

This is a self-archived version of an original article. This version may differ from the original in pagination and typographic details.

Author(s): Kothalawala, Veenavee Nipunika; Suzuki, Kosuke; Nokelainen, Johannes; Hyvönen, Arttu; Makkonen, Ilja; Barbiellini, Bernardo; Hafiz, Hasnain; Tynjälä, Pekka; Laine, Petteri; Välikangas, Juho; Hu, Tao; Lassi, Ulla; Takano, Kodai; Tsuji, Naruki; Amada, Yosuke; Devi, Assa Aravindh Sasikala; Alatalo, Matti; Sakurai, Yoshiharu; Sakurai, Hiroshi; Bansil, Arun

Title: Compton scattering study of strong orbital delocalization in a LiNiO2 cathode

Year: 2024

Version: Published version

Copyright: ©2024 American Physical Society

Rights: In Copyright

Rights url: http://rightsstatements.org/page/InC/1.0/?language=en

Please cite the original version:

Kothalawala, V. N., Suzuki, K., Nokelainen, J., Hyvönen, A., Makkonen, I., Barbiellini, B., Hafiz, H., Tynjälä, P., Laine, P., Välikangas, J., Hu, T., Lassi, U., Takano, K., Tsuji, N., Amada, Y., Devi, A. A. S., Alatalo, M., Sakurai, Y., Sakurai, H., & Bansil, A. (2024). Compton scattering study of strong orbital delocalization in a LiNiO2 cathode. Physical Review B, 109(3), Article 035139. https://doi.org/10.1103/PhysRevB.109.035139

Compton scattering study of strong orbital delocalization in a LiNiO₂ cathode

Veenavee Nipunika Kothalawala⁰,^{1,*} Kosuke Suzuki,² Johannes Nokelainen,³ Arttu Hyvönen⁰,⁴ Ilja Makkonen⁰,⁴ Bernardo Barbiellini⁰,^{1,3} Hasnain Hafiz,³ Pekka Tynjälä,^{5,6} Petteri Laine,^{5,6} Juho Välikangas⁰,^{5,6} Tao Hu⁰,⁵ Ulla Lassi⁰,^{5,6}

Kodai Takano,² Naruki Tsuji,⁷ Yosuke Amada,² Assa Aravindh Sasikala Devi[®],⁸ Matti Alatalo,⁸

Yoshiharu Sakurai ⁰,⁷ Hiroshi Sakurai ⁰,² and Arun Bansil³

¹Department of Physics, School of Engineering Science, LUT University, FI-53851 Lappeenranta, Finland

²Graduate School of Science and Technology, Gunma University, Kiryu, Gunma 376-8515, Japan

³Department of Physics, Northeastern University, Boston, Massachusetts 02115, USA

⁴Department of Physics, University of Helsinki, P.O. Box 43, FI-00014 Helsinki, Finland

⁵Research Unit of Sustainable Chemistry, University of Oulu, Oulu, Finland

⁶Kokkola University Consortium Chydenius, University of Jyvaskyla, Kokkola, Finland

⁷Japan Synchrotron Radiation Research Institute (JASRI), Sayo, Hyogo 679-5198, Japan

⁸Research Unit of Sustainable Chemistry and Materials and Mechanical Engineering, University of Oulu,

Pentti Kaiteran Katu 1, FI-90570 Oulu, Finland

(Received 7 March 2023; revised 31 August 2023; accepted 21 December 2023; published 17 January 2024)

Cobalt is used in Li-ion batteries, but it is expensive and could be replaced by nickel to deliver better performance at a lower cost. With this motivation, we discuss how the character of redox orbitals of $LiNiO_2$ can be ascertained through x-ray Compton scattering measurements combined with parallel first-principles simulations. Our analysis reveals the nature of hole states in Li-doped NiO resulting from the hybridization of O 2p and Ni 3d orbitals. Our study also gives insight into the ferromagnetic ground state and provides a pathway toward the rational design of next-generation battery materials.

DOI: 10.1103/PhysRevB.109.035139

I. INTRODUCTION

Compton scattering with hard x rays has proven to be an effective probe of redox processes in battery materials [1,2]. This bulk-sensitive spectroscopy is less sensitive to defects and surfaces compared to the related positron annihilation technique [3]. Both methods, however, provide unique windows into the nature of the redox orbitals and how their subtle characteristics, such as their localization/delocalization properties, evolve during the lithiation and delithiation processes.

The first Compton scattering study in cathode materials by Suzuki *et al.* [4] examined the $Li_x Mn_2 O_4$ (LMO) cathode and showed that the change in the shape of the Compton profile with increasing Li concentration is consistent with the appearance of states of mainly O 2p character. These authors also noted a negative excursion in the so-called "difference Compton profile" (i.e., the difference between the Compton profile of the cathode with higher Li concentration and the cathode with lower Li concentration) as a basis for adducing the presence of signatures of Mn 3d electrons becoming more itinerant (less localized) with increasing Li content. The mechanism is that when electrons enter O 2p states, they hybridize with the transition metal (TM) 3d states and induce delocalization of the Mn 3d states. A similar study in $Li_x CoO_2$ (LCO) [5] identified the aforementioned negative excursion as a descriptor for improved electrochemical operation in cationic redox reactions. In fact, this descriptor, called the

delocalization profile, was shown to correctly point to the Li concentration range that exhibits improved cathode operation in both LMO and LCO cathodes. In high-capacity Li-excess systems [6], such as $\text{Li}_x \text{Ti}_{0.4}\text{Mn}_{0.4}\text{O}_2$ (LTMO), cationic redox reactions are complemented by anionic ones [1]. The anionic redox reaction in LTMO produces a positive tail in the difference Compton profile spectrum at higher momentum, called the *Coulomb profile*, as opposed to the delocalization profile. This behavior implies that electrons introduced into O 2p states repel other electrons in the Mn 3*d* states, resulting in the localization of both O 2p and Mn 3*d* electrons.

Interestingly, a recent study by Menon *et al.* [7] utilized high-resolution oxygen *K*-edge resonant inelastic x-ray spectroscopy (RIXS) to investigate $\text{LiNi}_{0.98}W_{0.02}O_2$. This study provided insight into the crucial role of oxygen ions and presented evidence of anionic redox in this non-Li-excess system. This finding is in contrast to a previous x-ray Compton scattering study by Chabaud *et al.* [8] in LiNiO₂ (LNO) that suggested cationic redox. These contrasting results have left the question of the nature of hole states in Li-doped NiO controversial.

Here, we address the oxygen character of the redox orbital in LNO and the issues raised by RIXS experiments [9]. In this connection, utilizing high-quality LNO samples [10,11], we performed x-ray Compton scattering measurements along with parallel first-principles modeling of the associated electronic and magnetic structures. Our analysis reveals the coexistence of orbital delocalization produced by Ni-O hybridization and the presence of a dominant O 2p character in the redox orbital. Our study suggests that the electronic

^{*}veenavee.kothalawala@lut.fi

redistribution in LNO is favorable for Li-ion battery applications and the development of Ni-rich cathode materials for next-generation Li-ion batteries [12].

II. METHODS

A. Samples

Spherical Ni(OH)₂ precursors were synthesized using alkali metal hydroxide (NaOH) coprecipitation in an inert gas (nitrogen) atmosphere (see Välikangas et al. [10,11] and Zhou et al. [13] for details). Inert gas was used to prevent the oxidation of Ni(OH)₂ precursor. Precipitation was conducted in a stirred-tank reactor (CSTR) with a reactor volume of 3 L at temperatures of 50 °C under vigorous agitation. Aqueous solutions of metal sulfate NiSO4 · 6H2O, NaOH, and concentrated ammonia were fed into the reactor using peristaltic pumps. The ammonia concentration in the solution was adjusted based on the target ammonia concentration during the experiment. Particle size growth during Ni(OH)₂ coprecipitation was followed by determining the particle size distribution of the slurry sampled from the reactor's overflow tubing. The solution was heated to a precipitation temperature, and the pH was adjusted to a desired level with NaOH solution. The feeding rates of nickel sulfate, NaOH, and ammonia solutions were adjusted to maintain the desired residence time. After coprecipitation, the precursor slurry was filtered in a vacuum, and the precipitate was carefully washed with an adequate amount of de-ionized water. The synthesized Ni(OH)₂ precursors were dried overnight at 60 °C in a vacuum oven. The material was milled and sieved 40 µm in dry room conditions. Ni(OH)2 precursors were mixed with LiOH. Nonstoichiometric Li:Ni mole ratios from zero to one were used. Correspondingly, samples denoted LNO_x were obtained for x = 0, x = 0.25, x = 0.5, x = 0.75, and x = 1. The mixtures were calcined with a 2.5 °C/min heating ramp and 5 h holding time at a temperature of 670 °C under an O₂ atmosphere. The sample with a lithium concentration of x can be written as $Li_x Ni_{2-x}O_2$ as confirmed by the comprehensive sample characterization process discussed in the Supplemental Material (SM) [14]. In particular, the measured x-ray diffraction patterns are in excellent agreement with theoretical predictions by Choi et al. [15]. Notably, Välikangas et al. (2022) have demonstrated that our fully lithiated samples exhibit high capacity and excellent capacity retention. Also, since we did not cycle the cathode materials in the current Compton study, there is no Li/Ni disordering.

B. Compton profiles

The Compton profile $J(p_z)$ can be calculated within the *impulse approximation* [16,17] using the formula

$$J(p_z) = \iint \rho(\mathbf{p}) dp_x dp_y, \tag{1}$$

where $\mathbf{p} = (p_x, p_y, p_z)$ is the electron momentum, and $\rho(\mathbf{p})$ is the electron momentum density that can be expressed as

$$\rho(\mathbf{p}) = \sum_{j} n_{j} \left| \int \Psi_{j}(\mathbf{r}) \exp(-i\mathbf{p} \cdot \mathbf{r}) d^{3}\mathbf{r} \right|^{2}.$$
 (2)

The electron momentum density can be cast in terms of natural orbitals $\Psi_j(r)$, which are the eigenstates of the oneparticle density matrix of the many-electron system, and their occupation numbers, n_j [18]. Here, we consider the *independent particle model*, where $n_j = 1$ if the state is occupied and $n_j = 0$ otherwise. The magnetic Compton profile $J_{mag}(p_z)$ is given by

$$J_{\text{mag}}(p_z) = \iint [\rho_{\uparrow}(\mathbf{p}) - \rho_{\downarrow}(\mathbf{p})] dp_x dp_y, \qquad (3)$$

where $\rho_{\uparrow}(\mathbf{p})$ and $\rho_{\downarrow}(\mathbf{p})$ are the momentum densities of the majority and minority spins, respectively. The spin magnetic moment μ_{spin} is obtained by integrating $J_{mag}(p_z)$. We then calculate the spherical average of the Compton profile using Monte Carlo sampling coupled with linear interpolation.

Theoretical Compton profiles were computed using density functional theory (DFT) and the tabulated values for the deep core contributions [19]. In DFT, the electron momentum density $\rho(\mathbf{p})$ was obtained from the Kohn-Sham orbitals following Makkonen *et al.* [20] using the Vienna *ab initio* simulation package (VASP) [21,22] and the projector augmented-wave (PAW) method [23]. The generalized gradient approximation (GGA) exchange-correlation functional parametrized by Perdew, Burke, and Ernzerhof (PBE) was used [24] with a kinetic energy cutoff of 520 eV for the planewave basis set. To account for electron correlation effects, a Hubbard parameter U = 4 eV was applied to Ni 3*d* electrons following earlier studies [25–27]. The Brillouin zone of the supercell was sampled using a uniform Γ -centered $4 \times 8 \times 4$ *k*-point grid.

Compton and magnetic Compton profiles were measured at the high-energy inelastic scattering beamline 08W at the Japanese synchrotron facility SPring-8 [28,29]. Circularly polarized x rays of 182.6 keV emitted from an elliptical multipole wiggler were irradiated to the sample. The size of the incident x-ray beam at the sample position is a 1 mm square. Compton scattered x rays were measured using a pure Ge solid-state detector. The scattering angle was fixed at 178°, and Compton profiles were measured at room temperature. For magnetic Compton profiles, a magnetic field of ± 2.5 T was applied to the sample that was kept at 7 K to obtain Compton scattered x-ray intensities, I_+ and I_- , by flipping the magnetic field every 60 s.

III. RESULTS AND DISCUSSION

We begin by examining the Compton profiles of Li-doped NiO (Fig. 1). Theoretical profiles for both LNO and NiO agree well with the corresponding experimental results, indicating that the Kohn-Sham orbitals employed in our DFT calculations accurately capture the electron momentum distribution in Li-doped Ni oxide.

We isolate the signature of the redox orbital by subtracting the NiO_2 contribution from the valence Compton profile of $LiNiO_2$. The result is given by

$$\Delta J(p) = J_v^{\text{LiNiO}_2}(p) - J_v^{\text{NiO}_2}(p), \qquad (4)$$

where $J_v^{\text{LiNiO}_2}(p)$ is the spherical average valence Compton profile for LNO while $J_v^{\text{NiO}_2}(p)$ is the spherical average valence Compton profile for NiO₂. Since the experimental

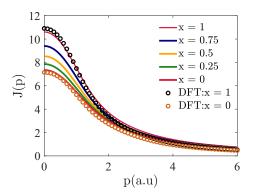


FIG. 1. Experimental and theoretical total Compton profiles (spherical averaged) for various *x* values. Theoretical profiles are convoluted with a Gaussian of 0.5 a.u. full width at half maximum. All profiles are normalized to the electrons per nickel atom (i.e., $\text{Li}_{x/(2-x)}\text{NiO}_{2/(2-x)}$).

Compton profile of NiO₂ is not available, this analysis only involves our first-principles results (Fig. 2). As discussed previously [1,5], the difference profile can be rationalized using a model with Slater orbitals, which involves two main contributions: the atomic O-2*p* Compton profile and the socalled delocalization profile. To model these contributions, we utilize the radial wave functions given by Slater orbitals, characterized by effective exponents Z_{eff} that are fitted to the DFT profile (see SM [14] for details). The importance of the O 2*p* character has been previously observed in connection with XAS experiments [30], while the existence of the delocalization profile *D*(*p*) is necessary to explain the negative excursion in the difference Compton profile. The delocalization profile

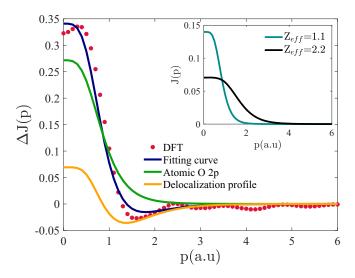


FIG. 2. Theoretical difference valence Compton profiles (spherical averaged) of LNO and NiO₂, along with the corresponding curve-fitting results (solid lines). Contributions of O 2*p* and Ni 3*d* electrons are included. The inset provides Compton profiles of Ni 3*d* orbital states for two different values of Z_{eff} . The Delocalization profile is determined by the difference between the profile for $Z_{\text{eff}} = 2.2$ and the profile for $Z_{\text{eff}} = 1.1$. The area under the negative excursion of the profiles gives the number of electrons delocalizing in the lithiation process.



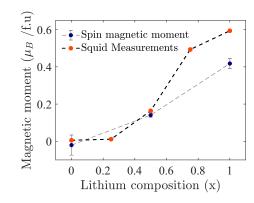


FIG. 3. Spin magnetic moments for various Li concentrations x. The dashed line is a guide to the eye.

also allows us to quantify the number of electrons delocalizing in the lithiation process in terms of the integral $\int dp |D(p)|$. We estimate this number to be 0.089 electrons per Li atom.

With the preceding results in mind, we are in a position to provide a clearer explanation of the significant physics revealed by our study regarding LNO. Our VASP first-principles calculations clearly show that the number of electrons in the interstitial region increases with increasing lithium concentration while the number of electrons on the nickel sites remains constant, as also shown by Genreith-Schriever and collaborators [31]. A similar behavior was observed by Suzuki et al. [4] in LMO. The number of electrons within the oxygen muffin-tin spheres also remains constant, although some of the additional charge in the interstitial region belongs to the oxygen atoms. These results strongly suggest a significant delocalization of oxygen 2p character and a dominant involvement of oxygen in the redox process. This process also leads to a redistribution of Ni 3d electrons and results in a favorable orbital delocalization that supports battery operation.

Goodenough and colleagues first observed the ferromagnetic nature of LNO in 1958 [32]. This intriguing ferromagnetic phase has since been confirmed by accurate diffusion quantum Monte Carlo (DQMC) calculations [33] and further discussed in a recent review by Tranquada [34]. Leveraging ferromagnetism, we conducted magnetic Compton scattering experiments on LNO samples with varying Li concentrations (x). Figure 3 shows magnetic moments as a function of x so obtained along with the values we obtained using superconducting quantum interference device (SQUID) measurements. Although the SQUID values exceed the values obtained via magnetic Compton scattering, both sets consistently yield an increasing magnetic moment with x. The discrepancy between the two measurements arises from the fact that SQUID measures the total moment (i.e., orbital and spin moment), while magnetic Compton scattering only provides the spin moment.

Notably, the magnetic moment in our case did not reach saturation under the field of 2.5 T, which was used in both the magnetic Compton scattering and SQUID experiments. This lack of saturation is a significant factor contributing to the discrepancy between our measurement and our theoretical predictions, which give a magnetic moment of $1\mu_B$ for x = 1.

Magnetic Compton profiles for x = 1 and x = 0.5 exhibit a remarkable similarity in that the two profiles can be

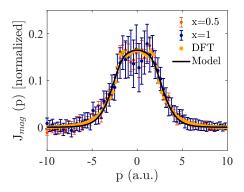


FIG. 4. Magnetic Compton profiles (spherical averaged) for x = 1, and x = 0.5. The DFT calculation is for x = 1.

collapsed onto a single curve when normalized to the same scale (Fig. 4). It is important to distinguish between the difference Compton profile and the magnetic Compton profiles, as they offer complementary insights into the redox and magnetic orbitals, respectively [35]. To capture the shape of the magnetic Compton profile, we employed a fitted model using a Ni 3d Slater orbital with $Z_{eff} = 3.8$. Additionally, we included a small magnetic contribution from O 2p orbitals with $Z_{\text{eff}} = 1.1$, reflecting the mixing of a few percent due to the presence of a small local magnetic moment on the oxygen site. This fitted model is consistent with the LNO spin density calculated within the DFT, as shown in Fig. 5. Interestingly, our findings indicate a positive magnetization on the O atom, while the DQMC [33] predicts a negative contribution because of the approximate $R\bar{3}m$ crystal symmetry used in the DQMC calculation.

IV. CONCLUSION

We utilize x-ray Compton scattering along with parallel first-principles modeling to investigate the electronic structure of LNO cathode materials to gain insight into the delithiation process of going from LiNiO₂ to NiO₂. By directly measuring the electron density distribution (spherically averaged) of individual orbitals in momentum space, we showcase the unique ability of the Compton scattering technique to extract redox and magnetic orbitals realistically. Our analysis reveals that

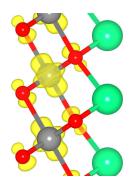


FIG. 5. Spin density in LNO using an isosurface value of 0.01 a.u. on Li (green), Ni (gray), and O (red).

the Ni charge in NiO, NiO₂, and LiNiO₂ is the same, while the occupation of oxygen orbitals changes with lithiation, indicating that O dominates the underlying charge-transfer mechanism. These results help explain oxygen loss in Ni-rich layered cathode materials, reported in recent RIXS experiments [7]. Our study also sheds light on the role of 3d electron delocalization in the layered LNO chemistry, highlighting its importance in the redox processes.

ACKNOWLEDGMENTS

K.S. was supported by JSPS KAKENHI Grants No. JP19K05519, No. 21KK0095, and No. 22H02103. Compton and magnetic Compton scattering experiments were performed with the approval of JASRI (Proposal No. 2022A1454). Magnetization measurements were performed with the approval of the National Institute of Material Science (NIMS) Open Facility (Proposals No. 22NM8130 and No. 22NM8141). K.S. and Y.A. thank Shigeki Nimori for his support of the magnetization measurements. Part of this work at Northeastern University was supported by the Office of Naval Research Grant No. N00014-23-1-2330, and the work benefited from Northeastern University's Advanced Scientific Computation Center and the Discovery Cluster. The authors wish to acknowledge CSC-IT Centre for Science, Finland, for computational resources.

- H. Hafiz, K. Suzuki, B. Barbiellini, N. Tsuji, N. Yabuuchi, K. Yamamoto, Y. Orikasa, Y. Uchimoto, Y. Sakurai, H. Sakurai, A. Bansil, and V. Viswanathan, Tomographic reconstruction of oxygen orbitals in lithium-rich battery materials, Nature (London) **594**, 213 (2021).
- [2] J. Nokelainen, B. Barbiellini, J. Kuriplach, S. Eijt, R. Ferragut, X. Li, V. Kothalawala, K. Suzuki, H. Sakurai, H. Hafiz, K. Pussi, F. Keshavarz, and A. Bansil, Identifying redox orbitals and defects in lithium-ion cathodes with compton scattering and positron annihilation spectroscopies: A review, Condensed Matter 7, 47 (2022).
- [3] G. Pagot, V. Di Noto, K. Vezzù, B. Barbiellini, V. Toso, A. Caruso, M. Zheng, X. Li, and R. Ferragut, Quantum view of Liion high mobility at carbon-coated cathode interfaces, iScience 26, 105794 (2023).
- [4] K. Suzuki, B. Barbiellini, Y. Orikasa, N. Go, H. Sakurai, S. Kaprzyk, M. Itou, K. Yamamoto, Y. Uchimoto, Y. J. Wang, H. Hafiz, A. Bansil, and Y. Sakurai, Extracting the redox orbitals in Li battery materials with high-resolution x-ray Compton scattering spectroscopy, Phys. Rev. Lett. 114, 087401 (2015).
- [5] B. Barbiellini, K. Suzuki, Y. Orikasa, S. Kaprzyk, M. Itou, K. Yamamoto, Y. J. Wang, H. Hafiz, R. Yamada, Y. Uchimoto, A. Bansil, Y. Sakurai, and H. Sakurai, Identifying a descriptor for *d*-orbital delocalization in cathodes of Li batteries based on x-ray Compton scattering, Appl. Phys. Lett. **109**, 073102 (2016).
- [6] G. Assat and J.-M. Tarascon, Fundamental understanding and practical challenges of anionic redox activity in Li-ion batteries, Nat. Energy 3, 373 (2018).
- [7] A. S. Menon, B. Johnston, S. G. Booth, L. Zhang, K. Kress,B. Murdock, G. Fajardo, N. N. Anthonisamy, N. T. Ruiz,

S. Agrestini, K. Zhou, T. Lee, A. Nedoma, S. Cussen, and L. Piper, Oxygen-redox activity in non-Li-excess W-doped LiNiO₂ cathode, ChemRxiv (2022).

- [8] S. Chabaud, C. Bellin, F. Mauri, G. Loupias, S. Rabii, L. Croguennec, C. Pouillerie, C. Delmas, and T. Buslaps, Electronic density distortion of NiO₂ due to intercalation by Li, J. Phys. Chem. Solids 65, 241 (2004).
- [9] N. Li, S. Sallis, J. K. Papp, J. Wei, B. D. McCloskey, W. Yang, and W. Tong, Unraveling the cationic and anionic redox reactions in a conventional layered oxide cathode, ACS Energy Lett. 4, 2836 (2019).
- [10] J. Välikangas, P. Laine, M. Hietaniemi, T. Hu, P. Tynjälä, and U. Lassi, Precipitation and calcination of high-capacity LiNiO₂ cathode material for lithium-ion batteries, Appl. Sci. 10, 8988 (2020).
- [11] J. Valikangas, P. Laine, M. Hietaniemi, T. Hu, M. Selent, P. Tynjälä, and U. Lassi, Correlation of aluminum doping and lithiation temperature with electrochemical performance of LiNiO cathode material, J. Solid State Electrochem. 27, 641 (2022).
- [12] M. Bianchini, M. Roca-Ayats, P. Hartmann, T. Brezesinski, and J. Janek, There and back again—the journey of LiNiO₂ as a cathode active material, Angew. Chem., Int. Ed. 58, 10434 (2019).
- [13] F. Zhou, X. Zhao, van A. Bommel, A. Rowe, and J. R. Dahn, Coprecipitation synthesis of $Ni_x Mn_{1-x}(OH)_2$ mixed hydroxides, Chem. Mater. **22**, 1015 (2010).
- [14] See Supplemental Material at http://link.aps.org/supplemental/ 10.1103/PhysRevB.109.035139 for the characterization of the samples and about the DFT calculations (DOS), which includes Refs. [36–39].
- [15] D. Choi, J. Kang, and B. Han, Unexpectedly high energy density of a Li-ion battery by oxygen redox in LiNiO₂ cathode: First-principles study, Electrochim. Acta **294**, 166 (2019).
- [16] I. G. Kaplan, B. Barbiellini, and A. Bansil, Compton scattering beyond the impulse approximation, Phys. Rev. B 68, 235104 (2003).
- [17] M. Cooper, P. Mijnarends, N. Shiorani, N. Sakai, and A. Bansil, in *X-Ray Compton Scattering* (Oxford University Press, Oxford, UK, 2004), pp. 31–39.
- [18] B. Barbiellini and A. Bansil, Treatment of correlation effects in electron momentum density: Density functional theory and beyond, J. Phys. Chem. Solids 62, 2181 (2001).
- [19] F. Biggs, L. Mendelsohn, and J. Mann, Hartree-Fock Compton profiles for the elements, At. Data Nucl. Data Tables 16, 201 (1975).
- [20] I. Makkonen, M. Hakala, and M. Puska, Calculation of valence electron momentum densities using the projector augmentedwave method, J. Phys. Chem. Solids 66, 1128 (2005).
- [21] G. Kresse and J. Furthmüller, Efficiency of ab-initio total energy calculations for metals and semiconductors using a plane-wave basis set, Comput. Mater. Sci. 6, 15 (1996).

- [22] G. Kresse and D. Joubert, From ultrasoft pseudopotentials to the projector augmented-wave method, Phys. Rev. B 59, 1758 (1999).
- [23] P. E. Blöchl, Projector augmented-wave method, Phys. Rev. B 50, 17953 (1994).
- [24] J. P. Perdew, K. Burke, and M. Ernzerhof, Generalized gradient approximation made simple, Phys. Rev. Lett. 77, 3865 (1996).
- [25] M. Tuccillo, O. Palumbo, M. Pavone, A. Muñoz-García, A. Paolone, and S. Brutti, Analysis of the phase stability of LiMO₂ layered oxides (M = Co, Mn, Ni), Crystals **10**, 526 (2000).
- [26] L. Wang, T. Maxisch, and G. Ceder, Oxidation energies of transition metal oxides within the GGA + U framework, Phys. Rev. B 73, 195107 (2006).
- [27] V. N. Kothalawala, A. A. S. Devi, J. Nokelainen, M. Alatalo, B. Barbiellini, T. Hu, U. Lassi, K. Suzuki, H. Sakurai, and A. Bansil, First principles calculations of the optical response of LiNiO₂, Condens. Matter 7, 54 (2022).
- [28] Y. Sakurai, High-energy inelastic-scattering beamline for electron momentum density study, J. Synchrotron Radiat. 5, 208 (1998).
- [29] Y. Kakutani, Y. Kubo, A. Koizumi, N. Sakai, B. L. Ahuja, and B. K. Sharma, Magnetic Compton profiles of fcc-Ni, fcc-Fe₅₀Ni₅₀ and hcp-Co, J. Phys. Soc. Jpn. **72**, 599 (2003).
- [30] P. Kuiper, G. Kruizinga, J. Ghijsen, G. A. Sawatzky, and H. Verweij, Character of holes in Li_xNi_{1-x}O and their magnetic behavior, Phys. Rev. Lett. **62**, 221 (1989).
- [31] A. R. Genreith-Schriever, H. Banerjee, A. S. Menon, E. N. Bassey, L. F. Piper, C. P. Grey, and A. J. Morris, Oxygen hole formation controls stability in LiNiO₂ cathodes, Joule 7, 1623 (2023).
- [32] J. B. Goodenough, D. G. Wickham, and W. J. Croft, Some ferrimagnetic properties of the system Li_xNi_{1-x}O, J. Appl. Phys. 29, 382 (1958).
- [33] K. Saritas, E. R. Fadel, B. Kozinsky, and J. C. Grossman, Charge density and redox potential of LiNiO₂ using *ab initio* diffusion quantum Monte Carlo, J. Phys. Chem. C **124**, 5893 (2020).
- [34] J. M. Tranquada, John Goodenough and the many lives of transition-metal oxides, J. Electrochem. Soc. 169, 010535 (2022).
- [35] K. Suzuki, Y. O. K. Hoshi, H. Sakurai, N. Tsuji, K. Yamamoto, N. Yabuuchi, H. Hafiz, Y. Orikasa, Y. Uchimoto, Y. Sakurai, V. Viswanathan, A. Bansil, and B. Barbiellini, Magnetic compton scattering study of Li-rich battery materials, Condens. Matter 7, 4 (2022).
- [36] FE-SEM, Carl Zeiss Microscopy GmbH, Germany.
- [37] A Rigaku SmartLab.
- [38] Thermo Electron iCAP 6500 Duo, Thermo Fisher Scientific, USA.
- [39] Quantum Design Japan, Inc.