutrient atom leaves compartment  $j$  within one time step without being taken up by any other compartment, thus exiting the modeled ecosystem. The turnover rate  $k_j$  of a given compartment  $j$  (i.e., the proportion of nutrient exiting a given compartment per unit time) will be determined by the sum of the proportion consumed by other compartments and the proportion lost  $\lambda_j$ :

$$k_j = \lambda_j + \sum_{i=1}^C v_{ij}. \tag{2}$$

In other words, equation (1) is equivalent to stating that the nutrient dynamics of any given compartment  $j$  is described by the time-specific change in nutrient content:

$$\Delta x_j^{(t)} = \sum_{1 \leq i \leq C, i \neq j} v_{ji} x_i^{(t)} - k_j x_j^{(t)} + y_j^{(t)}, \tag{3}$$

which can be simplified in the case where  $y_j^{(t)} = 0$  (i.e., no external input for compartment  $j$ ) to

$$\Delta x_j^{(t)} = \sum_{1 \leq i \leq C, i \neq j} v_{ji} x_i^{(t)} - k_j x_j^{(t)}. \tag{4}$$

For example, let us consider a simple ecosystem with four compartments: an inorganic nutrient pool, a primary producer, a herbivore that consumes the primary producer, and an omnivore that feeds on both the primary consumer and the herbivore (fig. 1). Such system would be defined by the following  $4 \times 4$  transition matrix:

$$\Psi = \begin{bmatrix} 1 - k_1 & 0 & 0 & 0 \\ v_{2,1} & 1 - k_2 & 0 & 0 \\ 0 & v_{3,2} & 1 - k_3 & 0 \\ 0 & v_{4,2} & v_{4,3} & 1 - k_4 \end{bmatrix} \tag{5}$$

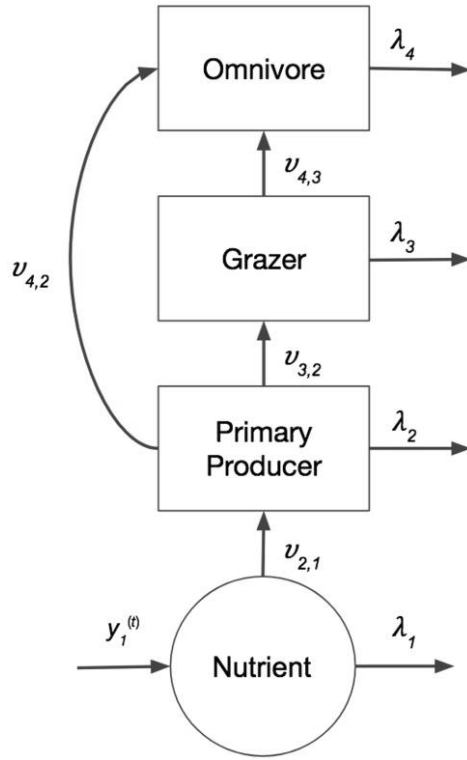


Figure 1: Schematic example/representation of a hidden Markov model and food web matrix.

and an exogenous input vector  $\mathbf{y}^{(t)} = \{y_1^{(t)}, 0, 0, 0\}$ . Note that if we assume the concentration of inorganic nutrient to be at a steady-state equilibrium ( $x_1^{(t)} = x_1^{(t_0)}$  does not depend on time), it must fulfill that

$$\forall t, \quad \frac{\Delta x_1^{(t)}}{\Delta t} = 0 \Leftrightarrow y_1^{(t)} - k_1 x_1^{(t)} = 0 \tag{6}$$

$$\Leftrightarrow y_1^{(t)} = (v_{2,1} + \lambda_1) x_1^{(t_0)}; \tag{7}$$

thus,  $y_1$  does not depend on  $t$ . Note also that it is straightforward to modify these equations describing a discrete-time system to describe a continuous-time system. In this case, equation (1) becomes

$$\frac{d\mathbf{x}^{(t)}}{dt} = \Psi \cdot \mathbf{x}^{(t)} + \mathbf{y}^{(t)}, \tag{8}$$

with  $\Psi \cdot \mathbf{x}^{(t)}$  and  $\mathbf{y}^{(t)}$  describing instantaneous transition rates and input rates, respectively, instead of transition probabilities and input per time step. Equation (8) is basically a system of inhomogeneous linear differential equations (which simplifies into a homogeneous system if  $\mathbf{y}^{(t)} = 0$ ). The transition matrix  $\Psi$  for a continuous-time



model corresponding to the ecosystem shown in figure 1 becomes (compare with eq. [5])

$$\Psi = \begin{bmatrix} -k_1 & 0 & 0 & 0 \\ v_{2,1} & -k_2 & 0 & 0 \\ 0 & v_{3,2} & -k_3 & 0 \\ 0 & v_{4,2} & v_{4,3} & -k_4 \end{bmatrix}. \quad (9)$$

The choice between a discrete and a continuous model depends on the biology of the system under study. We use a continuous model in the case study of Trinidadian montane streams presented below.

In the case of tracer addition experiments, the aim is to increase the exogenous input of a tracer (or marked) nutrient population and track the changes in the ratio between marked and unmarked nutrient (atomic ratio, in the case of isotope tracers). The addition of marked nutrient should cause a significant enrichment of the proportion of marked nutrient in water yet a marginal increase in the total amount of nutrient in water. This can be achieved, for example, by using rare isotopic forms (e.g., <sup>15</sup>N, <sup>13</sup>C, <sup>18</sup>O, or <sup>2</sup>H) that occur at extremely low proportions in nature. To model this, it is therefore necessary to follow two subpopulations of nutrient atoms: a tracer (or marked) population, usually the heavy isotopic form, and an unmarked population, defined by vectors  $\mathbf{m}^{(t)} = \{m_1^{(t)}, \dots, m_C^{(t)}\}$  and  $\mathbf{n}^{(t)} = \{n_1^{(t)}, \dots, n_C^{(t)}\}$ , respectively, which add up to the total nutrient population  $\mathbf{x}^{(t)} = \mathbf{n}^{(t)} + \mathbf{m}^{(t)}$ . The proportion of tracer can then be defined as

$$\mathbf{z}^{(t)} = \mathbf{m}^{(t)} \oslash \mathbf{x}^{(t)}, \quad (10)$$

where  $\oslash$  stands for the element-by-element division, also known as Hadamard division. Similarly, the exogenous input comprises marked  $\mathbf{y}_m^{(t)}$  and unmarked  $\mathbf{y}_n^{(t)}$  portions, such that  $\mathbf{y}^{(t)} = \mathbf{y}_n^{(t)} + \mathbf{y}_m^{(t)}$ . In a tracer addition experiment, the marked nutrient should be at much lower concentration than the unmarked nutrient, such that  $\mathbf{y}_m^{(t)} \ll \mathbf{y}_n^{(t)}$ , and therefore  $\mathbf{y}^{(t)} \approx \mathbf{y}_n^{(t)}$ .

The schedule of tracer addition is reflected in the exogenous input vector of marked material  $\mathbf{y}_m^{(t)}$  and usually consists of a period of increased input for one or two inorganic nutrient pools (e.g.,  $\text{NH}_4^+$  or  $\text{NO}_3^-$ ) followed by a period of background input (although other experimental designs, such as repeated pulses, can be easily defined). The exogenous input for the unmarked population  $\mathbf{y}_n^{(t)}$  is normally assumed constant.

Once we have an expected realization of the biological process model, the observation process can be modeled as sampling and measurement error around that expectation. The observed proportion of marked tracer in any given compartment  $i$  at time  $t$  can be modeled as a gamma distribution, which fulfills the multiplicative properties of proportions and allows for the skewed distribution typical

of low-concentration data. We parameterized the gamma distribution with the projected mean  $z_i^{(t)}$  and a coefficient of variation  $\eta$  shared across compartments, such that the observed proportion  $z_{\text{obs},i}^{(t)}$  follows (using Gamma\* to denote the nonstandard gamma parameterization):

$$z_{\text{obs},i}^{(t)} \sim \text{Gamma}^*(z_i^{(t)}, \eta). \quad (11)$$

This is equivalent to modeling gamma distributions with shape parameter  $\alpha_i = \eta^{-2}$  and rate parameter  $\beta_i = (z_i^{(t)} \cdot \eta^2)^{-1}$ . Although the gamma distribution can hypothetically reach values larger than 1, the expected isotopic proportions are extremely low, and therefore the probability density for values higher than 1 is negligible.

We will assume the total biomass of nitrogen  $x_i$  in compartment  $i$  to be approximately constant throughout the experiment, following a truncated normal distribution. This assumes additive properties and allows for zero values of biomass, which can occur for a given compartment in some sampling points. We note the truncated normal distribution with a mean  $x_i^{(t0)}$  (the initial biomass of compartment  $i$ ) and a compartment-specific standard deviation SD <sub>$i$</sub> :

$$x_i^{(t)} \sim \text{TNorm}_{\text{lower}=0}(x_i^{(t0)}, \text{SD}_i). \quad (12)$$

#### Overenriched Compartments

The model as formulated above assumes that the tracer is well mixed and that consumers do not selectively feed on differently labeled subcomponents of the source compartment. If this is true, the tracer signature of a consumer cannot exceed the signature of the source compartment. In practice, however, it is not uncommon for a consumer's isotopic label to be higher than its resource (Newbold et al. 1983; Dodds et al. 2014). This is because some compartments, particularly detrital ones, consist of material in which only a proportion is biologically active and assimilating tracer during the experiment. If consumers selectively feed on active constituents and/or preferentially assimilate active fractions, their signature can become higher than the average of the resource compartment. For example, coarse benthic organic matter (CBOM) is largely biologically inactive, and nutrient uptake into leaf packs is associated with the biofilm surrounding it. While the average tracer signal measured on the whole compartment might be low, the biofilm can have a high tracer signature, and organisms selectively feeding on (or assimilating) that biofilm will become highly labeled.

To allow for this in the model, one can assume that the biomass of any given compartment  $i$  is split into two portions: an active one and a refractory one. The active portion takes up nutrients throughout the experiment and contributes to changes in  $x_i^{(t)}$  (both  $m_i^{(t)}$  and  $n_i^{(t)}$ ). The refractory portion has negligible nutrient uptake and turnover within

the time span of the experiment and thus does not contribute to changes in  $x_i^{(t)}$ . If we define a vector of active proportions for the  $C$  compartments  $\pi = \{\pi_1, \dots, \pi_C\}$  where  $0 < \pi_i < 1$  whenever compartment  $i$  is assumed to be nonhomogeneous, the apparent uptake rates  $v'_i$  and apparent turnover rate  $k'_i$  of the whole compartment will be:

$$v'_i = v_i \cdot \pi_i, \quad (13)$$

$$k'_i = k_i \cdot \pi_i. \quad (14)$$

In practice, this means that while the biological model (eq. [5]) runs only on the active portion of biomass, the observation model accounts for the total biomass. Newbold et al. (1983) preceded the present article in recognizing that the standing stocks of the actively cycling components (as well as transfer fluxes) can be estimated from the model's steady-state solution. Note that  $\pi$  bears a similar meaning to the estimates of exchangeable P in Newbold et al. (1983) and the inverse of multiplier  $M$  in Dodds et al. (2014).

### Model Fitting

Fitting the above HMM requires time series of the observed tracer proportions  $z_{obs,i}^{(t)}$  in each compartment and data on compartment biomasses  $x_{obs,i}^{(t)}$ . In isotope tracer studies where there is a heavy isotope (the marked tracer) and a light (unmarked) isotope, the amount of marked tracer will often be expressed as a  $\delta$  value. For example, in studies of nitrogen dynamics, the tracer is  $^{15}\text{N}$  (heavier than the naturally common  $^{14}\text{N}$ ), and data are obtained as  $\delta^{15}\text{N}$ , which for any given compartment  $i$  at time  $t$  is

$$\delta^{15}\text{N}_i^{(t)} = \left( \frac{R_i^{(t)}}{R_0} - 1 \right) \cdot 1,000, \quad (15)$$

where  $R_i^{(t)} = (^{15}\text{N}/^{14}\text{N})_i^{(t)}$  is the isotopic ratio in compartment  $i$  at time  $t$  and  $R_0$  is the isotopic ratio in a standard air sample (e.g., for  $^{15}\text{N}$  this is taken to be 0.003663). To fit the above-described model to these data, it is necessary to convert the  $\delta$  values to observed proportions. This can be done by expressing  $z_{obs,i}^{(t)}$  as a function of  $R_i^{(t)}$ ,

$$z_{obs,i}^{(t)} = \frac{m_i^{(t)}}{n_i^{(t)} + m_i^{(t)}} = \frac{^{15}\text{N}_i^{(t)}}{^{14}\text{N}_i^{(t)} + ^{15}\text{N}_i^{(t)}} = \frac{R_i^{(t)}}{R_i^{(t)} + 1},$$

and then using a rearrangement of equation (15) to replace  $R_i^{(t)}$  in the equation for  $z_{obs,i}^{(t)}$ :

$$z_{obs,i}^{(t)} = R_0 \left( \frac{\delta^{15}\text{N}_i^{(t)}}{1,000} + 1 \right) \left[ R_0 \left( \frac{\delta^{15}\text{N}_i^{(t)}}{1,000} + 1 \right) + 1 \right]^{-1}. \quad (16)$$

Given these data and an assumed system topology denoting which compartment pairs are assumed to be linked as consumer and resource (i.e., which off-diagonal elements  $\psi_{ij} > 0$ ), we can fit the model to the data using a Bayes-

ian framework. To do so, we need to define priors for all  $v_{ij} \geq 0$ ,  $0 \leq \pi_i \leq 1$ ,  $\lambda_i$ , and  $\eta$ . These can be uninformative (i.e., flat) distributions within the parameter bounds or informative priors if there is prior knowledge on these quantities. For parameters that are positive but for which no upper bound is known precisely a priori, a half-Cauchy distribution defined by its scale parameter (i.e., its median) is a reasonable choice. In the case study of Trinidadian montane streams presented below, we used half-Cauchy priors for the uptake rates from the inorganic input compartments, since those compartments are constantly being renewed with the stream flow. For uptake rates and loss rates from biotic compartments, we used (scaled) beta priors to impose a maximum rate while allowing more prior belief to be put in small rate values: for example, it is unreasonable to allow uptake or loss rates greater than 1 with our data, since this would indicate a replacement of the whole nitrogen content of a biotic compartment within 1 day. Hence, we started our modeling approach with the following weakly informative priors:

$$\begin{aligned} v_{ij} &\sim \text{Half-Cauchy}(\text{scale} = 250) \text{ for input compartments } j \in \mathcal{I}, \\ v_{ij} &\sim \text{Beta}(\alpha = 1, \beta = 3, \text{scale} = 1) \text{ for all other uptake rates } v_{ij} > 0, \\ \lambda_i &\sim \text{Beta}(\alpha = 1, \beta = 3, \text{scale} = 1), \\ \pi_i &\sim \text{Uniform}(0, 1) \text{ for all basal compartments } \pi_i < 1, \\ \eta &\sim \text{Half-Cauchy}(\text{scale} = 1), \end{aligned}$$

where  $\mathcal{I}$  defines the set of inorganic nutrient compartments. We adjusted them for some parameters after realizing from initial runs that they could be either too restrictive or too permissive, depending on the compartments:

$$\begin{aligned} v_{\text{eudan,CBOM}} &\sim \text{Beta}(\alpha = 1, \beta = 3, \text{scale} = 0.5), \\ v_{\text{lepto,seston}} &\sim \text{Beta}(\alpha = 1, \beta = 3, \text{scale} = 0.5). \end{aligned}$$

In the formulation above, we define  $X$  as following a scaled beta distribution  $\text{Beta}(\alpha, \beta, \text{scale})$  if  $X/\text{scale}$  follows a beta distribution  $\text{Beta}(\alpha, \beta)$ .

The likelihood  $\mathcal{L}$  of each observation  $z_{obs,i}^{(t)}$  is given by equation (11), and the joint log likelihood of all observations is given as the sum of logarithms of all individual likelihoods. To help identifiability, the model can be constrained so that the total nutrient biomass of each compartment  $x_i$  is randomly distributed with known constant mean and standard deviation  $\text{SD}_i$ , as described in equation (12). These values can be obtained from independent estimations of compartment-specific biomasses  $x_{obs,i}$ . The likelihood of each biomass  $x_i^{(t)}$  projected by the model is evaluated against this distribution at each time point where there is any observation  $z_{obs,i}^{(t)}$  in order to constrain the biomass change of the system compartments in the model. The posterior distribution of the parameters can be obtained by sampling the product of prior and likelihood using Markov chain Monte Carlo (MCMC) techniques (Geman and Geman 1984).

*Model Selection, Derived Properties,  
and Statistical Comparisons*

If there is uncertainty over the presence or absence of any given trophic link, it is possible to define and fit alternative models representing different hypothesized food web topologies  $\Psi_h$  differing in whether particular uptake rates  $v_{ij}$  are equal to zero. The model fits can then be compared using the deviance information criterion (DIC; Spiegelhalter et al. 2002), defined as

$$DIC = \bar{D} + p_D, \tag{17}$$

where  $D$  is the set of deviance values calculated from the log-likelihood value at each MCMC iteration as  $-2 \cdot \log \mathcal{L}$ ,  $\bar{D}$  is the mean deviance value, and  $p_D$  is the effective number of parameters in the model and can be calculated as  $\text{var}(D)/2$  (Gelman et al. 2003). The most parsimonious model will be the one with the lowest DIC. A DIC difference ( $\Delta DIC$ ) greater than 2 indicates some evidence for the model with a lower DIC, while substantial evidence would be indicated by  $\Delta DIC > 5$ . It is also possible to compare the proportional support for any given model  $\Psi_h$  as a DIC weight (Link and Barker 2010):

$$w_h = \frac{\exp(\Delta DIC_h/2)}{\sum_{g=1}^M \exp(\Delta DIC_g/2)}, \tag{18}$$

where  $h$  represents the model hypothesis in question,  $\Delta DIC_i$  is the DIC difference between the most parsimonious model and model  $i$ , and  $M$  represents the total number of models tested.

Any derived metric of the system, such as total uptake and residence times of different compartments or proportion of a given prey in a consumer's diet, can be calculated using the MCMC chains of the parameter estimates involved in the calculations. This will produce an equally sized MCMC chain from which to create the distribution of the metric and its uncertainty (e.g., 95% credible intervals). Similarly, one can compare estimates of parameters or derived metrics between streams by subtracting (or dividing) the MCMC chains of the two estimates and producing a distribution and credible intervals of the difference in the estimates. The 95% credible intervals of statistically significant differences should not overlap zero (or 1 for ratios).

**Case Study: Nitrogen Fluxes in Trinidadian  
Montane Streams**

*Study System and Experimental Methods*

As an empirical illustration of our statistical modeling framework, we showcase its use in a case study conducted in Trinidadian streams, using simultaneous  $^{15}\text{N}$  tracer isotope additions to evaluate the effects of an experimental manipulation of light availability on major food web fluxes.

These experiments were carried out in streams of the Northern Range of Trinidad: Upper La Laja (UL) and Lower La Laja (LL). The study reaches are 100 and 156 m long, respectively, and form part of a long-term experiment to study interactions between ecological and evolutionary processes (Travis et al. 2014). These data have been previously analyzed using current methodology in Collins et al. (2016), providing a good point of comparison between the current method and our proposed modeling.

Details on the experiment and sampling can be found in Collins et al. (2016). In summary, we established a continuous drip of a solution of  $^{15}\text{N}$ -labeled ammonium (as dissolved  $^{15}\text{NH}_4\text{Cl}$ ) on the upstream end of each stream with a rate of  $10 \text{ mL min}^{-1}$  over a 10-day period from March 7 to 16, 2010. The N injections increased the  $\delta^{15}\text{N}$  of dissolved ammonium to approximately 20,000, yet the concentration of ammonium added was below 5% of ambient  $\text{NH}_4$  and thus did not enrich the stream. We sampled the biomass of food web compartments and water chemistry at approximately 15, 30, and 60 m downstream, in both pool and riffle habitat, on days 3, 7, and 10 of the injection and on days 13, 17, 20, 30, and 40 postinjection. The sampled food web compartments include water chemistry ( $\text{NH}_4^+$  and  $\text{NO}_3^-$ ), basal resources (epilithon, seston, fine benthic organic matter [FBOM], and CBOM), eight common invertebrate taxa representing all major functional feeding groups including grazers (*Petrophila* and *Psephenus*), filterers (*Leptonema*), collectors (*Tricorythodes*, *Phylloicus*, and *Eudaniela*), and predators (*Argia* and *Euthyplocia*). For simplicity, fish were not included in this illustrative analysis. For each of the 14 compartments we analyzed the isotopic ratio ( $\delta^{15}\text{N}$ ) of the samples obtained through time and estimated the standing biomass of each compartment in mass of nitrogen per square meter at three points in time. We also collected background samples from each compartment, either before the experiment or upstream from the injection, to estimate background isotopic values. We detail the analytical methods in the appendix (available online).

*Model Specification and Selection*

The Trinidadian stream web modeled is composed of the 14 compartments described above. Therefore, the distribution of nitrogen biomasses at any given time  $t$  is described by the vector

$$\mathbf{x}^{(t)} = \{x_{\text{NH}_4}^{(t)}, x_{\text{NO}_3}^{(t)}, x_{\text{epi}}^{(t)}, x_{\text{ses}}^{(t)}, x_{\text{FBOM}}^{(t)}, x_{\text{CBOM}}^{(t)}, x_{\text{pet}}^{(t)}, x_{\text{pse}}^{(t)}, x_{\text{lep}}^{(t)}, x_{\text{tri}}^{(t)}, x_{\text{eud}}^{(t)}, x_{\text{phy}}^{(t)}, x_{\text{arg}}^{(t)}, x_{\text{eut}}^{(t)}\},$$

which can be projected following the system of differential equations shown in equation (8), given a transition matrix  $\Psi$  of trophic relationships. Given the uncertainty of some trophic links, we test eight variations of the food web structure assumed by Collins et al. (2016), which corresponds to the matrix shown in box 1.



**Box 1: Transition matrix describing the food web structure assumed by Collins et al. (2016)**

$$\Psi_{111} = \begin{bmatrix} \psi_{1,1} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \psi_{2,2} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ u_{\text{epi},\text{NH}_4} & u_{\text{epi},\text{NO}_3} & -\lambda_{\text{epi}} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ u_{\text{ses},\text{NH}_4} & u_{\text{ses},\text{NO}_3} & 0 & -\lambda_{\text{ses}} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ u_{\text{FBOM},\text{NH}_4} & u_{\text{FBOM},\text{NO}_3} & 0 & 0 & -\lambda_{\text{FBOM}} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ u_{\text{CBOM},\text{NH}_4} & u_{\text{CBOM},\text{NO}_3} & 0 & 0 & 0 & -\lambda_{\text{CBOM}} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & u_{\text{pet},\text{NO}_3} & 0 & 0 & 0 & -\lambda_{\text{pet}} & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & u_{\text{pse},\text{NO}_3} & 0 & 0 & 0 & 0 & -\lambda_{\text{pse}} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & u_{\text{lep},\text{ses}} & 0 & 0 & 0 & 0 & -\lambda_{\text{lep}} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & u_{\text{tri},\text{FBOM}} & 0 & 0 & 0 & 0 & -\lambda_{\text{tri}} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & u_{\text{eud},\text{CBOM}} & 0 & 0 & 0 & 0 & -\lambda_{\text{eud}} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & u_{\text{phy},\text{CBOM}} & 0 & 0 & 0 & 0 & 0 & -\lambda_{\text{phy}} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & u_{\text{arg},\text{lep}} & u_{\text{arg},\text{tri}} & 0 & 0 & -\lambda_{\text{arg}} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & u_{\text{eut},\text{phy}} & 0 & -\lambda_{\text{eut}} \end{bmatrix}$$

Because the dynamics of the two inorganic element compartments,  $\text{NH}_4^+$  and  $\text{NO}_3^-$ , occur at much faster rates than the rest, the system can be numerically approximated by assuming that they are completely regenerated at each infinitesimal time step and driven by external inputs—or, in other words, that they are completely replaced by the flux from upstream. Note that this assumption does not imply that the system modeled is completely open but is merely a mathematical simplification that treats water nutrient as a given in order to simplify the estimation. This can be mathematically expressed by setting  $\psi_{1,1} = \psi_{2,2} = 0$  and by replacing after each step of the numerical integration of the system of differential equations the elements  $x_1$  and  $x_2$  of  $\mathbf{x}$  with values that reflect the measured profiles for  $\text{NH}_4^+$  and  $\text{NO}_3^-$  at sampling point  $s$ . In our example, we have three sampling points (transects) per stream.

Given this, we can model the two parallel subsystems comprising  $\mathbf{x}$ : unmarked nutrient  $\mathbf{n}$  and marked nutrient  $\mathbf{m}$ , representing the dynamics of each isotope. While both systems will be governed by the same transition matrix  $\Psi$ , they have different initial values  $\mathbf{n}^{(0)}$  and  $\mathbf{m}^{(0)}$  corresponding to the background isotopic ratios before the drip experiment has started. The inorganic nutrient compartments also have different forced input profiles between unmarked and marked nutrient pools. The forced quantity of unmarked tracer in the inorganic compartments is constant through time, such that

$$n_i^{(s,t)} = {}^{14}\text{N}_{i,\text{bkg}}^{(s)} \quad \text{for } i \in \mathcal{I} \text{ and all } t \text{ values,} \quad (19)$$

where  $\mathcal{I}$  defines the set of inorganic nutrient compartments ( $\text{NH}_4^+$  and  $\text{NO}_3^-$ ) and  ${}^{14}\text{N}_{i,\text{bkg}}^{(s)}$  is the natural (background) abundance of  ${}^{14}\text{N}$  ( $\text{mgN m}^{-2}$ ) in the inorganic nutrient compartment  $i$  measured at sampling transect  $s$ .

On the contrary, the forced quantity of marked nutrient in the inorganic compartments changes with the experimental enrichment profile. This means that if we define  $t_{\text{off}}$  as the time the drip is turned off, then the following step function drives  $m_i^{(s,t)}$ :

$$m_i^{(s,t)} = \begin{cases} {}^{15}\text{N}_{i,\text{bkg}}^{(s)} + {}^{15}\text{N}_{i,\text{add}}^{(s)} & \text{for } i \in \mathcal{I} \text{ and } t < t_{\text{off}}, \\ {}^{15}\text{N}_{i,\text{bkg}}^{(s)} & \text{for } i \in \mathcal{I} \text{ and } t \geq t_{\text{off}}. \end{cases} \quad (20)$$

Here,  ${}^{15}\text{N}_{i,\text{bkg}}^{(s)}$  represents the natural (background) abundance of the heavy isotope ( ${}^{15}\text{N}$ ) form of the inorganic nutrient compartment measured at sampling transect  $s$  before nutrient addition, and  ${}^{15}\text{N}_{i,\text{add}}^{(s)}$  is the additional  ${}^{15}\text{N}$  measured during the experimental addition at sampling transect  $s$ .

We tested eight topological model structures of the network  $\Psi_h$  representing the variations of  $\Psi_{111}$  where one or more of three uncertain links were eliminated. The uncertain links corresponded to the uptake of FBOM by the *Eudaniela* crabs and predation of *Psephenus* waterpennies and *Petrophila* caterpillars by *Argia* damselflies (table 2).

We fit the models to the data on Lower and Upper La Laja using transect- and compartment-specific time series of isotopic proportions  $z_{\text{obs},i}^{(s,t)}$  as well as compartment-specific biomass data  $x_{\text{obs},i}^{(s,t)}$  at three points in time  $t$  and three points in space  $s$ . Latent biomasses  $x_i$  were assumed to be constant (i.e., at steady state); therefore, sample differences were considered to be random with observed standard deviation  $\text{SD}_i$ . In practice, this allows for deviations of the steady-state assumption that are within the range of the compartment's natural variation.

We fit the model in R version 3.6 (R Core Team 2019) by implementing it in Stan (Carpenter et al. 2017) and running it with the RStan package (Stan Development Team 2019). Details on the model implementation and of the

**Table 2:** Comparison of alternative models of food web structure regarding *Argia* and *Eudaniella* diets

Model	Trophic link			No. parameters	DIC	ΔDIC	w <sub>DIC</sub>
	<i>Petrophila</i> → <i>Argia</i>	<i>Psephenus</i> → <i>Argia</i>	FBOM → <i>Eudaniella</i>				
Ψ <sub>100</sub>	Yes	No	No	68	-2,844.8	0	.757
Ψ <sub>110</sub>	Yes	Yes	No	70	-2,841.5	3.3	.146
Ψ <sub>000</sub>	No	No	No	66	-2,839.3	5.4	.05
Ψ <sub>010</sub>	No	Yes	No	68	-2,839.1	5.6	.046
Ψ <sub>111</sub>	Yes	Yes	Yes	72	-2,830	14.8	0
Ψ <sub>011</sub>	No	Yes	Yes	70	-2,828.2	16.6	0
Ψ <sub>101</sub>	Yes	No	Yes	70	-2,823.9	20.8	0
Ψ <sub>001</sub>	No	No	Yes	68	-2,810.5	34.2	0

Note: DIC = deviance information criterion; FBOM = fine benthic organic matter.

priors used are described in supplementary material S1 (supplementary materials S1, S2 are available online). The data and the source code used in our study can be found as an R package in the Dryad Digital Repository (<https://doi.org/10.5061/dryad.8sf7m0chx>; López-Sepulcre et al. 2020).

We assumed that both streams have the same network topology of trophic links, albeit with different parameter values. We therefore calculated the joint DIC for both streams by adding the DICs of the same model fit to the two streams. We chose the best model as the one with the lowest joint DIC.

*Calculation of Derived Parameters*

After selecting the best model, we illustrate the calculation of some important derived metrics, their uncertainty, and their comparison between the natural (LL) and open canopy (UL) streams. To do so, one only has to apply the required calculation with all 1,000 sampled values of the MCMC chain rather than with the estimates of the parameters. This produces a probability distribution for the derived parameter, which can be used to calculate measures of dispersion, such as standard errors or 95% quantiles (i.e., credible intervals).

A common quantity of interest is the expected residence or turnover time  $T_j$  of nutrient N in each compartment  $j$ , which can be calculated as the inverse of the turnover rate:

$$T_j = \frac{1}{k_j} = \frac{1}{\lambda_j + \sum_{i=1}^C v_{ij}}. \tag{21}$$

In the case of compartments divided into active and refractory subcompartments, the apparent residence time  $T'_j$  will be larger:

$$T'_j = \frac{1}{\pi_j k_j} = \frac{1}{\pi_j (\lambda_j + \sum_{i=1}^C v_{ij})} = \frac{T_j}{\pi_j}. \tag{22}$$

The flux rates between compartments can be calculated as

$$F_{ij} = v_{ij} \hat{X}_j, \tag{23}$$

where  $F_{ij}$  represents the flux from compartment  $j$  to compartment  $i$  and  $\hat{X}_j$  is the expected biomass. Because we assume the system to be at steady state, expected biomasses can be calculated using an eigenanalysis of the system as follows. Under steady state, the two nutrient forms  $\text{NH}_4^+$  and  $\text{NO}_3^-$  ought to remain constant, which we can achieve by defining a transfer matrix  $\Psi'$  that equals  $\Psi$  but with  $\psi'_{1,1} = \psi'_{2,2} = 1$  and  $\psi'_{i,i} = 1 - k_i$  for the other compartments. This matrix will have at least two right eigenvectors  $\mathbf{v}^{(\text{NH}_4)}$  and  $\mathbf{v}^{(\text{NO}_3)}$  corresponding to an eigenvalue of 1, which are scaled to a norm of 1. The elements  $i$  of each of these  $14 \times 1$  vectors represent the relative equilibrium biomass of compartment  $i$  that originates from each of the two inorganic nutrients,  $\text{NH}_4^+$  and  $\text{NO}_3^-$ , respectively. Because the eigenvectors  $\mathbf{v}^{(\text{NH}_4)}$  and  $\mathbf{v}^{(\text{NO}_3)}$  are scaled to a norm of 1, they need to be rescaled on the basis of the mass of  $\text{NH}_4^+$  and  $\text{NO}_3^-$  in the water, respectively. The total equilibrium biomass  $\hat{X}_i$  of compartment  $i$  at steady state can thus be calculated as the sum elements  $i$  of the two rescaled vectors as follows:

$$\hat{X}_i = x_1 \frac{v_i^{(\text{NH}_4)}}{v_1^{(\text{NH}_4)}} + x_2 \frac{v_i^{(\text{NO}_3)}}{v_2^{(\text{NO}_3)}}, \tag{24}$$

where  $x_1$  and  $x_2$  are the background masses ( $\text{mgN m}^{-2}$ ) of  $\text{NH}_4^+$  and  $\text{NO}_3^-$  in the stream. It is worth noting that at steady state, it should be true that inputs should equal outputs, and therefore

$$F_{i..} = k_i \cdot \hat{X}_i \Leftrightarrow \hat{X}_i = F_{i..} \cdot T_i, \tag{25}$$

where  $F_{i..}$  is the total flux through compartment  $i$ :

$$F_{i..} = \sum_{j=1}^C F_{ij} \hat{X}_j. \tag{26}$$

The total flux of N through the system can then be calculated as the sum of fluxes from the set of nutrient input compartments  $\mathcal{I}$  (in our case,  $\text{NH}_4^+$  and  $\text{NO}_3^-$ ) to the set of basal compartments  $\mathcal{B}$  (in our case, epilithon, seston, FBOM, and CBOM):

$$F_T = \sum_{j \in \mathcal{I}} \sum_{i \in \mathcal{B}} F_{ij}. \quad (27)$$

Total flux is of interest as an indicator of whole-ecosystem productivity, and we expect it to be higher under higher light conditions (i.e., in Upper La Laja). A second metric of interest is the relative use of  $\text{NO}_3^-$  compared with  $\text{NH}_4^+$  by primary producers. Primary producers favor  $\text{NH}_4^+$  over  $\text{NO}_3^-$ , as a result of lower assimilation cost (Morris 1974). Because more productive streams have higher demand of N and greater energy supply, we expect primary producers in the high light stream to supplement their N need by assimilating nitrate and therefore have a higher ratio of  $\text{NO}_3^-$  flux to  $\text{NH}_4^+$  (Morris 1974). The proportion of N uptake flux into a given consumer compartment  $i$  coming from a given source compartment  $j$  can be calculated as

$$P_{ij}^U = \frac{v_{ij}x_j}{\sum_{r=1}^C v_{ir}x_r}. \quad (28)$$

We will calculate the proportional use of  $\text{NO}_3^-$  by epilithon ( $P_{\text{epi},\text{NO}_3}^U$ ) to test the above-described hypothesis of preferential  $\text{NH}_4^+$  use under light limitation. Note that this can also be expressed as a ratio of  $\text{NO}_3^-$  to  $\text{NH}_4^+$  use:

$$R_{\text{epi},\text{NO}_3} = \frac{P_{\text{epi},\text{NO}_3}^U}{1 - P_{\text{epi},\text{NO}_3}^U}. \quad (29)$$

Similarly, one can use  $P_{ij}^U$  to evaluate the importance of a particular compartment in the diet of a consumer. We illustrate this by calculating the importance of *Petrophila* water moths in the diet of *Argia* damselflies  $P_{\text{arg},\text{pet}}^U$ .

Conversely, we can calculate the contribution of a particular consumer  $i$  to the turnover of a given resource compartment  $j$  as

$$P_{ij}^K = \frac{v_{ij}}{k_j} = \frac{v_{ij}}{\lambda_j + \sum_{r=1}^C v_{rj}}. \quad (30)$$

As an example, we calculate the contribution of *Eudaniela* crabs to the turnover of CBOM,  $P_{\text{eud},\text{CBOM}}^K$ .

#### Derived Parameter Uncertainty and Statistical Comparisons

One of the main advantages of Bayesian inference through MCMC is that it is straightforward to carry out the estima-

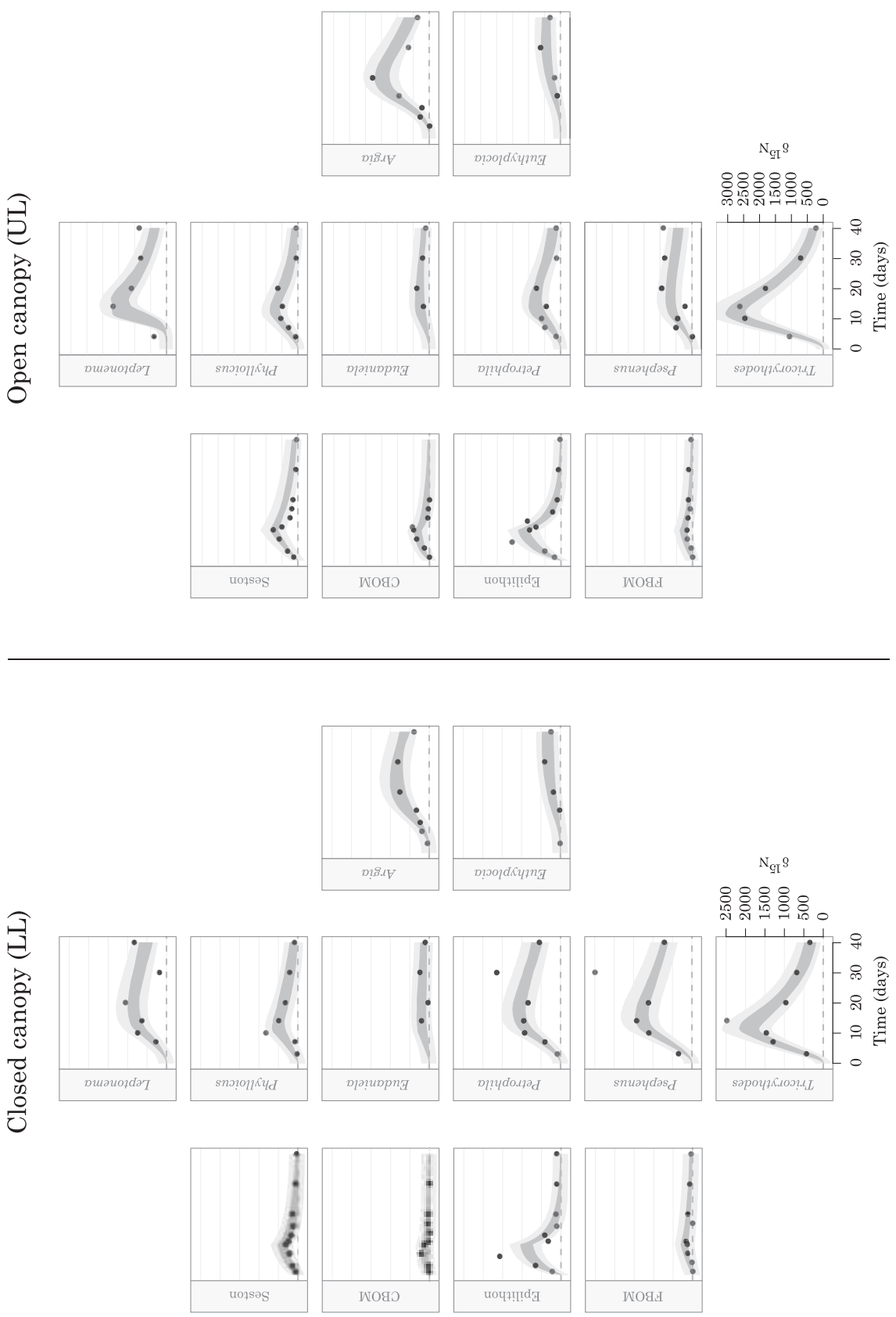
tion error on the primary parameters onto the derived parameters. This is done by simply applying the relevant calculation elementwise on the MCMC chains of the estimated parameters. This results in a posterior distribution of the derived parameter that naturally accounts for the error in all its component parameters. One can then calculate from the posterior distribution any relevant measure of uncertainty (e.g., standard error or credible intervals).

In the same manner, one can compare the parameter estimates between two streams by simply calculating the elementwise difference (or ratio, or any other measure of effect size) in the MCMC chains. A Bayesian posterior predictive  $P$  value for the difference can then be extracted by calculating the proportion of the posterior distribution that falls below zero (or 1, in the case of a ratio).

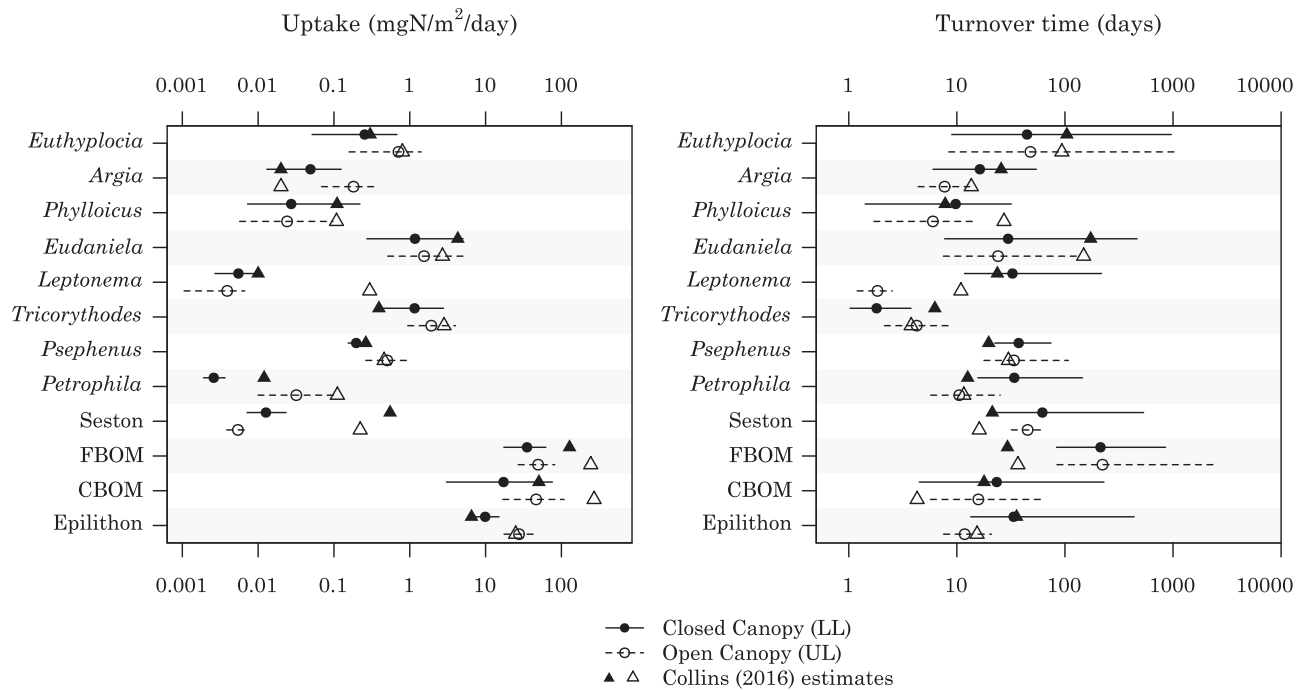
## Results

The most parsimonious network topology corresponded to model  $\Psi_{100}$ , which includes the consumption of *Petrophila* by *Argia* but not consumption of *Psephenus* by *Argia* nor FBOM by *Eudaniela* crabs (table 2). The second-best model was 3.3 DIC units away, indicating moderate support for the best model. However, the overall support for a *Petrophila*  $\rightarrow$  *Argia* link is higher if we consider all tested models. The sum of the DIC weights of all of the models including that link is 0.90 (out of 1), compared with only 0.19 for a *Psephenus*  $\rightarrow$  *Argia* link and  $<0.01$  for an FBOM  $\rightarrow$  *Eudaniela* link. We therefore present the results for model  $\Psi_{100}$ . Figure 2 shows the fit for isotope ratios for this model in both streams for the first transects (see fig. S1 for all transects and fig. S2 for biomass fit; figs. S1–S3 are available online), while the parameter estimates, credible intervals, MCMC chains, and posterior distributions can be found in table S1 and fig. S3).

To compare our proposed approach to current standard methodology, in figure 3 we compare our estimates of compartment fluxes and turnover times with estimates obtained in a previous analysis of the same data (Collins et al. 2016), using current methodology (Dodds et al. 2000). For basal compartments that are split into an active portion  $\pi_i$  and a refractory portion  $1 - \pi_i$ , apparent turnover times  $T_i'$  in our analyses (eq. [22]) are equivalent to the turnover times estimated in Collins et al. (2016). Fourteen of the 24 compartment uptake rates estimated by Collins et al. lie within the 95% credible intervals of our estimates, as 14 of the 24 turnover time estimates do. Relative to the estimates derived by our model, the estimates of Collins et al. tend to overestimate uptake in the basal compartments and underestimate it for some consumers, while the converse is true for turnover time. Differences between



**Figure 2:** Model fit for comparing data with credible and prediction envelopes. Solid circles are observed data, dark gray envelopes are 95% credible intervals, and light gray envelopes are 95% prediction intervals. Only data for the first transect of each stream are shown here. Profiles for all three transects can be found in figure S1. CBOM = coarse benthic organic matter; FBOM = fine benthic organic matter; LL = Lower La Laja; UL = Upper La Laja.



**Figure 3:** Estimates of uptake fluxes and turnover times of all compartments for Lower La Laja (LL; solid symbols) and Upper La Laja (UL; open symbols). Circles and error bars represent our estimates and 95% credible intervals. Triangles represent the estimates made by Collins et al. (2016). Turnover was not estimated for *Argia* or *Euthyplocia* in Collins et al. (2016). Note that the axis scale is logarithmic. CBOM = coarse benthic organic matter; FBOM = fine benthic organic matter.

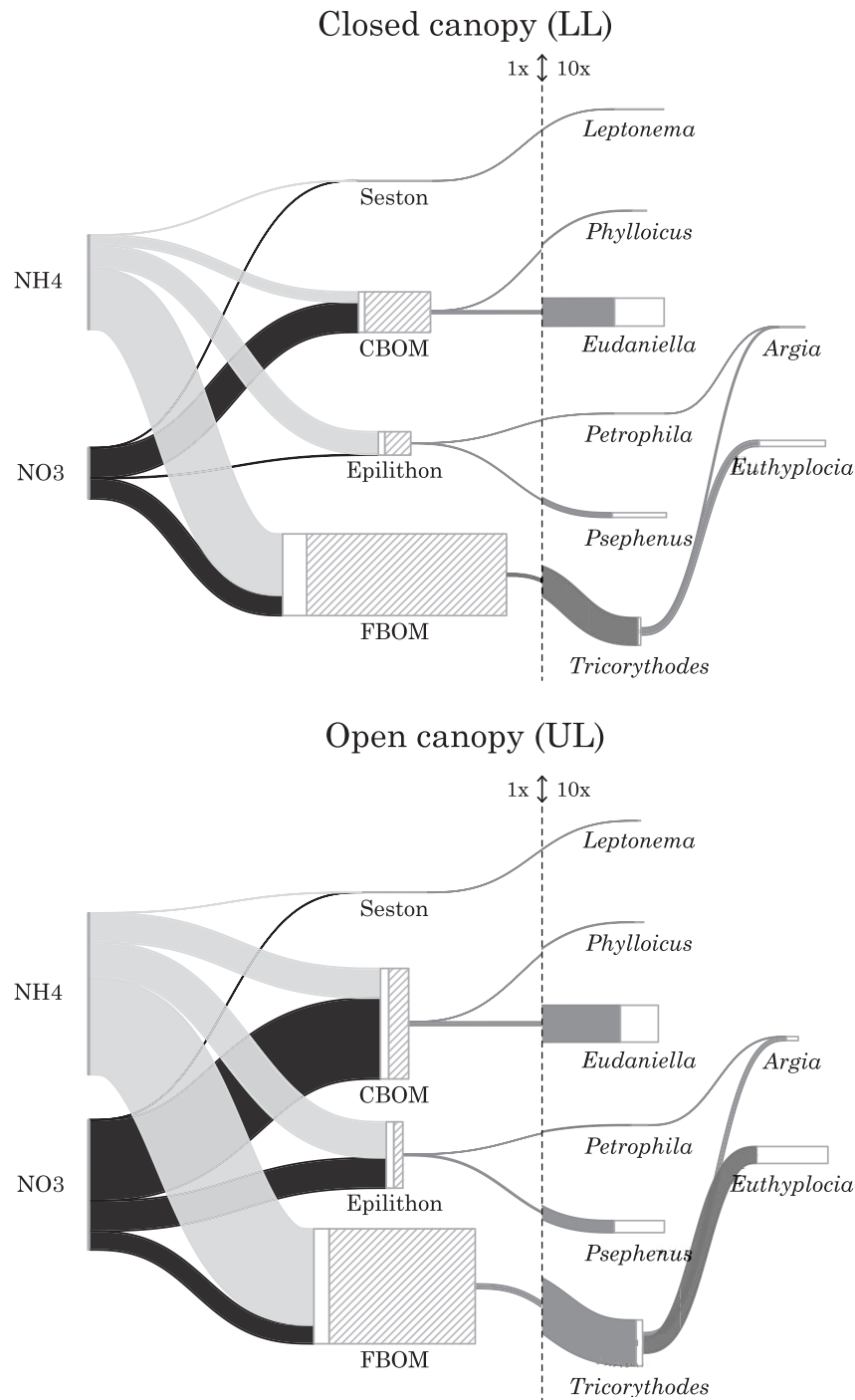
methods in estimates were often not trivial and in some cases varied by an order of magnitude (e.g., CBOM uptake or *Eudaniela* turnover). The negative relationship between the bias of uptake and turnover time is expected, given that an overestimate of uptake must be balanced by decreased turnover time in order to explain the same concentration of tracer in a given compartment.

The estimates and 95% credible intervals of all fluxes among compartments, turnover times, and expected steady-state biomasses are found in supplementary material S2 (tables S2, S3) and represented in figure 4. This figure summarizes the three main aspects of nitrogen dynamics across compartments: fluxes between compartments, turnover (or residence) times, and compartment biomasses. Basal compartments are divided into their active (solid white) and refractory (hatched) portions as estimated by  $\pi_i$ , with  $T_i$  and  $T'_i$  represented by the width of the white solid portion of the box and the total width of the box, respectively. As expected, active portions of basal compartments tend to be larger in the open canopy stream than the closed canopy stream, particularly for epilithon ( $(\pi_{\text{epi}})^{\text{LL}} = 0.13 \pm 0.07$ ,  $(\pi_{\text{epi}})^{\text{UL}} = 0.44 \pm 0.12$ ) and CBOM ( $(\pi_{\text{CBOM}})^{\text{LL}} = 0.30 \pm 0.14$ ,  $(\pi_{\text{CBOM}})^{\text{UL}} = 0.50 \pm 0.13$ ; values given as mean  $\pm$  SD; table S1). Another clear and expected pattern that emerges

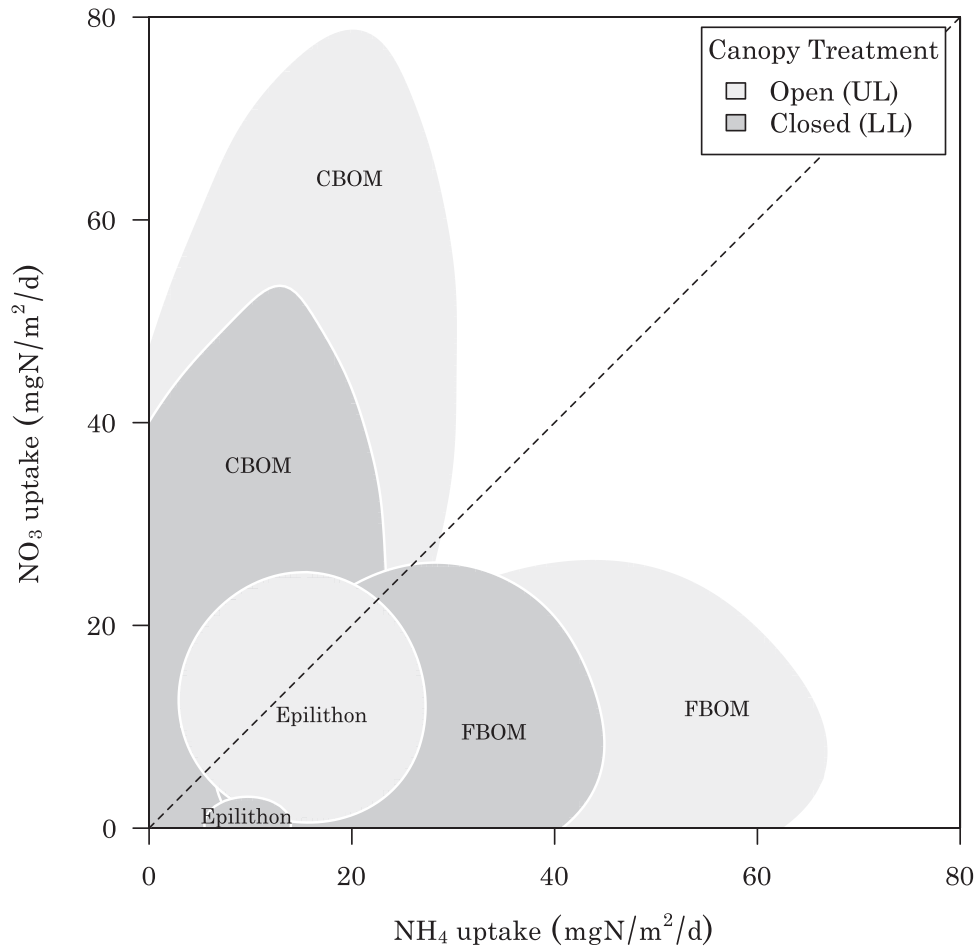
from figure 4 is the overall higher fluxes into the basal compartments in the open canopy stream. This is illustrated in figure 5 and is in good part due to an increased  $\text{NO}_3^-$  uptake by epilithon and CBOM. In contrast, the increase in N uptake by FBOM is mostly due to increased  $\text{NH}_4^+$  uptake.

A consistent pattern across our analyses was the high uncertainty associated with estimates of fluxes, turnover, and other derived parameters. Despite this quantitative uncertainty, it is possible to make important statistical inferences regarding differences among compartments and between streams. Total flux is higher in the open canopy than the closed canopy stream ( $(F_T)^{\text{UL}} - (F_T)^{\text{LL}} = 63.7 \pm 35.9$ , one-sided Bayesian  $P = .036$ ; fig. 6A), and epilithon's uptake shows a higher ratio of  $\text{NO}_3^-$  to  $\text{NH}_4^+$  uptake ( $\log[(R_{\text{epi},\text{NO}_3})^{\text{UL}}] - \log[(R_{\text{epi},\text{NO}_3})^{\text{LL}}] = 3.54 \pm 1.51$ ;  $P = .008$ , fig. 6B), as expected. Although there seems to be a higher contribution of *Eudaniela* crabs to CBOM turnover in the closed canopy stream, the parameters around *Eudaniela* are highly uncertain due to irregular sampling (crab captures are patchy), and this difference is not significant ( $\logit[(P_{\text{eud,CBOM}}^{\text{UL}})] - \logit[(P_{\text{eud,CBOM}}^{\text{LL}})] = -1.02 \pm 1.74$ ;  $P = .28$ ; fig. 6C). A clearer but still nonsignificant result is that *Petrophila* moths seem to represent a higher proportion of the diet of *Argia* damselflies in our high light stream





**Figure 4:** Quantitative food web reconstruction of the two streams. Compartments are represented by boxes, and fluxes between them are represented by filled curved lines connecting them. The white box area represents the active portion of the compartment  $\pi_i$ , while the gray hatched area on the basal compartments represents the nonactive (refractory) proportion  $(1 - \pi_i)$ . Curve thickness is proportional to the flux rate calculated following equation (23). The height of all nonnutrient compartment boxes is therefore proportional to the total uptake of N by that compartment. Box widths of nonnutrient compartments are proportional to the compartment's turnover time, with the width of the white area representing the turnover time of the active component and the total width representing the overall turnover time. The area of the box is therefore proportional to the compartment's biomass under the steady-state assumption (as per eq. [25]). Note that the fluxes and biomasses have been magnified by  $\times 10$  on the right side of the figure in order to visualize differences between streams. CBOM = coarse benthic organic matter; FBOM = fine benthic organic matter; LL = Lower La Laja; UL = Upper La Laja.



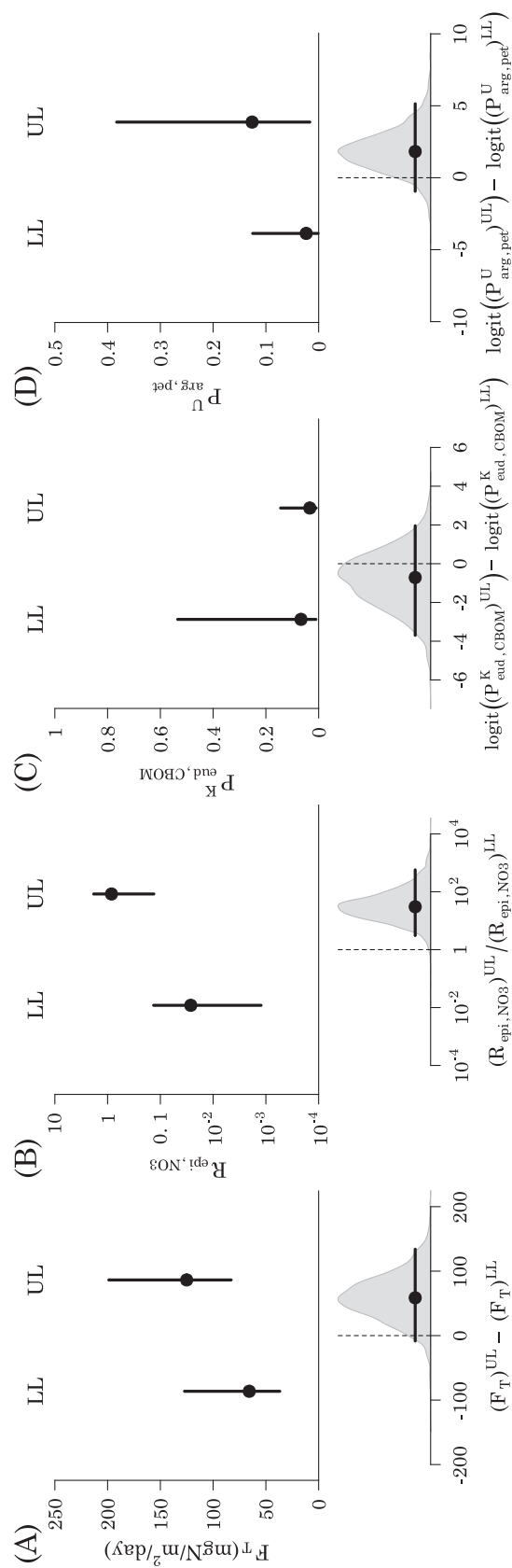
**Figure 5:** Distribution of total  $\text{NH}_4^+$  and  $\text{NO}_3^-$  uptake among the three main basal compartments. Gray areas represent 95% credible bounds. The dashed isoline indicates equal uptake of  $\text{NH}_4^+$  and  $\text{NO}_3^-$ , with estimates above it indicating a dominance of  $\text{NO}_3^-$  uptake over  $\text{NH}_4^+$ . Estimated values can be seen in table S3. Seston uptake is not visible because it is very close to zero and has small credible bounds. CBOM = coarse benthic organic matter; FBOM = fine benthic organic matter; LL = Lower La Laja; UL = Upper La Laja.

$(\text{UL} > \text{LL}, \text{logit}[(P_{\text{arg,pet}}^{\text{UL}})^{\text{UL}}] - \text{logit}[(P_{\text{arg,pet}}^{\text{LL}})^{\text{LL}}]) = 1.48 \pm 1.43; P = .13; \text{fig. } 6D).$

### Discussion

We have presented a statistical formalization of a tracer addition to track nutrient movement through an ecosystem. As such, this is the first evaluation of the uncertainty involved in the estimation of uptake and turnover using these experiments. Quantifying and managing such uncertainty is important in these experiments because of the limited amount of data involved and because they measure phenomena that propagate across scales. Beyond accounting for sampling error, our method can handle three important sources of error or bias that were previously suboptimally handled. First, modeling the system as a whole ensures that the interdependence of parameter estimates among com-

partments becomes explicit, and thus the error in the estimates of nitrogen dynamics of a particular compartment is incorporated in the estimation of the compartments that consume it. In the past, this kind of error propagation has been ignored (Dodds et al. 2000). Second, it is now possible to model diet uncertainty at two levels: topological and quantitative. By topological uncertainty we refer to the uncertainty regarding the presence or absence of a particular trophic link. By modifying the topology of the transfer matrix  $\Psi$  (i.e., changing which of its elements  $\psi_{ij}$  are different from zero), one can explicitly test different hypotheses regarding the trophic structure of the ecosystem using model selection techniques and either select the best model or average across models using model averaging. We have illustrated how to do so using the DIC (Spiegelhalter et al. 2002), but other Bayesian techniques, such as reversible-jump MCMC (Green 1995) or variable selection methods,



**Figure 6:** Statistical comparisons of derived parameters between streams. Each panel is composed of two plots: an upper plot with the estimate (and 95% credible interval) for both streams side by side, and a lower plot with the distribution of the difference (or ratio) and its 95% credible interval. Each panel corresponds to a derived parameter: A, total N flux  $F_T$ ; B, ratio of  $\text{NO}_3^-$  to  $\text{NH}_4^+$  uptake by epilithon  $R_{\text{epi},\text{NO}_3}$ ; C, proportion of *Petrophila* N in the diet of *Argia*  $P_{\text{arg},\text{pet}}^K$ ; D, contribution of *Eudaniela* consumption to coarse benthic organic matter (CBOM) turnover  $P_{\text{end,CBOM}}^K$ . FBOM = fine benthic organic matter; LL = Lower La Laja; UL = Upper La Laja.

can be implemented (for reviews on available methods, see Tenan et al. 2014; Hooten and Hobbs 2015). By quantitative uncertainty we refer to the diet of organisms with more than one food source. Past models required the input of assumed proportions of each source. This is not necessary in our approach, and the proportion of each resource consumed (and its uncertainty) can be calculated as a derived parameter after the model fit (see eq. [29]). Finally, our method offers a solution to the paradox of overenrichment, whereby consumer compartments appear more labeled than their sources (Dodds et al. 2014). It does so by allowing the partitioning of resource compartments into an active portion  $\pi$ , that uptakes detectable marked nutrient during the time frame of the experiment and a refractory one that does not (or does so at much larger timescales). Because this portion is an estimated parameter, its uncertainty is evaluated, which is an advantage over the post hoc multiplicative factor approach previously proposed (Dodds et al. 2014).

All of the above-mentioned sources of uncertainty get integrated to produce the uncertainty in the posterior distribution of the evaluated parameters. As exemplified by our case study, this uncertainty can sometimes be rather large, which is not surprising given the typically high dimensionality of these systems and the limited amount of data (due to the high cost of isotopic analysis and the need to minimize invasiveness). This highlights further the importance of measuring and reporting the uncertainty in the estimated parameters in order to temper our statements on the results. One of the advantages of our Bayesian implementation is that it can incorporate prior knowledge to help reduce this uncertainty, a strategy increasingly used in ecological management (McCarthy and Masters 2005). This can be in the form of supplementary experiments on specific organisms or published values on similar taxa and systems. Moreover, it is possible to evaluate the influence of prior information using prior sensitivity analysis and therefore formally evaluate the contribution of our data to the increase (or decrease) of certainty in the studied parameters. Ultimately, our method can be used on simulated data prior to an experiment in order to test the power of alternative experimental designs regarding the dripping regime and the sampling schedule of each compartment. In our opinion, this is one of the most powerful advantages of having a formal statistical framework available for isotope tracer experiments. While a full exploration of different designs is beyond the scope of this article, two important aspects of the design that are important to parameter identifiability seem apparent to us. First, it is necessary to have good temporal resolution of samples where uptake of tracer changes slope significantly (e.g., at peak uptake). Second, if more than one nutrient is labeled (as is the case here with both forms of nitrogen), it is important that their labeling is not strongly positively correlated if one is to dis-

tinguish differential uptake of each source. In our example, the dynamics of nitrification ensure that as  $^{15}\text{NH}_4^+$  label decreases downstream,  $^{15}\text{NO}_3^-$  increases, allowing us to tease apart  $^{15}\text{NH}_4^+$  from  $^{15}\text{NO}_3^-$  uptake.

Despite large uncertainties around some parameter values, we were able to identify some important expected differences in the functioning of the two study streams. For example, basal (and total fluxes) are higher in the open canopy stream (fig. 6A), as expected by the limiting effect of light in forested streams (Vannote et al. 1980). This result is consistent with previous analyses (Collins et al. 2016) and with other contemporary work at the same study sites that show an increase in chlorophyll *a* abundance with light (Kohler et al. 2012) and increased gross primary production in the open canopy stream (A. O. H. C. Leduc, S. A. Thomas, A. López-Sepulcre, et al., unpublished manuscript). Our analysis also clearly shows a higher ratio of  $\text{NO}_3^-$  to  $\text{NH}_4^+$  use by epilithon in the open canopy stream (fig. 6B). This is consistent with the fact that  $\text{NH}_4^+$  is the preferred form of nitrogen to algae, and as light increases the higher nutrient demand drives algae to use other sources of nitrogen, such as  $\text{NO}_3^-$  (Morris 1974).

Our analysis also suggests potential biases in previous estimation methods that approximate postdrip  $^{15}\text{N}$  turnover by fitting an exponential decay curve (Collins et al. 2016). Previous estimates show higher consumer turnover times than our statistical implementation and, consequently, higher uptake rates too (in order to maintain the same observed  $^{15}\text{N}$  concentration). This could be due to the increasing difficulty of detecting a clear exponential decrease in the isotopic ratio with increasing trophic level. The converse pattern is true for basal compartments: our approach estimates higher turnover times and higher uptake rates than Collins et al. (2016). This may be a consequence of our splitting of basal compartments in active and refractory portions. In Collins et al. (2016) primary consumers need to eat a larger quantity of their resource to get enough  $^{15}\text{N}$  signal, while in our model they need to eat a lower biomass of the active portion, which has higher  $^{15}\text{N}$  concentration. Less consumption should result in lower turnover rates and higher turnover times. A full investigation of the potential biases of the different methods will require an intensive simulation approach.

Through our model selection exercise, we were also able to contrast some of the topological assumptions of Collins et al. (2016). While Collins et al. assumed that *Eudaniela* crabs consume comparable amounts of CBOM and FBOM, our model selection exercise shows clear evidence against the consumption of FBOM. On the other hand, while in Collins et al. we assume that *Argia* damselflies only consume *Tricorythodes* mayflies, we found evidence in favor of them also preying on *Petrophila* larvae. This illustrates the power and importance of being able to perform model

selection on isotope tracer experiments. Against a priori expectations, some of the untested links appear very weak (e.g., consumption of *Petrophila* by *Argia*). The purpose of our model comparison was illustrative, and a thorough examination of all trophic links is beyond the scope of our article, but we hope it is clear how this would be a straightforward exercise. We must caution, however, that the number of models increases exponentially with every link tested, and one must be wary of the risks of data dredging and overanalysis that come with testing too many models if there are no a priori reasons to test them all.

For all their advantages, from error propagation to the use of prior information, Bayesian models do have a main inconvenience: computing time. It took on average 4 h of computation to fit a single model to one stream, using parallel computing of the four MCMC chains on an Intel Core i5 processor (4590, 3.3 GHz) and 8 GB of RAM. Given that one of the strongest motivations to use this method is the need to statistically analyze the increasing number of large comparative studies (Mulholland et al. 2008; Norman et al. 2017; Tank et al. 2018), this is an important concern. However, faster computers and large clusters are likely to reduce these times quickly. It is also important to be aware of the method's limitations and simplifications. First, our model is based on a linear Markov process, which means that all transfer rates are a constant proportion of resource abundance. Strictly speaking, this is not a realistic assumption, since algal uptake often follow a nonlinear function of nutrient availability, such as Michaelis-Menten dynamics (O'Brien 1974), and consumers show saturating functional responses to prey abundance (Jeschke et al. 2002). However, this simplification, common in previous methods, is easily justified given the relatively short timeframe of isotope tracer addition experiments. This makes it unlikely that resource abundance will vary to the point that nonlinearities cannot be approximated locally by linear functions. In fact, our methods assumes that the system is approximately at steady state, meaning that there are no major changes in the biomass of compartments during the period of the study. It is possible that this assumption will not hold for some longer experiments in highly productive environments, and future developments of the model may alleviate this assumption using time series of biomass data throughout the experiment.

We can think of other aspects that can be incorporated into this framework in the future other than nonlinear uptake and growth dynamics. For example, this model could incorporate the longitudinal dimension explicitly, as was done in Newbold et al. (1983). In that effort, the water column was treated as a dynamic compartment and included particle exchange between the bed and the water column (the latter being critical to fitting the dynamics of the net-spinning caddisfly). The present article, by contrast, is not

spatially explicit, replaces the water column dynamics with external forcing, and neglects particle suspension, transport, and deposition. An explicit treatment of flow and longitudinal linkage would allow one to combine the temporal and spatial information of tracer distribution along the stream in order to increase the accuracy of our estimates of uptake and turnover. This can be particularly powerful for understanding the dynamics of nutrient pools and basal compartments (e.g., nitrification), whose faster dynamics makes tracer differences most apparent along the spatial axis (Mulholland et al. 2000; Peterson et al. 2001). A second potential development is the incorporation of nutrient cycling in the form of excretion or decomposition. This would essentially involve a new set of parameters  $\rho_i$  denoting the recycling rate of compartment  $i$  (i.e., the proportion of that compartment that returns to the  $\text{NH}_4^+$  pool). These parameters would populate the first row of the transfer matrix  $\Psi$ . For compartment-specific recycling rates to be identifiable, however, they would likely require the incorporation of priors (e.g., using supplementary excretion trials) and the incorporation of the spatial scale proposed above.

Another possible development would be the integration of generalized linear mixed models (Bolker et al. 2009) or other models that allow for covariates to affect uptake and turnover rates. This would be particularly powerful in comparative analyses across different experiments and sites, as it would improve our ability to explicitly test effects of a particular variable of interest (e.g., light, temperature, or time) across streams or treatments.

In conclusion, we have presented a method that improves the statistical rigor of tracer addition analyses. Our hope is that it will not only be of great use as it stands but also provide a baseline template for further developments and improvements that extract the most information from such elegant experiments. Most importantly, our modeling approach allows statistical comparisons among systems and treatments as well as formal testing of alternative hypotheses, expanding the utility of isotope tracer experiments in comparative and experimental settings.

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