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1 **Simultaneous optimization of harvest schedule and data quality**

2

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8

1 **Abstract**

2

3 In many recent studies, the value of forest inventory information (VOI) in the harvest scheduling
4 has been examined. In a previous paper, we demonstrated that selecting only a small part of stands
5 for additional measurements simultaneously with making the harvest decisions may be highly
6 profitable. In that study, the quality of additional measurements was not a decision variable, and the
7 only options were between making no measurements and measuring perfect information. In this
8 study, we introduce the data quality into the decision problem, i.e., the decision maker can select
9 between making imperfect or perfect measurements. The imperfect information is obtained with a
10 specific scenario tree formulation. Our decision problem includes three types of decisions: harvest
11 decisions, measurement decisions, and decisions about measurement quality. In addition, we decide
12 about the timing of the harvests and measurements. These decisions are evaluated based on two
13 objectives, discounted aggregate incomes for the planning periods and the end value of the forest at
14 the end of the planning horizon. Solving the biobjective optimization problem formed shows that
15 imperfect information is mostly sufficient for the harvest timing decisions during the planning
16 horizon but perfect information was required in order to meet the end inventory requirement. The
17 relative importance of the two objectives affects the measurements indirectly, through increasing or
18 decreasing the number of decisions that are identical in all scenarios, i.e., certain decisions.

19

20 **Keywords:** information economics, data quality, decision making, forest inventory, stochastic
21 optimization, constraints, biobjective optimization

1 **1. Introduction**

2

3 Any non-trivial decision typically includes uncertainty concerning the prevailing state of nature
4 (Hirshleifer and Riley 1979). The decision maker can then either make an optimal choice between
5 different alternatives with the current information or reduce the uncertainty by collecting more
6 information. Value of information (VOI) in decision making (ex ante) can hereby be defined as the
7 difference between the expected value of this choice with and without the information (e.g.
8 Hirshleifer and Riley 1979, Lawrence 1999, Birchler and Bütler 2007 and Kangas 2010).

9

10 In harvest scheduling, the VOI in forest inventory can be calculated to support the decision for
11 measuring the area in question as a whole. The measurements are profitable, if VOI is higher than
12 the measurement costs. It is also possible to formulate the forest planning problem in such a way
13 that the data acquisition decisions are optimized at the same time as the harvest decisions. In this
14 case, it is possible to select a sub-set of stands or some sub-areas as stands to be measured. For
15 instance, Duvemo et al. (2014) formulated a problem where the stands that were eligible to be
16 harvested during the first years of planning horizon in a tactical plan were selected for a pre-harvest
17 inventory, for which more accurate data was acquired before the final operational decisions. The
18 selection of the stands for a pre-harvest inventory was not optimized, though. Kangas et al. (2014)
19 included the measurement decisions into the harvest scheduling optimization problem, and then it
20 was possible not only to select some stands to be measured, but also to define when such data
21 would be needed.

22

23 If it was assumed that the uncertainty can be resolved, i.e., perfect information of the forests will
24 become available at some time point, two-stage optimization (also programming with recourse)
25 could be utilized. In the first stage, decisions are made under uncertainty, but the second stage
26 decisions are assumed to be made under certainty. In a multi-stage problem, new information

1 becomes available after each stage and the uncertainty involved diminishes in time. If the decision
2 of forest inventory in a given stand is optimized at the same time as the harvests, the harvest
3 decision gives the optimal timing of the harvest and the inventory decision indicates whether a
4 stand is measured or not. This decision depends on the costs of the inventory per hectare. This
5 means that if the stand is measured, optimization with perfect information is carried out for that
6 stand, and if it is not measured, optimization is carried out under uncertainty. In this case, moving to
7 a second stage is an active decision, rather than happening in time as in common “wait-and-see”
8 problem formulations (see e.g. Birge and Louveaux 2011).

9

10 A generalization of the described problem is that besides the harvest and inventory decisions we
11 also decide about the quality of the inventory. Then, for each of the stands we can choose whether it
12 requires additional information, and also whether imperfect information is sufficient, or whether
13 perfect information is needed. That may depend on the decisions to be made, the relative
14 importance of the different objectives, the quality ratio of imperfect information and perfect
15 information, and the costs of the different measurements.

16

17 In a previous paper (Kangas et al. 2014), we demonstrated that selecting only a small part of stands
18 for additional measurements simultaneously with making the harvest decisions may be highly
19 profitable. In that study, the quality of additional measurements was not a decision variable but,
20 instead, the only options were either to make no measurements and to measure perfect information.
21 In this study, we extend the consideration and introduce the data quality in the decision problem,
22 i.e., the decision maker can select between making imperfect or perfect measurements. We study
23 this by formulating an optimization problem where we optimize simultaneously both the decision of
24 whether to harvest the stand or not, whether to measure the stand or not, and the optimal quality of
25 the information acquired. In addition, we study the optimal timings of the harvests and

1 measurements. We formulate this as a multiobjective optimization problem (see e.g. Miettinen
 2 1999) and solve it using the ε -constraint method (Haimes et al. 1971, Miettinen 1999), using as the
 3 objectives both the end value of the forests and the aggregated discounted incomes from the
 4 planning periods within the planning horizon. We study the effects of measurement costs, interest
 5 rate and values of end-inventory, which is measured as a relative maximum decline allowed in end-
 6 inventory value during the planning horizon.

7

8 **2. Material**

9

10 The study site consists of 29 stands, i.e., $J = 29$ and 67.29 hectares located in the municipality of
 11 Juuka in Eastern Finland (Table 1). This estate is a part of a larger estate owned by UPM-
 12 Kymmene. The stands were measured using a compartment-wise inventory (for details, see
 13 Mustonen et al. 2008).

14

15 The initial data was assumed to include inventory errors. The prior distributions of the basal area
 16 and dominant height in the beginning of the planning horizon were formulated using Monte Carlo
 17 simulation. Correlated multinormal errors were introduced to the initial variables using the
 18 `rmvnorm` package of R (R Development Core Team 2011). The relative standard error of dominant
 19 height and stand age was assumed to be 10%, and that of basal area 27.5%. Correlation was
 20 assumed to be 0.1. The means of errors were assumed to be zero. This level corresponds to the level
 21 of five-year old data obtained with a traditional stand-level forest inventory (Haara & Leskinen
 22 2009).

23

24 The errors were simulated so that the prior variance of each variable (dominant height (H_{dom}), stand
 25 age (T) and basal area (G)) was divided into two components: $\sigma_{\text{prior}}^2 = \sigma_{\text{imperfect}}^2 + \sigma_{\text{residual}}^2$. First, 10

1 scenarios of an error component $\varepsilon_{imperfect}$ were generated using random number generation. Then, for
 2 each of these scenarios 10 additional error components $\varepsilon_{residual}$ were generated, giving a total of $I =$
 3 100 scenarios of stand characteristics (see Figure 1 for a case with 3 replications). Then, in the
 4 optimization calculations the mean basal area (or mean height or age) from each set of 10 scenarios
 5 served as one estimate of the imperfectly measured basal area $\hat{G}_{imperfect}$, i.e. altogether these sets
 6 formed 10 different values of imperfectly measured basal area. In this study, the imperfect
 7 information was assumed to resolve 70% of the prior variation, which means that the variance of
 8 the imperfect information was 70% and the residual uncertainty 30% of the prior variance for each
 9 of the variables. That would reflect that the imperfect information for basal area for instance, is in
 10 the level of modern ALS forest inventory (Packalén & Maltamo 2007).

11

12 When the initial data was generated, a simple stand-level simulator was used to predict the
 13 development of the stands for $K = 9$ five-year periods, for each of the I scenarios. The simulator
 14 consisted of a model for the relative growth of basal area as a function of stand age, mean height,
 15 site index (dominant height at the age of 100 years, H_{100}) and basal area, and of a growth model for
 16 the relative growth of dominant height (H_{dom}) as a function of stand age and dominant height for
 17 spruce and pine (Vuokila and Väliaho 1980). The latter model was also used to predict the site
 18 index.

19

20 Stand volume (V) was calculated with a model $V = G \cdot H_{gm} \cdot f$, where f is the form factor. The form
 21 factor was predicted using models by Gustavsen and Fagerström (1983) as a function of mean
 22 height and site type. The relation between mean height and dominant height was assumed to be
 23 constant in the data, and a model of the form

24

$$25 \quad \hat{H}_{gm} = 0.5784 + 0.7807 H_{dom}$$

1

2 for the mean height was estimated from the dataset in the beginning of the simulation.

3

4 The alternative decisions available for the decision maker were the different timing options for
5 clearcut. No thinnings were included in the planning. The net revenues from the clearcut were
6 obtained by multiplying the total volume with the price 35 €/m³. Thus, every produced cubic meter
7 was assumed to be equally valuable. Possible clearcut was assumed to be carried out at the end of
8 the period.

9

10 **3. Methods**

11

12 The problem here is a typical planning problem for a private forest owner, with the goal to get
13 incomes from the estate and also to save some cutting possibilities also for the future. We start with
14 a general multiobjective optimization problem that models the simultaneous optimization of harvest
15 schedule and data quality. The intention is to study how different trade-offs in the values of the
16 objectives affect the measurement and harvest decisions.

17

18 Let $x_{ijk} \in \{0,1\}$ be the harvest decision of stand $j \in J$, for scenario $i \in I$ and in period $k \in K$. Here,
19 sets J, I and K stand for the stands, scenarios and periods, respectively. Furthermore, let $(I_l)_{l \in L}$
20 (where L is an index set) be an exclusive partition of scenarios in I (i.e., $I_{l_1} \cap I_{l_2} = \emptyset$ for all $l_1 \neq l_2$
21 and $\cup_{l \in L} I_l = I$). The index sets I_l mathematically model the imperfect information, which was
22 explained previously. That is, the variance is smaller inside the index sets I_l than it is between
23 them. Finally, let $w_{jk} \in \{0,1\}$ be the decision of making a perfect inventory of stand j on period k
24 and $v_{jk} \in \{0,1\}$ be the decision of making an imperfect inventory of stand j on period k . In addition,

1 we fix an index $i_l \in I_l$ for each $l \in L$. Finally the model has the following parameters: parameter δ is
 2 the interest rate, real values c_{jik} are the incomes (€/ha), q and r are the costs of full and partial
 3 inventories (€/ha) and a_j are the areas of stands.

4

5 Then, we formulate the multiobjective optimization problem as

$$6 \quad \max \left(\left(\sum_{k \in K} \sum_{j \in J} (x_{jik} c_{jik} - w_{jk} q - v_{jk} r) a_j \left(\frac{1}{1 + \delta} \right)^{5k} \right)_{i \in I}, \left(\sum_{j \in J} c_{ji\#K} (1 - \sum_{k \in K} x_{jik}) \right)_{i \in I} \right)$$

7 (1)

8 subject to

$$9 \quad \sum_{k \in K} x_{jik} \leq 1, \text{ for all } j \in J, i \in I \quad (2)$$

$$10 \quad x_{jik'} - x_{ji,k'} - \sum_{k=1}^{k'} v_{jk} - w_{jk} \leq 0, \text{ for all } j \in J, i \in I, k' \in K \quad (3)$$

$$11 \quad x_{jik'} - x_{jik'} - \sum_{k=1}^{k'} v_{jk} - w_{jk} \leq 0, \text{ for all } j \in J, i \in I, k' \in K \quad (4)$$

$$12 \quad x_{jik'} - x_{ji,k'} - \sum_{k=1}^{k'} w_{jk} \leq 0, \text{ for all } j \in J, i \in I, l \in L \quad (5)$$

$$13 \quad x_{jik'} - x_{jik'} - \sum_{k=1}^{k'} w_{jk} \leq 0, \text{ for all } j \in J, i \in I, l \in L \quad (6)$$

$$14 \quad x_{jik}, w_{jk}, v_{jk} \in \{0, 1\}, \text{ for all } j \in J, i \in I, k \in K,$$

15 where #K refers to the number of periods. In the above problem, the objectives are to maximize the
 16 discounted incomes in all scenarios and, at the same time, to maximize the value of the forest left
 17 unharvested. The problem has $2\#I$ objectives. The first constraint (2) determines that each stand
 18 can be clearcut at most once during the planning horizon. Constraints (3) and (4) make sure that if
 19 nothing is measured, then all the harvest decisions in all the scenarios must be the same. It means
 20 that if no measurements at all are carried out, all the decisions for the given stand are first-stage

1 decisions. These constraints can be interpreted as non-anticipativity constraints. Constraints (5) and
2 (6) make sure that if full inventory is not taken, then the harvest decisions must be the same within
3 the partitions I_l . When imperfect measurements are made, we can interpret the decisions as second-
4 stage decisions, where we know to which group of scenarios the realized scenario belongs. The
5 perfect information gives the possibility for third-stage decisions that can be optimal for each
6 scenario separately.

7

8 Unlike in typical multi-stage problems, here the uncertainty is not resolved in time, when moving
9 from one planning period to next, unless measurements are carried out. It also means that unlike in
10 typical multi-stage problems, the stands can be at different stages: it is possible that for some stands
11 stepping from first stage to second or third stage never happens, and it is likewise possible that in
12 some stands there is a need to step to the third stage right in the beginning of the planning horizon.
13 The movement from one stage to another is thus a result of a decision. In this context, the possible
14 consequences of uncertainty are that the harvest timing decisions are sub-optimal, i.e. produce less
15 incomes than would have been optimal. In addition, the uncertainty may cause the solution to be
16 infeasible (end-inventory value too small) or inefficient (part of the harvest possibilities are left
17 unused).

18

19 The optimization problem (1) - (6) means that both the incomes and the value of the forest left
20 unharvested must be maximized, whatever happens, i.e., whatever scenario realizes. The scenarios,
21 however, are not real but, instead, merely technical means to model the uncertainty. When one takes
22 into consideration the fact that there is a large number of scenarios and, thus, the problem
23 formulated has a very large number of objectives, it is desirable to find a formulation of the
24 problem with a lower number of objectives and formulation that handles the uncertainty in the
25 scenarios. For this, we formulate a biobjective optimization problem

$$1 \quad \max \left(\sum_{j=1}^{\#J} \sum_{k=1}^{\#K} \left[\left(\frac{1}{\#I} \sum_{i=1}^{\#I} x_{jik} c_{jik} - w_{jk} q - v_{jk} r \right) a_j \left(\frac{1}{1+\delta} \right)^{5k} \right], \min_{i \in I} \left(\frac{\sum_{j=1}^{\#J} c_{ji\#K} (1 - \sum_{k=1}^{\#K} x_{jik})}{\sum_{j=1}^{\#J} c_{ji1}} \right) \right) \quad (7)$$

2 subject to

3 constraints (2) – (6)

4 $x_{jik}, w_{jk}, v_{jk} \in \{0,1\}$, for all $j \in J, i \in I, k \in K$.

5 The objectives of the above problem are to maximize the mean income over all scenarios and to
 6 maximize the minimum value (over all scenarios) of the forest left unharvested relative to the value
 7 at the beginning of the planning horizon. That is, if the value of the second objective is, for
 8 example, greater than 0.7, then the reduction in the forest value is less than 30% in all scenarios.

9

10 The objectives of the optimization problem (7) and (2)-(6) cannot be combined directly into a single
 11 objective, because it is not completely clear how they should be combined. By studying the above
 12 biobjective optimization problem with different preferences between the objectives, we can get
 13 better picture about what should be the most preferred way of cutting and measuring the stands.

14

15 Finally, we solve the biobjective optimization problem using the augmented ε -constraint method
 16 (Movrotas 2009). That is, we solve optimization problems of the type

$$17 \quad \max \sum_{j=1}^{\#J} \sum_{k=1}^{\#K} \left[\left(\frac{1}{\#I} \sum_{i=1}^{\#I} x_{jik} c_{jik} - w_{jk} q - v_{jk} r \right) a_j \left(\frac{1}{1+\delta} \right)^{5k} \right] + \rho \min_{i \in I} \left(\frac{\sum_{j=1}^{\#J} c_{ji\#K} (1 - \sum_{k=1}^{\#K} x_{jik})}{\sum_{j=1}^{\#J} c_{ji1}} \right) \quad (8)$$

18 subject to

19 constraints (2) – (6)

$$1 \quad \frac{\sum_{j=1}^{\#J} c_{ji\#K} (1 - \sum_{k=1}^{\#K} x_{jik})}{\sum_{j=1}^{\#J} c_{ji1}} \geq \varepsilon \text{ for all } i \in I \quad (9)$$

$$2 \quad x_{jik}, w_{jk}, v_{jk} \in \{0, 1\}, \text{ for all } j \in J, i \in I, k \in K,$$

3

4 where the parameter ε ranges from 0.7 to 1. This means that we allow a drop from 0 to 30% in the
 5 value of the forest when compared to the value at the beginning of the planning horizon. The
 6 parameter ρ is given a very small value (in the computational test we have used 0.0001). Without
 7 the additional term

$$8 \quad + \rho \min_{i \in I} \left(\frac{\sum_{j=1}^{\#J} c_{ji\#K} (1 - \sum_{k=1}^{\#K} x_{jik})}{\sum_{j=1}^{\#J} c_{ji1}} \right)$$

9 in the objective function (8), the optimal solutions could only be guaranteed to be weakly Pareto
 10 optimal to the optimization problem (8), (2)-(6), (9), but with the complete objective function (8)
 11 the optimal solutions of this problem are guaranteed to be Pareto optimal solutions to the
 12 optimization problem (see Movrotas 2009). Finally, the above problem can be formulated as a
 13 mixed-integer linear problem using the standard way of linearizing max-min type optimization
 14 problems (see e.g., Posner and Wu 1981).

15

16 When solving the problem, all the mixed-integer linear optimization problems were solved using
 17 the IBM ILOG CPLEX Optimization Studio V 12.5.1.0 (IBM ILOG CPLEX), which is commonly
 18 known merely as Cplex. Cplex was running on a computing server with 64 cores and approx.
 19 1032GB of Random-access memory (RAM). Cplex was able to take advantage of extensive
 20 parallelization and was simultaneously running in parallel on up to 32 cores.

1 **4. Results**

2
3 The biobjective optimization problem was solved with different costs of perfect and imperfect
4 measurements and with different interest rates. By using the ϵ -constraint method, we could study
5 trade-offs between the expected income over all the scenarios and the end inventory value.

6 According to the results, a fairly stable number of perfectly measured stands (being 8-10) is the
7 best, while the number of imperfectly measured stands sharply diminished as a function of interest
8 rate (Figure 2). With a 10€/ha cost, the number of stands profitably measured with imperfect data
9 dropped already when the interest rate rose to 2 per cent, while with a 5 € cost/ha the biggest drop
10 happened when the interest rate rose to 3. Yet, some stands were always measured with perfect
11 information, even though the associated cost was set to 100€/ha.

12
13 When the proportion of measured area was shown, again the perfectly measured area seemed to be
14 pretty constant, but the area of imperfectly measured stands dropped fast as a function of interest
15 rate, and clearly faster with the 10€/ha cost. With the 1% interest rate, the proportion of the area
16 measured was clearly over 40%. This result is due to the fact that the number of uncertain harvest
17 decisions was greatest with the interest rate 1%, as the value growth percent in many of the stands
18 was below 1% in part of the scenarios and above it in others. However, even with a 2% interest
19 rate, the benefits of imperfect measurements were too low to measure much over 10% with 10€/ha
20 costs, while with a 5€/ha cost it was profitable to measure about 20% with the interest rate 3.

21 Besides this obvious difference, the two cost options produced fairly similar results and, thus, the
22 results shown in the rest of the figures mostly concern 5€/ha costs.

23
24 When the measurement period and the quality of information is plotted as a function of stand age, it
25 can be seen that with the interest rate 1%, it was profitable to measure mainly old stands during
26 periods 3-6 with imperfect information, and mainly young stands during periods 7-9 with perfect

1 information (Figure 3). This suggests that imperfect measurements were mainly made for harvest
2 timing decisions, and perfect measurements for meeting the desired end-inventory level. When the
3 area measured with perfect information was studied more closely, it turned out that the probability
4 of a stand to be measured with perfect information rapidly decreased as a function of stand area.
5 The two smallest stands were measured with perfect information in all studied problems with
6 different parameters (Figure 4), but stands larger than 2 hectares were never measured with perfect
7 information. That also indicates that the perfect information was practically always just used to
8 meet the end-inventory requirement.

9

10 The use of imperfect and perfect data for different types of decisions could be seen from the
11 distributions of the harvest timings across scenarios and the quality of information required (Figure
12 5). The stands where no measurements were profitable were harvested either in the beginning
13 (period 1) or not at all (N). In both cases, the decision was clear (upper left, lower right). In one
14 stand (middle right) the decision to harvest was certain, and the main problem was to decide upon
15 the harvest timing. In the last three stands, both the decision of whether the stand should be
16 harvested or not was uncertain (in part of the scenarios the stand was left unharvested). In one of
17 these cases, the imperfect measurement was sufficient. In two stands, where perfect data was
18 needed, the decisions were more uncertain, for instance, the timing options varied more.

19

20 Varying the relative reduction allowed in the end-inventory from 0 to 30%, the area of measured
21 stands varied, but not in a linear fashion. With a 1% interest rate, the measured area was lowest
22 between 0.09 and 0.15 relative reduction, with 2% there seemed to be an increasing trend in the
23 imperfectly measured area up to 0.18 relative reduction, and with a 5% interest rate the area to be
24 measured was highest from 0.09 to 0.21 relative reduction (Figure 6). The variation was quite
25 modest, though. It depended on how uncertain the timing decisions and cutting decisions actually

1 were, and in the range studied the relative reduction did not affect much to the uncertainties (Figure
2 7). With high interest rates, there could be seen a slight increasing trend with certain harvest timing
3 decisions and a slight decreasing trend in certain unharvest decisions. This means that as the
4 relative reduction increased, part of the certain unharvest decisions changed to uncertain unharvest
5 decisions, part of the uncertain unharvest decisions changed to uncertain or certain timing decisions,
6 and all this affected the measured area. Instead, increasing the interest rate sharply increased the
7 number of certain decisions, i.e., decisions which were the same for all scenarios (Figure 7). With a
8 1% interest rate, no harvest timing decisions were certain, i.e., same in all scenarios.

9

10 The same could also be seen from the stand-level decisions. In the same stands presented before,
11 but with a higher relative reduction allowed, the main change was that in two stands the
12 measurement options was changed, but to opposite directions, one perfect measurement changed to
13 an imperfect measurement and vice versa (Figure 8). This indicated that the optimum in the
14 problem was quite flat, i.e., minor changes in the measurements of single stands could be
15 exchangeable, if the decisions to be made and the uncertainties of these decisions were fairly
16 similar.

17

18 The flatness of the optimum and the uncertainties of the decisions could be clearly seen from the
19 optimal measurement costs and gaps in the optimal solutions (gap = difference between the best
20 integer solution found and upper bound for the optimal solution) were in the same level of
21 magnitude. The gap was highest for the 1% interest rate, where the decisions were most uncertain,
22 and the optimal measurement cost levels as well (Figure 9). It means that the measurement
23 decisions in single stands were uncertain, and many quite good solutions could be found.

24

1 We also calculated the net value of information with 10€/ha cost for different interest rates and
2 relative reductions varying from 0 to 15%. It means that we subtracted from the objective function
3 values where the measurements we allowed (minus the measurement costs) the objective function
4 value assuming that no measurements were possible. At minimum, the net VOI was 4477€ (about
5 65€/ha, 1% interest rate), and at its maximum it was 8144€ (about 121 €/ha, interest rate 3%). The
6 net VOI for a large part is due to being able to harvest in all scenarios all the allowed volume, while
7 if measurements are not allowed the decisions need to be made in all stands according the worst
8 case scenario. The difference between 1% and higher interest rates is clear (Figure 10 left). With
9 1% interest rate there are a little more certain unharvest decisions, and therefore the problem is not
10 as bad as with the higher interest rates. The net VOI with the higher interest rates is also gradually
11 decreasing as a function of relative reduction (Figure 10 right). This means that with more
12 demanding constraints, the net VOI is higher.

13

14 The Pareto optimal solutions with the five different interest rates are shown in Figure 11. In the
15 studies case, the set of Pareto optimal solutions demonstrates an almost linear behavior, as the
16 objectives are very closely related.

17

18 **5. Discussion**

19

20 The traditional forest harvest scheduling problem with an end-inventory constraint can be
21 interpreted to involve two types of decisions: the decisions of timing of harvests during the planning
22 horizon, and decisions of selecting the stands that are left unharvested for the next planning horizon.
23 It can also be interpreted as a multiobjective planning problem with two objectives: the incomes
24 obtained during the planning horizon and the value of the growing stock at the end of the planning
25 horizon.

26

1 In the studied case, we added the decisions of measuring time and measurement quality to the
2 traditional forest harvesting scheduling problem. By using optimization methods to find optimal
3 solutions to the problem, we found out that imperfect information was mainly used for deciding the
4 timing of the harvest, while perfect information was mainly used for selecting the stands that are
5 left unharvested. There are two reasons for this. First, the perfect data in this study was assumed
6 quite expensive, and the benefits obtainable from better harvest timing decisions using perfect data
7 were in most cases lower than this cost. However, since the measurement costs as well as the
8 incomes are discounted, the perfect information becomes cheaper and more profitable towards the
9 end of the planning horizon, when the unharvest decisions are made. Obviously, had the perfect
10 data been cheap enough, all the measurements would have been made with perfect information.

11

12 The second reason is that we required in each case a specific end-inventory value. The loss of
13 incomes if a stand that can be harvested is left unharvested is quite high when compared to the
14 measurement cost even with perfect information. On the other hand, the specific end-inventory
15 demand means that if no information is available, the stand needs to be left unharvested if there is a
16 risk that even in one scenario the resulting solution will not meet the end-inventory demand. Thus,
17 the only way to ensure that all the harvesting possibilities can be used is to measure perfect
18 information. This was the case even if the imperfect information was fairly good in the studied case,
19 i.e., it explained 70% of the prior variation with only a fraction of the cost of the perfect
20 information. However, the need for perfect information can be covered in small stands. In fact, the
21 two smallest stands were always measured with perfect information.

22

23 The situation with a long planning horizon and a specific end-inventory demand is not entirely
24 realistic. In real life, after the first period decisions have been implemented, a new plan would be
25 made, meaning that a rolling horizon is used. Then, a state where the expensive perfect information

1 would be needed is never actually reached. It is probable that if the problem was reformulated using
2 an infinite planning horizon, where the aggregated incomes from an infinite series of planning
3 periods, the profitability of the imperfect information would further improve compared to perfect
4 information. It also means that strict demands are not the best way to model the decisions in
5 stochastic settings.

6

7 Another option to formulate the problem would have been to formulate the end-inventory demand
8 using soft constraints, i.e., penalizing the violation of the constraint but not requiring that the
9 constraint needs to be met in all cases. Then, the profitability of the imperfect information
10 compared to perfect information should depend on the penalty set to the violations: the more costly
11 the violation would be, the higher the profitability of perfect information would be. However, in
12 this approach the difficulty lies in setting the penalty. We would need to define how much the
13 decision maker is willing to pay in the objective function value to meet the constraints. It means
14 that we would need to model what the consequences of violating the constraints are to the decision
15 maker as a simple recourse problem (King and Wallace 2012). Furthermore, using other methods
16 than the ϵ -constraint method (e.g., involving the achievement scalarizing function (Wierzbicki
17 1982)) for solving the stochastic multiobjective optimization problem (1)-(6) might have led to
18 other results, since here the method used led to dealing with the end-inventory demand as a hard
19 end-inventory constraint. Thus, the effects of the multi-objective problem formulation on the
20 decisions and VOI should be studied more carefully in the future.

21

22 In this study, we assumed two different levels of measurement quality, perfect and imperfect data,
23 where imperfect resolves 70% of the prior uncertainty, and perfect data 100%. The procedure can
24 easily be generalized to more than two data quality options by introducing more variance
25 components, but the number of scenarios needed for the analysis would then necessarily be higher,

1 and the problem more complicated to solve. Then, the formulation of the scenario tree and also the
2 method used to solve the problem need to more carefully analysed. We also assumed that the same
3 proportion of prior variance was resolved for each of the three variables (height, age and basal
4 area), but it would be possible to consider options for improving just one variable at time.

5

6 If the whole area had been measured with perfect information in the beginning, the total cost would
7 have been 6729 €. Measuring the whole area with imperfect information would have cost either
8 672.9€ (10€/ha), or 336.45 (5€/ha). The optimal measurement cost levels varied from 170€
9 (measuring in total 4.22 ha, interest rate 5%) to 378€ (measuring in total 34.14 ha, interest rate 1%)
10 with a 5€/ha cost and from 136€ (measuring in total 3.78 ha, interest rate 5%) to 495€ (measuring in
11 total 23.22 ha, interest rate 1%) with a 10€/ha cost. The net profit from these investments to
12 measuring varied from 4477€ to 8144€ with 10€/ha cost, i.e. at least about 10 times the
13 measurement investment and with interest rate higher than 1% even higher than measuring the
14 whole area with perfect information would have been. The total optimal measurement costs were
15 surprisingly low compared to the measurement of all stands in the beginning, but it was clear that
16 the measurements were postponed to the last possible point (Kangas et al. 2014), and then perfect
17 information was in many stands measured rather than imperfect information. The difference
18 between the two cost levels of imperfect information was also fairly low, but with the higher cost
19 level in some stands the harvest timing decisions were rather made without information. The
20 optimal amount of money to invest in measurements obviously would be dependent on the prior
21 variance, and the number of uncertain decisions.

22

23 We assumed that in a multiobjective optimization situation, different objectives may require
24 different kinds of information, and that different preferences over various trade-offs would affect
25 the profitability of different measurements. In this study, the trade-off was measured with the

1 relative reduction allowed in the end-inventory. Its effect was relatively small, but it can be seen
2 that emphasizing incomes more meant that unharvest decisions could be turned into harvest timing
3 decisions or certain unharvest decisions to uncertain unharvest decisions, and both of these
4 phenomena would affect the measured area and the net VOI. It is probable, however, that if the end-
5 inventory demands were high enough, it would be certain that no stands should be harvested, or if it
6 was low enough, it would be clear that most stands would be harvested. Thus, having different
7 emphasis on trade-offs would have a more profound effect if the ranges analyzed were larger. This
8 remains to be studied in the future. In addition, since the value of unharvested forest depends on
9 similar uncertainties as the other objective, the incomes from the harvested forest, emphasizing
10 them in trade-offs did not affect much the quality of information needed. This might be different, if
11 the problem had more different objectives, e.g., recreational value of the forest that depends on
12 uncertainty in a different fashion.

13

14 On the other hand, also the interest rate can be seen to reflect the trade-offs between the objectives:
15 since the end-inventory value of forests was not discounted, increasing the interest rate decreased
16 the importance of the income objective relative to that of the end-inventory value. In this case, the
17 increasing interest rate also decreased the uncertainty concerning the harvest timing decisions and,
18 therefore, the usefulness of imperfect information decreased.

19

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2

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- 18
19

1 Table 1. The properties of the estate stands

Variable	Age (T)	Basal area (G)	Volume (V)	Mean diameter (Dgm)	Dominant height (Hdom)
Min	10.1	1.5	4.2	2.2	2.4
Mean	63.7	17.0	111.0	14.3	13.3
Max	103.3	37.5	274.1	23.4	21.3
Sd	27.36	9.98	78.12	5.41	5.42

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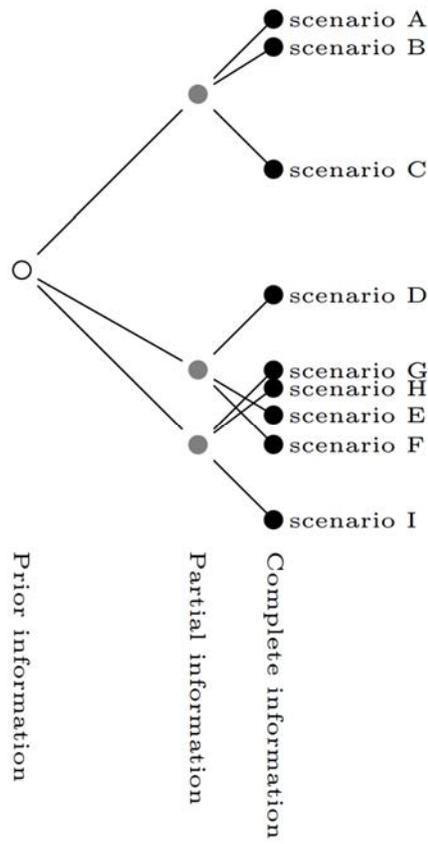


Figure 1. An example of a scenario tree, where there are three scenarios for the partial information and each scenario in partial information has three scenarios in complete information. The lengths of the lines represent the proportion of total variation.

2

3

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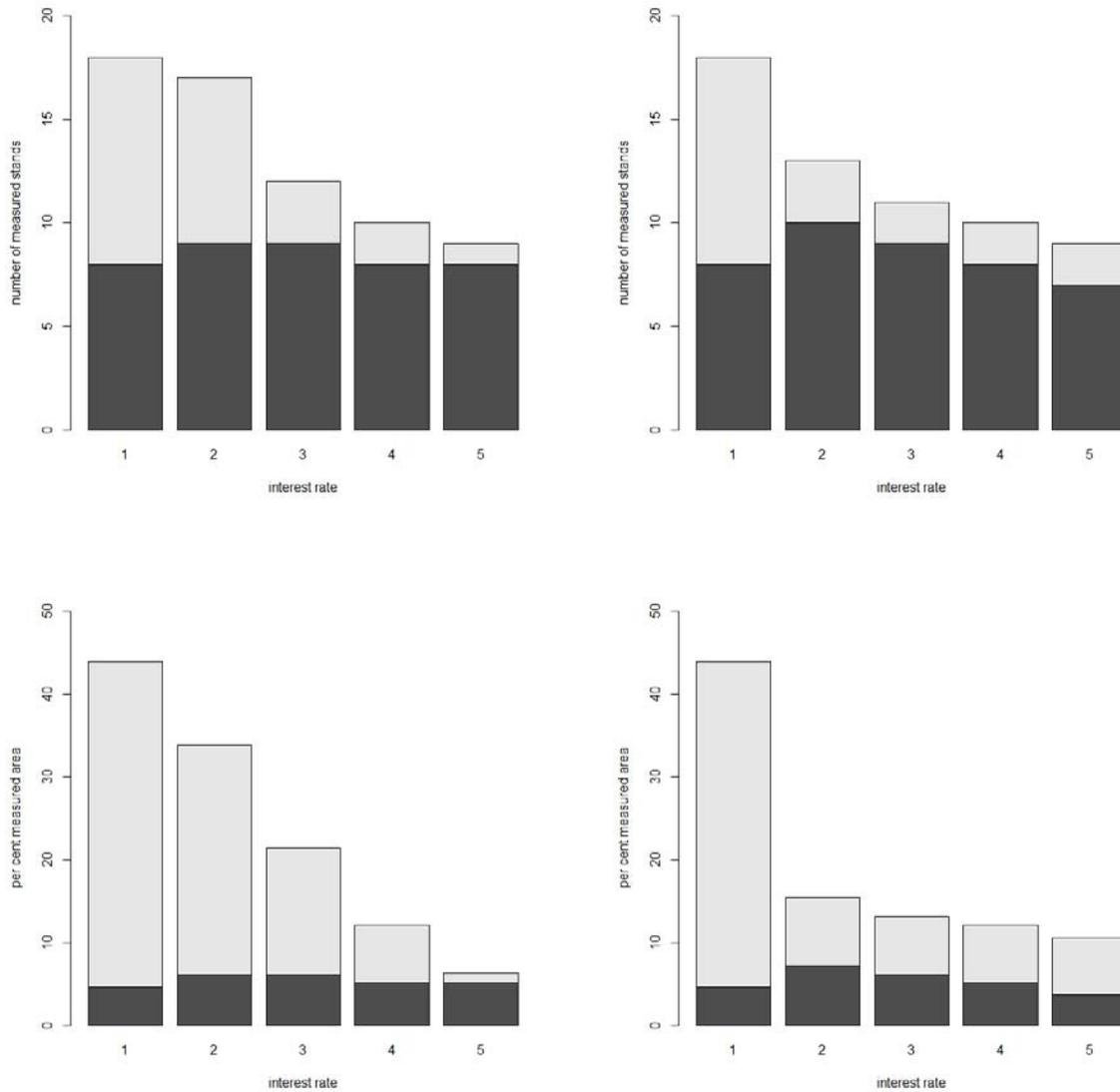


Figure 2. The upper row figures describe the number of stands measured with different interest rates, when the cost of imperfect inventory is 5€/ha (left column) or 10€ (right column), and the inventory cost of the perfect information is 100€/ha. Black color represents perfect information, and grey imperfect information. In the lower row is the proportion of the area measured with the same inventory costs and interest rates. The relative reduction allowed is 0.

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3

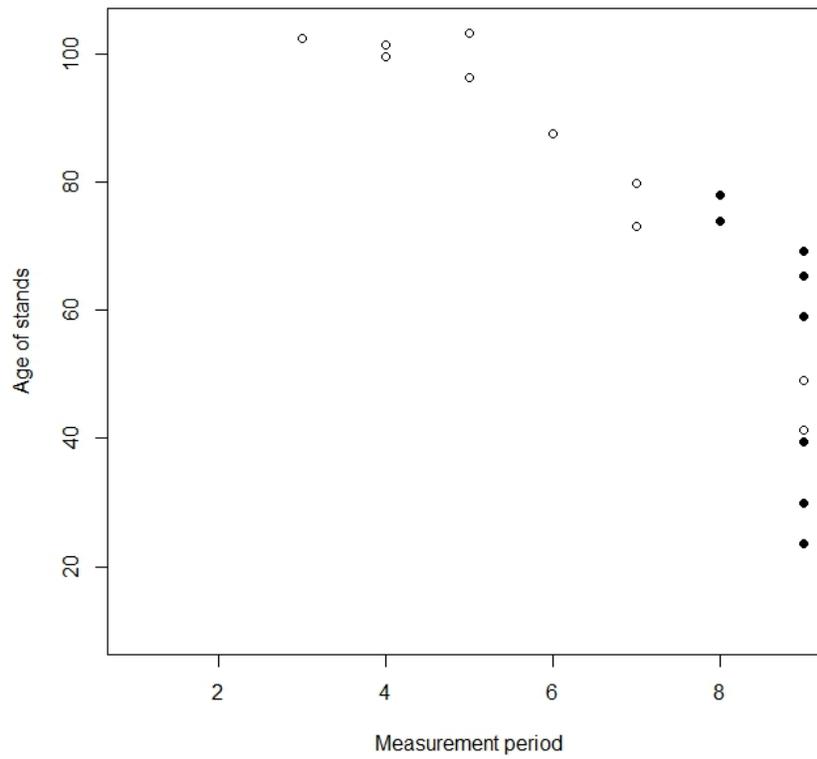


Figure 3. The measurement period as a function of stand age in the beginning of the planning horizon. Black dots represent perfect measurements, circles imperfect measurements. The interest rate is 1% and the relative reduction allowed is 0.

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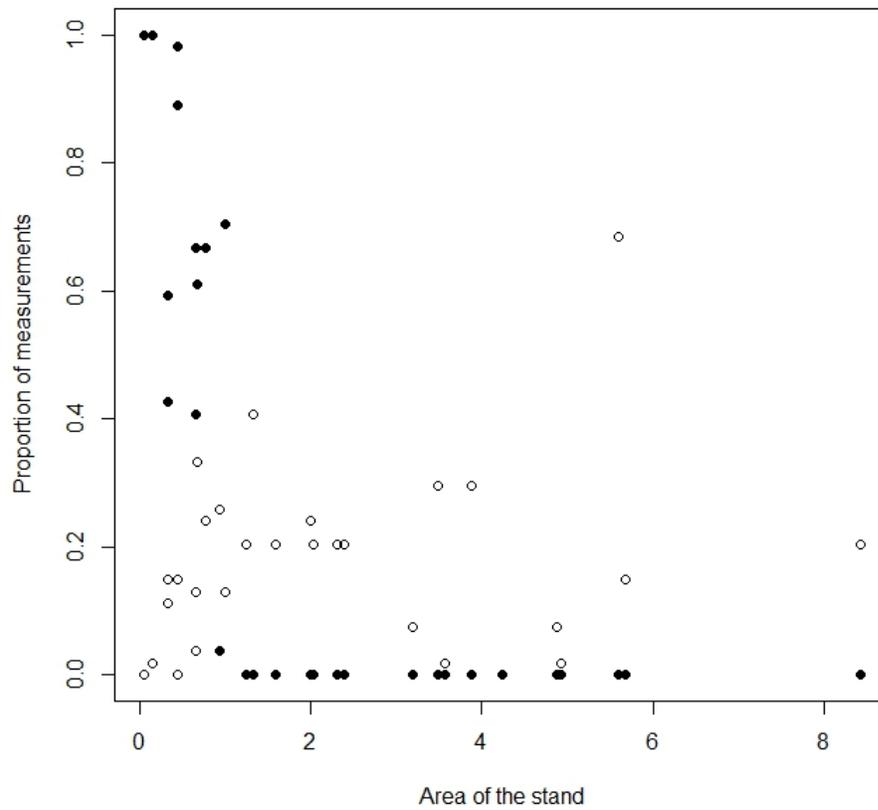


Figure 4. The proportion of cases where each stand was measured as a function of stand area.

Black dots represent perfect measurements, circles imperfect measurements.

1

2

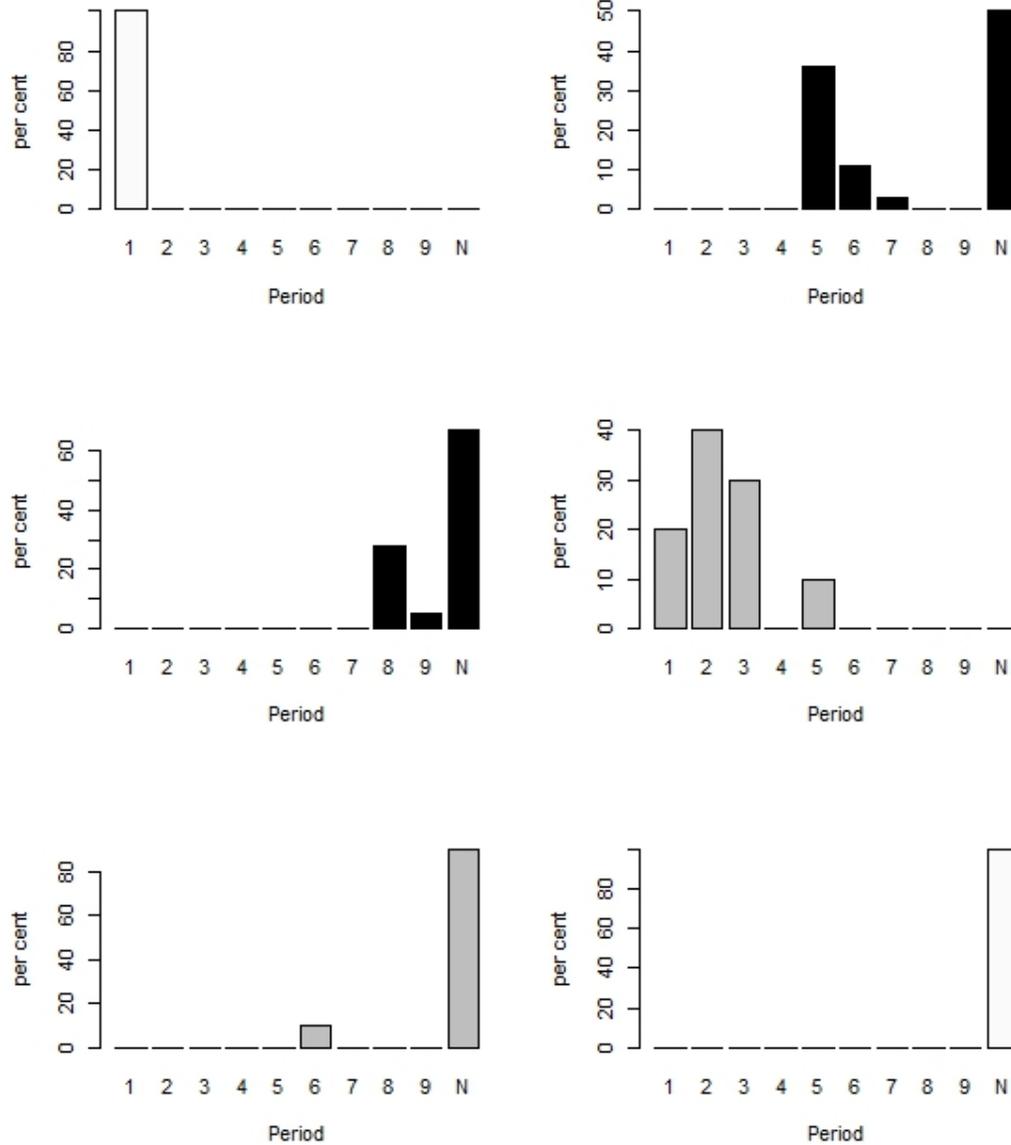
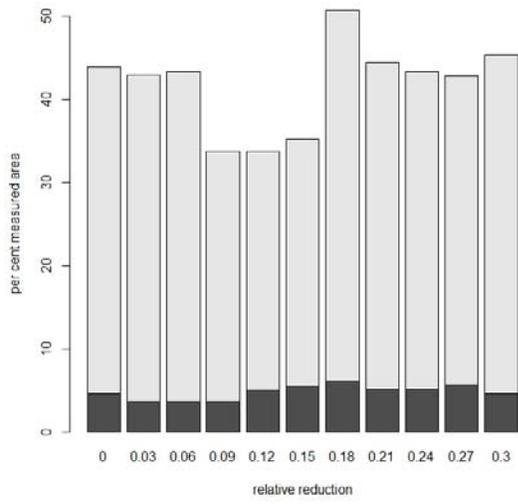


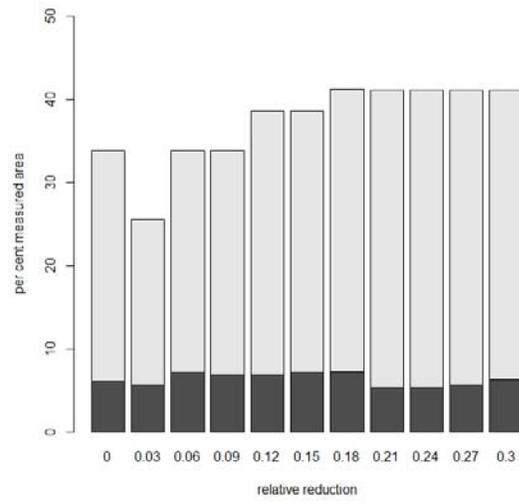
Figure 5. The harvest decisions for stands 2-7. Bars at periods 1-9 mean proportion of harvest decisions among the scenarios at that period. Period N means no harvest. Light grey denote no measurement, grey imperfect information and black perfect information. Interest rate is 2% and the maximum relative reduction allowed is 0.

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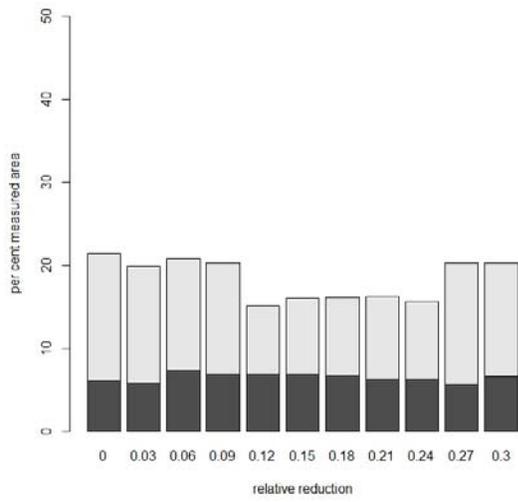
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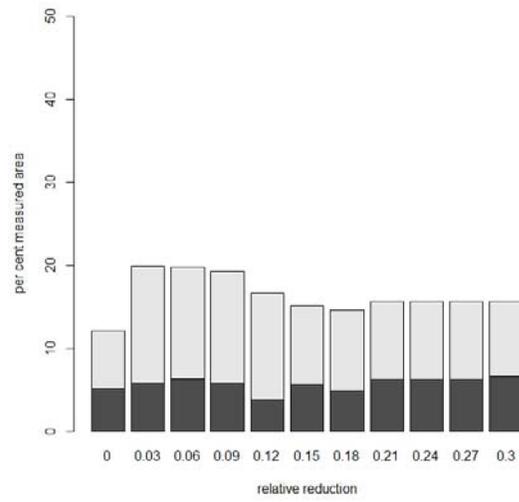
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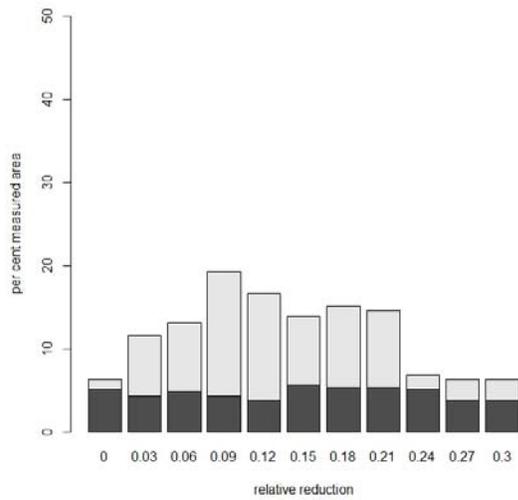
2%



3%



4%



5%

Figure 6. The proportion of measured area when the maximum allowed relative reduction varied from 0 to 30%, with different interest rates. Black color means perfect information, grey imperfect information. Measurement cost of imperfect information 5€/ha.

1

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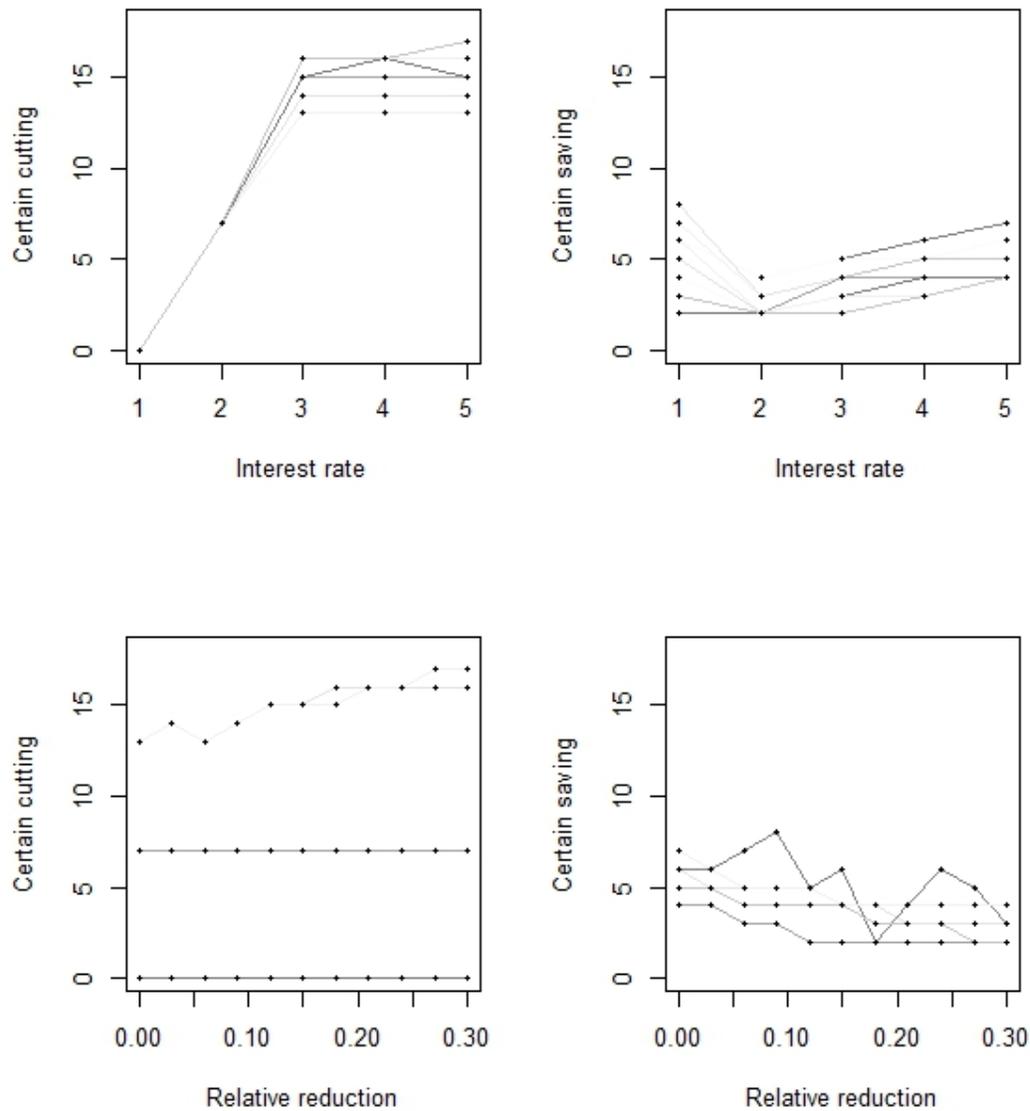


Figure 7. The upper left figure shows the number of certain harvest timing decisions as a function of interest rate. The different lines represent different values for maximal allowed relative reduction. The upper right figure shows the certain unharvest decisions. The lower left figure shows the certain harvest timing decisions as a function of relative reduction. The different lines describe different interest rates (interest rate is increasing from darkest to lightest line). The lower right figure shows the number of certain unharvest decisions.

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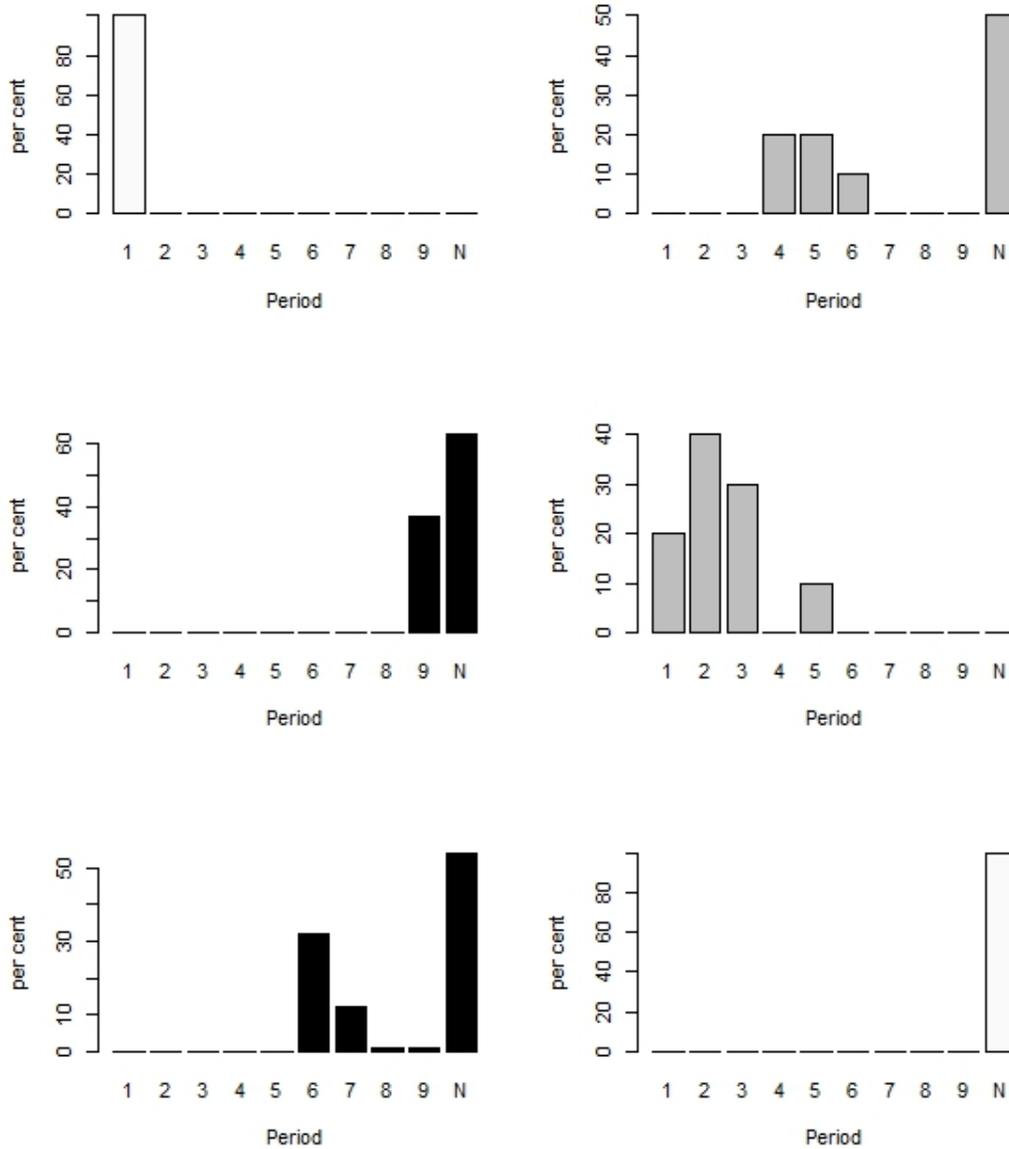


Figure 8. The harvest decisions for stands 2-7. Bars at periods 1-9 mean proportion of harvest decisions among the scenarios at that period. Period N means no harvest. Light grey denote no measurement, grey imperfect information and black perfect information. Interest rate is 2% and the maximum relative reduction allowed is 15%.

2

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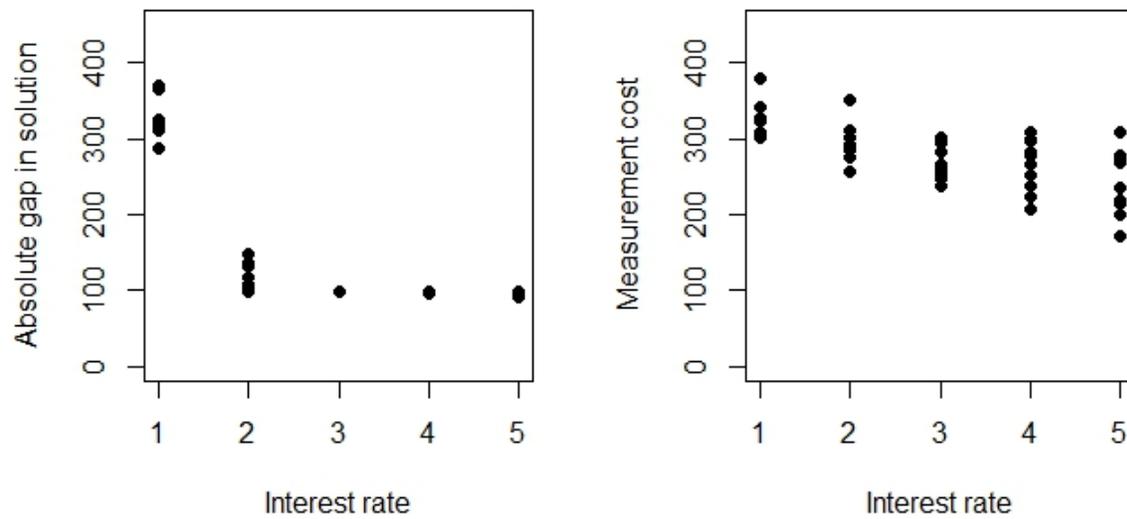


Figure 9. In the left hand figure is the absolute gap in the solution as a function of interest rate, and in the right hand figure the optimal total measurement costs. The dots describe the different end-inventory requirements.

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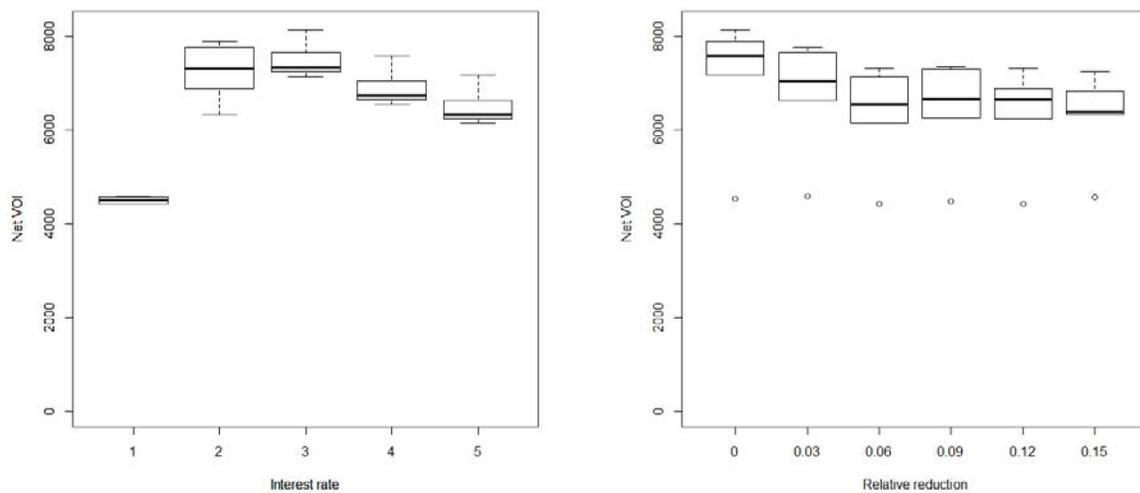


Figure 10. The net VOI as a function of interest rate (left) and as a function of relative reduction (right). The boxplots describe the variation between different values of relative reduction (left) and different interest rates (right).

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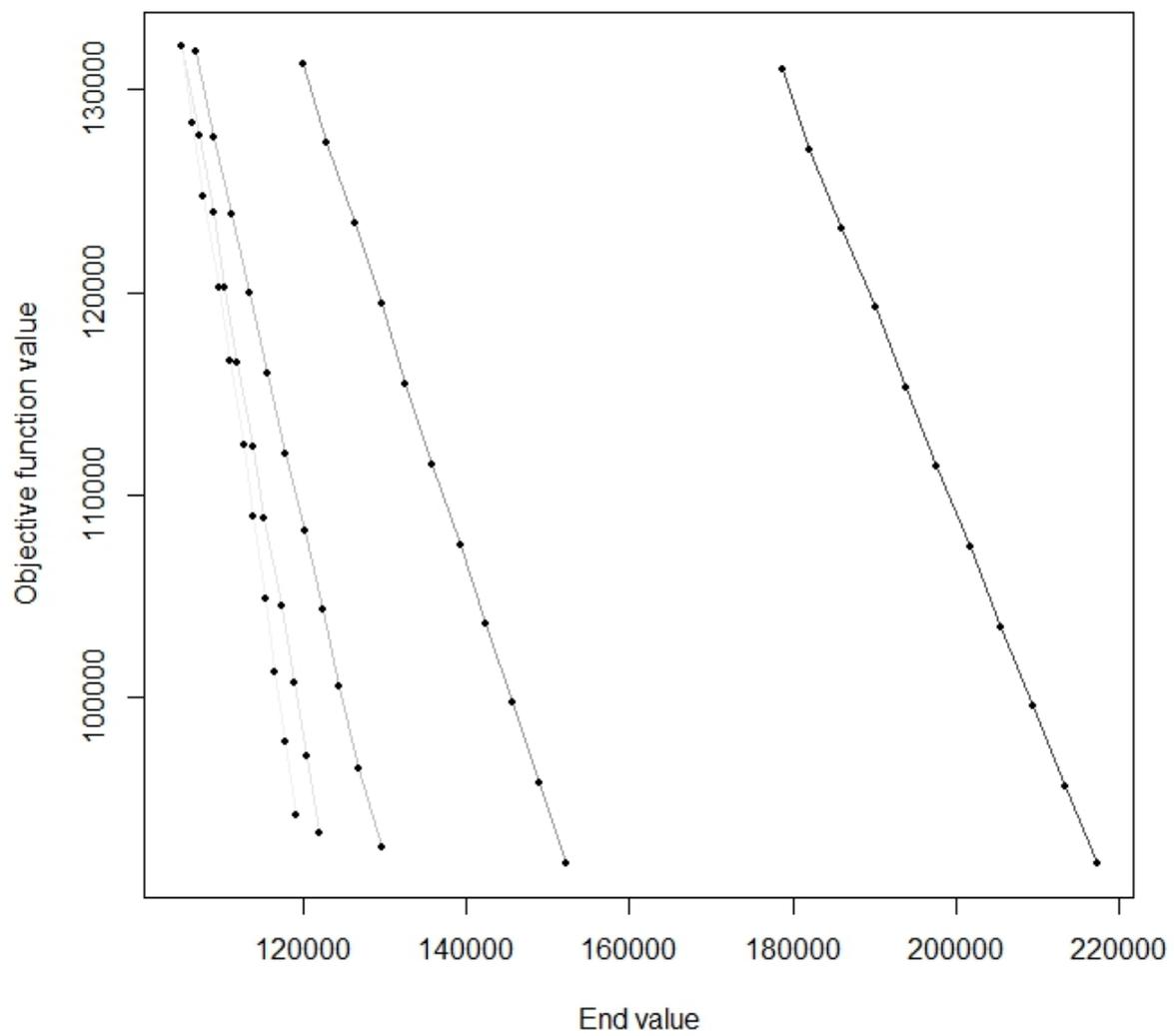


Figure 11. The Pareto front with the five different interest rates (increasing from the darkest line to the lightest line).