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


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Strain effects in phosphorus bound exciton transitions in silicon

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Donor spin states in silicon are a promising candidate for quantum information processing. One possible donor spin readout mechanism is the bound exciton transition that can be excited optically and creates an electrical signal when it decays. This transition has been extensively studied in the bulk, but in order to scale towards localized spin readout, microfabricated structures are needed for detection. As these electrodes will inevitably cause strain in the silicon lattice, it will be crucial to understand how strain affects the exciton transitions. Here we study the phosphorus donor bound exciton transitions in silicon using hybrid electro-optical readout with microfabricated electrodes. We observe a significant zero-field splitting as well as mixing of the hole states due to strain. We can model these effects assuming the known asymmetry of the hole g factors and the Pikus-Bir Hamiltonian describing the strain. In addition, we describe the temperature, laser power, and light polarization dependence of the transitions. Importantly, the hole mixing should not prevent donor electron spin readout, and using our measured parameters and numerical simulations, we anticipate that hybrid spin readout on a silicon-on-insulator platform should be possible, allowing integration into silicon photonics platforms.

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I. INTRODUCTION

Donor spin qubits in silicon are a promising candidate for processing quantum information [1–10]. Their application potential is, however, somewhat constrained by the lack of an optical interface, and considerable attention has been recently focused on spin-photon interfaces in silicon [11–15]. One possible readout avenue is the donor bound exciton transition [16–20], which, however, decays mostly via Auger recombination hence not enabling an efficient optical readout protocol. Hybrid electro-optical readout, where the spin-selective transition is excited optically, but the readout is done electrically, is possible and has been demonstrated with both direct electrical and capacitive readout [21] in bulk. Scaling the electro-optical readout towards the single-spin level will, however, require moving to microfabricated structures as well as most likely taking advantage of silicon photonics platforms. So far, only one demonstration using microfabricated electrodes exists [22], and the integration to photonics platforms remains an open challenge. The latter will require moving to silicon-on-insulator (SOI) substrates, where photoluminescence measurements have shown the existence of the bound exciton transition [23] but no electrical readout has been demonstrated.

One open question when moving towards microfabricated structures on SOI substrates is the role of strain in the exciton readout. At low temperatures the different thermal expansion coefficients of silicon and metal cause sharp strain profiles around the electrodes. This might be especially important when all the spins are located in the surface layer in an SOI structure (although see Sec. VII for further discussion on this

point). Several recent studies [24–26] have highlighted how strain can substantially change the donor spin states and their decoherence properties. Substantially less attention in this context has so far been paid to strain effects of the hole and exciton states.

Here we report experiments demonstrating the electro-optical donor exciton response using microfabricated electrodes and focused light on doped natural silicon. We have performed experiments on both silicon grown with the Czochralski method (CZ) and float-zone method (FZ). All data shown are from the FZ silicon unless otherwise mentioned. The strain from the on-chip electrodes creates significant effects but importantly does not create any fundamental obstacles for localized spin readout. We found strain-induced heavy-hole–light-hole splitting to be significant in all samples, and we see evidence of avoided crossings between the heavy-hole and light-hole transitions indicating a coupling term in the Hamiltonian. We can model these effects with remarkable agreement assuming the known asymmetry of the hole g factors and the Pikus-Bir Hamiltonian describing the strain, but we also have unresolved questions regarding temperature dependence and the light polarization response, which is complicated by the mixing of the different hole states. Nevertheless, using the extracted parameters, we predict with numerical simulations how the exciton signal should behave in an SOI structure where the strain effects must be considered with care.

II. EXPERIMENTAL SETUP

At low temperatures, phosphorus donors in a silicon lattice can bind an electron around them in a Coulomb potential forming a system that resembles a hydrogen atom but with a Bohr radius of around 1.8 nm [27]. The spin of this bound

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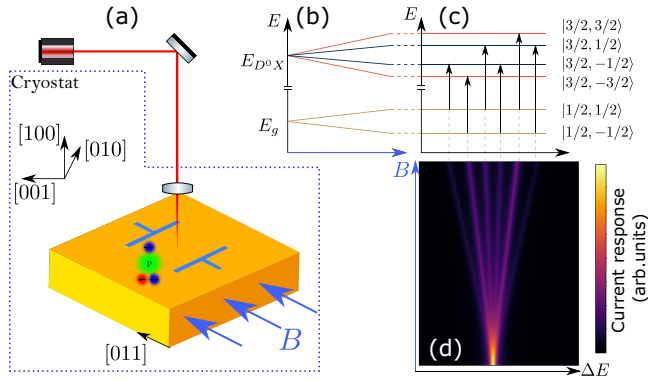


FIG. 1. (a) A schematic of our sample, the measurement geometry, and the optical setup. Light is guided to the sample in free space via a fixed lens. The magnetic field is in-plane and parallel to the direction of measured current and the [011] crystal direction. (b) Energy level diagram showing the Zeeman splitting of donor electron (E_g) and hole (E_{D^0X}) states. (c) Arrows showing the six allowed exciton transitions in a nonzero magnetic field. (d) Simulated current signal of the exciton transitions as a function of magnetic field in strain-free silicon. Transition brightness corresponds to the Clebsch-Gordan coefficient of the transition.

electron, in combination with the phosphorus nuclear spin, has been shown to be a promising quantum computing unit [1,5]. Unfortunately for optical applications, the loose binding potential means that the “atomic” transitions of this system are in the technologically inconvenient terahertz regime. There is nevertheless a bound exciton transition at a more technologically convenient 1078 nm wavelength. The electron of the exciton will form a singlet pair with the donor electron, leaving the hole $\frac{3}{2}$ -spin as the spin degree of freedom in the bound exciton state. Hence there are six allowed transitions between the original donor spin state and the exciton state in a finite magnetic field; these are depicted in Figs. 1(b) and 1(c). We neglect the hyperfine coupling between the donor electron spin and the nuclear spin throughout this paper as our linewidths are not narrow enough to resolve it. This could be ameliorated by moving to isotopically pure silicon [6,17]. As any single transition originates from a particular donor electron spin state, the existence or nonexistence of these transitions can be used for electron spin readout. The decay of the exciton happens mostly via Auger recombination, ending up with an ionized donor and an extra “hot” electron now in the conduction band. This causes a change in the conductivity of the silicon, which we detect.

The measurement scheme is presented in Fig. 1(a). The samples studied are uniformly doped silicon chips onto which two gold electrodes with length of 100 μm separated by 60 μm (CZ sample) or 100 μm (FZ sample) are fabricated using electron beam lithography and lift-off techniques. Experiments were carried out inside a “dry” dilution fridge, which, however, is mostly operated at 3.3 K temperatures for the data presented here. The laser spot diameter is roughly 50 μm in the data presented, and hence it is far from the diffraction limit. The sample is placed on a piezoelectric stage, which allows us to align and focus the laser spot with the readout electrodes using an infrared camera outside the cryostat. The electrodes connect to a voltage (CZ measurements) or a current source

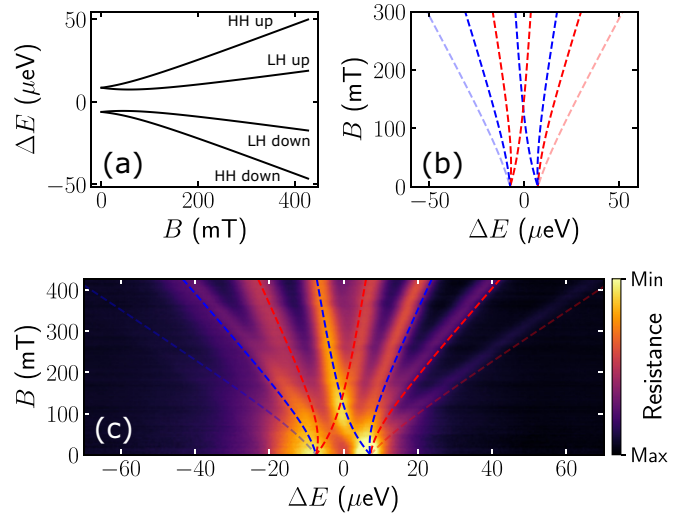


FIG. 2. (a) Strain split hole eigenenergies and (b) exciton transition energies calculated using Eqs. (1)–(3). B is the applied external magnetic field. The magnetic field lies in the [011] crystal direction. The labels show the dominating state at high magnetic fields. (c) Measured transition energies as a function of the magnetic field, in the [011] direction, overlaid with the calculated transition energies presented in (b). The center transition frequency is adjusted to match the data. Blue lines indicate transitions involving the donor electron spin-up state, and red lines indicate transitions coming from the donor electron spin-down state. Transitions that are forbidden without the hole mixing are shown with transparent lines.

(FZ measurements), and measured signals are amplified using low-noise amplifiers. Current-voltage characteristics of the sample are presented in the Supplemental Material [28]. We have light-emitting diodes (LEDs; peak wavelength 1020 nm) inside the cryostat to provide light with energy above the silicon band gap. The magnetic field direction is perpendicular to the light propagation direction, meaning that we are using the Voigt geometry here, allowing us to address all the transitions with linearly polarized light. The magnet is calibrated with a Hall sensor. We have a small uncertainty in the location of the sample with regard to the calibration location, from which we estimate a conservative error range of $\pm 5\%$ for the magnetic field calibration. See Supplemental Material [28] for more details about the measurement setup.

Figures 1(b) and 1(c) show schematically the six allowed bound exciton transitions, and Fig. 1(d) depicts the signal we would expect to get in different magnetic fields. The actual measured signal is shown in Fig. 2(c). There are several main differences which we assign to the effects of strain.

III. MAGNETIC FIELD DEPENDENCY AND STRAIN EFFECTS

As explained above, the transitions we observe happen essentially between a single-electron spin state (D_0) and a hole spin state (D_0X). Hence we need to write down the Hamiltonians for both the originating and the final state of the system, while taking strain effects into consideration. We note that we do not try to model the center frequency of the transition but rather only the magnetic field dependency. Our center transition frequency at zero field (1078.180 ± 0.015 nm) is

close to what has been reported before [18,29,30]; we assign the slight discrepancy to the substrate material, which is not especially free of impurities.

The magnetic field dependency of the neutral donor state is assumed to simply follow

$$H_D^Z = \frac{1}{2}\mu_B g_d \mathbf{B} \cdot \boldsymbol{\sigma}, \quad (1)$$

where μ_B is the Bohr magneton, $g_d = 1.9985$ is the donor electron g factor, \mathbf{B} is the magnetic field vector, and $\boldsymbol{\sigma}$ is a vector containing the Pauli spin matrices. We assume an isotropic g factor for the donor electron, although the isotropy might be broken by strain [25,31]. Nevertheless, the expected anisotropy is of the order of 10^{-3} [32], much smaller than the strain effects for the holes as we will show below, and can be neglected here. We also neglect the hyperfine interaction since we cannot resolve it. There is also strain variation in the electron energy levels coming from the variation of the hyperfine interaction as a function of strain, but these variations are expected to be small [24–26,31] compared with the effects we study here.

For the magnetic field dependence of the hole we use the anisotropic g -factor model [33]

$$H_B^Z = \mu_B(g_1 \mathbf{J} \cdot \mathbf{B} + g_2 \mathbf{J}^3 \cdot \mathbf{B}), \quad (2)$$

where \mathbf{J} is a vector containing $\frac{3}{2}$ -spin matrices in the x , y , and z directions, which we take to correspond to the crystal directions of [100], [010], and [001], respectively (this ensures we match the strain directions in Eq. (3) below), \mathbf{B} is the magnetic field vector, and g_1 and g_2 are the isotropic and anisotropic g factors, respectively.

Neglecting the strain effects, that is, only using Hamiltonians described by Eq. (1) for the donor and Eq. (2) for the hole, we get the exciton transition lines shown in Fig. 1(d). Comparing these with our actual measurement data shown in Fig. 2(c) reveals several features not described by the model. The most prominent discrepancy is the existence of two peaks at zero magnetic field. We assign this zero-field splitting (ZFS) to the splitting of the heavy-hole and light-hole states caused by strain. The strain effects affecting hole states in silicon are conventionally modeled with the Pikus-Bir strain Hamiltonian [34]

$$H_{PB}(\epsilon) = a \text{Tr}(\epsilon) + b \sum_{i=x,y,z} \left(J_i^2 - \frac{\mathbf{J}^2}{3} \right) \epsilon_{ii} + \frac{d}{\sqrt{3}} \sum_{i \neq j} (J_i J_j + J_j J_i) \epsilon_{ij}, \quad (3)$$

where ϵ is the strain matrix and a , b , and d are deformation potentials. The parameter a only changes the center frequency of the transition and is not important for our model here. The other factors, b and d , we use as fit parameters. The extracted values are listed in Table I. For strain, we use values from a COMSOL simulation of the strain caused by the different thermal expansion coefficients of silicon, the metallic electrodes, and the stage; see Appendix B for details. Note that as the strain and parameters b and d are always multiplied, any discrepancy in the strain parameters will then directly affect these values.

TABLE I. Extracted values for deformation potentials b and d along with hole g factors g_1 and g_2 from fitting Eqs. (3) and (2) to the data shown in Fig. 2(c). Reference values for b and d are taken from Ref. [35]. Reference values for g_1 and g_2 in the [100] and [111] orientations are from Ref. [16]. g_{LH} and g_{HH} were calculated using Eqs. (C1)–(C4). The reference values in the [011] orientation are taken from Ref. [36].

	b (eV)	d (eV)	g_1	g_2	g_{LH}	g_{HH}
This paper, [011]	−7	−4	0.83	0.22	1.40	1.28
Reference	−2.2	−5.1				
Reference, [100]			0.8	0.24	0.86	1.34
Reference, [111]			0.86	0.21	1.57	1.27
Reference, [011]			0.83	0.225	1.409	1.285

By itself the Pikus-Bir strain Hamiltonian simply splits the states at zero field. However, the anisotropic component of the Zeeman Hamiltonian [g_2 in Eq. (2)] causes coupling of the hole states, and we get the avoided crossings between the transitions [Figs. 2(a) and 2(b)], which we clearly also see in the measured data. Using just these equations, we can get a remarkable agreement with the data, as shown in Fig. 2(c). We use the QUTIP PYTHON package [37,38] to calculate the transition energies numerically from the Hamiltonians above.

Notably, we find that the data show eight transition lines instead of six. The two extra lines are the outermost and less bright lines. These transitions are seemingly violating the transition selection rules $\Delta m = m_h - m_e = -1, 0, 1$, where m_h and m_e are the hole and electron spins, respectively. However, due to the mixing of the hole states at low fields (close to the avoided crossings) these transitions are not strictly forbidden. As the magnetic field increases, the forbidden transition lines are getting fainter, which is the expected result, since the hole states become less mixed and the spin values of the hole states are getting better defined at higher magnetic fields.

From the data in Fig. 2(c) we can also extract the g factors (g_d, g_1, g_2) defined in Eqs. (1) and (2). The donor electron g -factor g_d anisotropy and strain dependence are well studied, and we use the literature value 1.9985 for all data. The hole g factors are known to have strong anisotropy between different crystal orientations [16,36,39]. Here we determine the hole g factors in the [011] orientation, and fits to the data give the g_1 and g_2 parameters shown in Table I. Our g_1 and g_2 are well in line with the measurements in other crystal directions and also agree well with the values obtained in Ref. [36] in the high-magnetic-field quadratic Zeeman regime. Using the measured g_1 and g_2 , we can also extract the g factors for heavy holes and light holes (the slopes of the transitions if there were no strain-induced crossings), g_{LH} and g_{HH} . These values are also shown in Table I with known literature values for several crystal orientations. Details of the analytical calculation of g_{LH} and g_{HH} are shown in Appendix C. Their values can also be extracted numerically.

IV. POLARIZATION DEPENDENCE

In all optical transitions the polarization of the absorbed or emitted light is intimately tied to the spin angular momentum change of the transition. Thus we would also expect a polar-

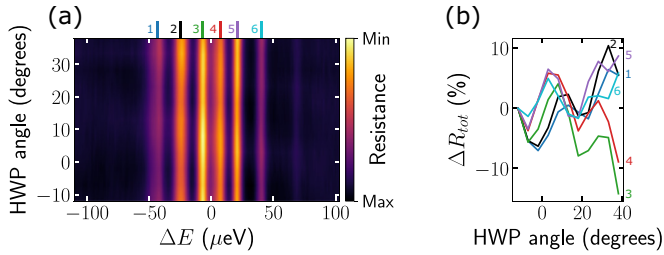


FIG. 3. (a) Half-wave-plate (HWP) angle dependence on the exciton signal at 427 mT. (b) Peak height profiles for each of the transitions. ΔR_{tot} is the change in total resistance. Color labels are given at the top of (a). Each line is normalized to start from zero in (b). The absence of proper polarization control is due to hole mixing. There is still a small trend visible where the middle transitions, transitions 3 and 4 (π transitions in the absence of hole mixing), get weaker and the other transitions (σ transitions in absence of hole mixing) get stronger from left to right as would be expected. This trend is partially obscured by some parasitic polarization-dependent power oscillations (the “fast” oscillations) in the data.

ization dependence of the transitions, based on the change in the spin quantum number Δm . As can be seen from the energy level diagram in Fig. 1(c), there are two transitions with $\Delta m = -1, 0, 1$ each. To convert these into the expected light polarization, one must also consider the relative direction of the light with regard to the magnetic dipole moment. In our geometry, where the magnetic field is perpendicular to the light travel direction (Voigt geometry), we would expect to be able to excite the $\Delta m = 0$ transitions (π transitions) with one linear polarization component and the $\Delta m = \pm 1$ components (σ transitions) with the orthogonal linear polarization.

The hole mixing changes this picture as the hole spin states are no longer well defined, and hence also the polarization dependence of the transitions is relaxed. Indeed, we see only a very small polarization dependence in our signal as can be seen in Fig. 3, where the polarization dependence of the signal is depicted at 427 mT. We see all six allowed transitions at all polarizations even at this field, with only a very slight variation in the amplitude. We also can still distinguish both forbidden transitions (the higher-energy one being significantly brighter), the appearance of which shows that there is still a significant amount of hole spin state mixing. (This is also apparent in our numerical modeling based on the parameters above.)

V. ABOVE-BAND-GAP LIGHT, LASER POWER DEPENDENCY, AND LINEWIDTHS

We now turn to the more technical details of the hybrid electro-optic readout. First, for a good signal-to-noise ratio it seems to be crucial to provide above-band-gap light. In Fig. 4(a) we show the zero-magnetic-field data measured at different optical powers, with and without the LEDs providing the above-band-gap light. It is obvious that the effect of the LEDs is considerable in increasing the signal. This is due to the extra electrons in the conduction band allowing for faster charge neutralization rate of the donors, increasing the “recycling” rate of electrons and hence the measured current, as has also been reported before [18,19,22].

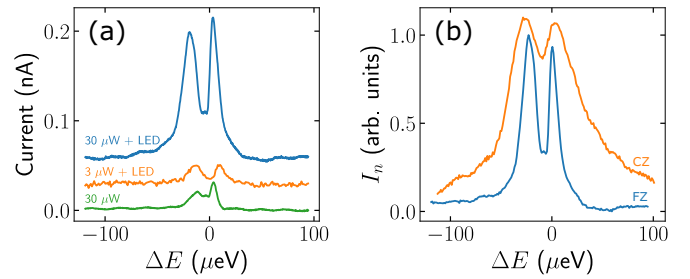


FIG. 4. (a) Laser power dependence of the exciton signal at zero magnetic field. Current values are offset to show the difference in the peak heights. The base current difference between LED-on and LED-off measurements is ≈ 3.5 nA. (b) Exciton transition at zero applied magnetic field for CZ and FZ silicon. Current values are normalized, and CZ data are offset to illustrate the difference in the linewidths. CZ data were captured without LED illumination, and FZ data were captured with LEDs. The laser power was the same in both measurements.

Interestingly, the shape of the zero-field data changes when the above-band-gap light is either on or off. When the LEDs are on, the zero-field data do not have a dependency on the laser power, as shown in Fig. 4(a), showing a constant ZFS of roughly 23 μeV . However, when the LEDs are off, we see a significant change in the shape of the data. Naively fitting still a two-peak function to the LED-off data would lead to a ZFS to roughly 15 μeV . If this would imply a ZFS change due to heating from the LEDs changing strain, the sample would be heating up to 100 K according to COMSOL simulations, which is not possible as at these temperatures neither the donor electrons nor the excitons would be bound.

Figure 4(b) shows comparison data at zero applied magnetic field in CZ and FZ samples. As is clearly visible the linewidth improves considerably when moving to FZ silicon, as is expected from the lower concentration of oxygen and carbon impurities [29]. The difference in the doping levels might also have a small effect [40]. In the CZ sample the full width at half maximum (FWHM) values are roughly 25 μeV , whereas in FZ we see a linewidth of 8 μeV for the lower energy peak and 5 μeV for the higher energy peak. When fitting to data acquired at a high magnetic field, we find FWHM values in the range 3–5 μeV , which is well in line with values reported before for natural silicon [30].

VI. MILLIKELVIN MEASUREMENTS

In addition to 3.3-K measurements, we also performed measurements at millikelvin temperatures. However, we did not see a significant difference compared with the 3.3-K data when a high laser power of 30 μW was used, as shown in Figs. 5(a) and 5(c) (sample stage thermometer temperature 115 mK). We assume that the heating from the laser power was enough to basically keep the sample at the same temperature as before (it also raised the fridge temperature). When the laser power was reduced to one-tenth of the high laser power, the signal became very weak, and we observe a very different pattern; see Figs. 5(b) and 5(d) (sample stage thermometer temperature 45 mK). LEDs providing above-band-gap light were on in both measurements. We cannot explain the

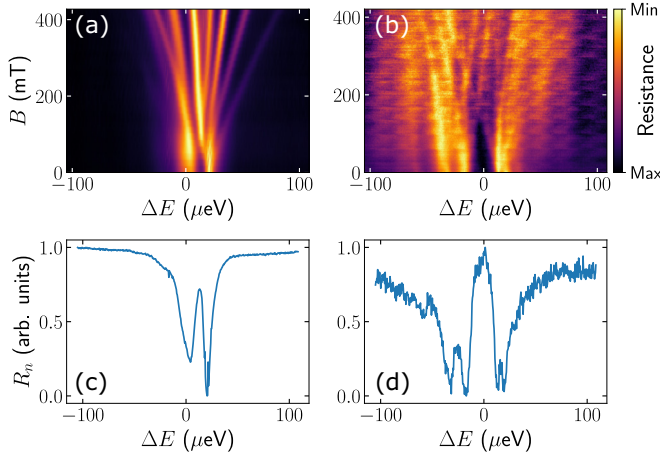


FIG. 5. Measured magnetic field dependence of the exciton spectrum at millikelvin temperatures with (a) 30 μW (sample stage temperature 115 mK) and (b) 3 μW of laser power (sample stage temperature 45 mK). (c) and (d) show crosscuts at zero magnetic field. R_n is the normalized resistance.

low-power data with strain effects, since the thermal contraction at low temperatures should be negligible. We note that “additional” zero-field splitting has been observed before at 1.4 K temperatures [18] and was attributed to other charge centers interacting with the spin state. However, the additional splitting in Ref. [18] is one to two orders of magnitude smaller than what we report here.

VII. DISCUSSION AND FUTURE OUTLOOK

We have characterized the phosphorus bound exciton transitions in silicon using hybrid electro-optical readout. The inevitable strain coming from the electrodes needed for this readout method causes hole mixing, which both complicates the analysis of the transitions and prevents polarization dependent addressing of the exciton transitions. Importantly, it does not, however, fundamentally prevent electron spin readout.

The strain can be seen as an unwanted property, when dealing with sensitive exciton transitions, but it could also be useful for tuning them. However, the tuning needs to take place already in the design of the system. Strain engineering in microelectromechanical systems is already a widely studied topic [41]; so the methods for the strain tuning are already available. This could be useful for, e.g., purposefully matching the transition frequency for photonic components.

We have also directly measured the heavy-hole and light-hole g factors in the [011] orientation, and our results confirm the expectation from the g_1 and g_2 measured at other crystal orientations and at higher fields at this orientation. Indeed, we get a remarkable agreement between theory and experiment for the magnetic field dependency using the Pikus-Bir strain Hamiltonian. It is notable that the g -factor anisotropy of holes also allows one to tune the exciton transition position just by rotating the sample, which could be done *in situ* with a rotating stage.

For widespread applications, it would be beneficial to integrate the hybrid readout with silicon photonics components. This would require integrating the readout electronics with

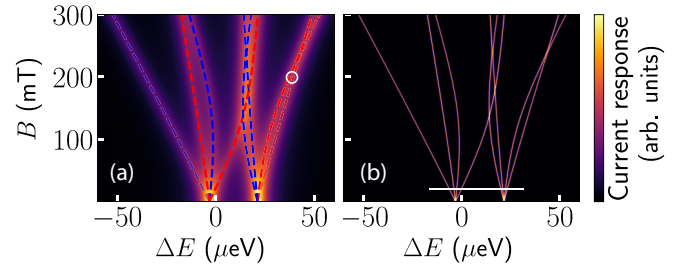


FIG. 6. Simulated exciton transitions on a SOI platform in (a) natural silicon and (b) 99.991% enriched ^{28}Si . B is the applied external magnetic field, and ΔE is the transition energy offset from the value without strain or magnetic field. Simulation parameters are presented in Table I, and strain is taken from simulations shown in Appendix B. The transition linewidth in (a) is the bulk value we have extracted from natural silicon, 4 μeV , and the transition linewidth in (b) is 150 neV as reported in Ref. [18]. The white ring in (a) shows possible spin readout conditions in natural silicon at just below 200 mT, where the transition is isolated enough to be addressed optically, and similarly for the white line in (b) at 20 mT.

SOI devices, where strain effects can be increased due to the thin device layer. On the other hand, in a SOI substrate it is easy to suspend the device layer. If one then places the readout electronics on the nonsuspended part, the strain caused by the electrodes around the donors is actually *decreased* compared with the bulk case (see strain simulations in Appendix B). More importantly, with our simulation parameters all the strain components have completely flat profiles in the suspended parts, as we leave 10- μm space between the electrode and the suspended Si film. This uniformity in the strain field will be crucial for any larger-scale architecture in order to avoid inhomogeneous broadening of the exciton transition.

If in addition isotopically pure silicon is used, the ensemble linewidths could be extremely narrow. Previously, it has been reported that the exciton transitions in 99.991% isotopically enriched ^{28}Si have a FWHM of 150 neV [18]. We show expected (simulated) signals from the SOI samples made with natural silicon and enriched ^{28}Si in Fig. 6 using the measured parameters and strain values from the SOI simulation (assuming a strain-free substrate at room temperature). From these it is expected that hybrid electro-optical spin readout should be possible in SOI platforms at low magnetic fields.

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APPENDIX A: SAMPLES

The CZ wafer used was a 380- μm -thick phosphorus-doped wafer acquired from Okmetic Oy with crystal direction (100). The wafer resistivity range at room temperature was

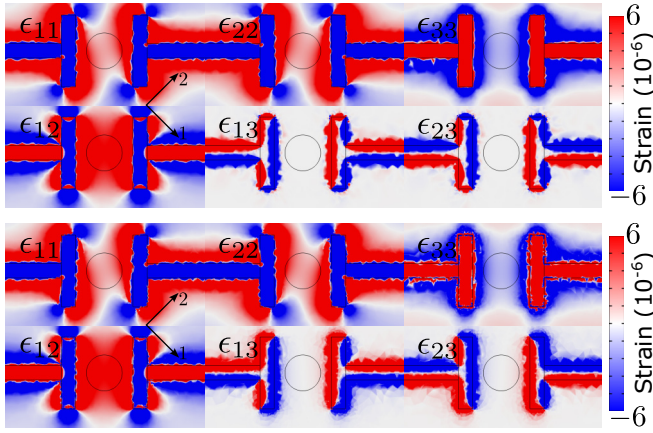


FIG. 7. Simulated strain tensor elements on the sample surface (top) and at 1 μm depth (bottom) in the bulk sample. The black arrows show the coordinate directions, and the circle between the electrodes shows the location and size of the laser spot.

specified to be 0.2–0.25 Ωcm , meaning doping levels of $(2.4\text{--}3.2) \times 10^{16} \text{ cm}^{-3}$. The FZ wafer used was a 200- μm -thick phosphorus-doped wafer acquired from Sil’Tronix ST with crystal direction (100). The wafer resistivity range at room temperature was specified to be 1–5 Ωcm , meaning doping levels of $0.9\text{--}4.9 \times 10^{15} \text{ cm}^{-3}$.

The electrodes were fabricated using electron beam lithography with poly(methyl methacrylate) (PMMA) resist and ultrahigh-vacuum (UHV) electron beam evaporation. The electrodes consist of a 5-nm titanium layer for adhesion to a silicon surface and 50 nm of gold.

APPENDIX B: STRAIN SIMULATIONS

The strain in our samples was estimated by simulating the thermal expansion mismatches using COMSOL MULTIPHYSICS software. In the simulation a silicon chip rests on a copper stage and has gold electrodes on the top. We assume zero strain at room temperature and then calculate the induced strain (by both the electrodes and the stage) at low temperatures. We made custom interpolation tables for the linear thermal expansion coefficients [42–44], since at low temperatures the coefficients are considerably different compared with the room temperature case. The temperature is swept down to 3.3 K, and the strain is calculated for each temperature step. An anisotropic model and parameters were used for silicon.

The strain varies considerably as a function of depth, and an interesting problem is the question, At which depths does our signal originate? It turns out that we can answer this question by considering the inhomogeneous broadening caused by the strain and comparing that with our measured transition linewidths. This analysis shows that our signal only originates from the first couple of micrometers of the substrate; otherwise we should see a much more pronounced widening of the transition linewidths according to our model (see Supplemental Material [28] for more details). Hence, in Fig. 7, we plot all the strain components at the surface and at 1 μm depth.

We repeated the simulation also for SOI material that has a 220-nm natural Si film, 3- μm SiO_2 layer, and 750- μm Si substrate. In the simulations we suspend the area between

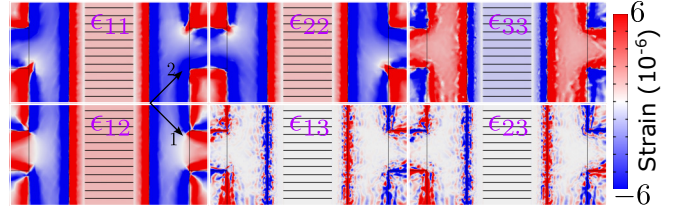


FIG. 8. Simulated strain tensor elements at 100 nm depth in the suspended 220-nm silicon film. The black arrows show the coordinate directions. The stripes between the electrodes are narrow holes that allow the release of the Si film by hydrofluoric acid (HF) etching. Note how constant the strain components are within the released area.

the electrodes, leaving a 10- μm gap between the suspension and the electrode edge. This allows the strain, created by the electrodes, to relax before the suspended silicon film starts and considerably both lessens the strain and relaxes any gradients in the suspended area as can be seen in the simulated strain components at 100 nm depth that are shown in Fig. 8.

APPENDIX C: EXTRACTING HOLE g FACTORS

The Zeeman energy splitting of a $\frac{3}{2}$ -spin hole can be calculated from [34]

$$E_{1,2} = \pm \mu_0 \left\{ \frac{\mathbf{B}^2}{8} \left[9 \left(g_1 + \frac{9}{4} g_2 \right)^2 + \left(g_1 + \frac{g_2}{4} \right)^2 \right] + \left(g_1 + \frac{7}{4} g_2 \right) \left[\left(g_1 + \frac{13}{4} g_2 \right)^2 \mathbf{B}^4 - 9 g_2 \left(g_1 + \frac{5}{2} g_2 \right) (B_x^2 B_y^2 + B_x^2 B_z^2 + B_y^2 B_z^2) \right] \right\}^{\frac{1}{2}} \quad (\text{C1})$$

and

$$E_{3,4} = \pm \mu_0 \left\{ \frac{\mathbf{B}^2}{8} \left[9 \left(g_1 + \frac{9}{4} g_2 \right)^2 + \left(g_1 + \frac{g_2}{4} \right)^2 \right] - \left(g_1 + \frac{7}{4} g_2 \right) \left[\left(g_1 + \frac{13}{4} g_2 \right)^2 \mathbf{B}^4 - 9 g_2 \left(g_1 + \frac{5}{2} g_2 \right) (B_x^2 B_y^2 + B_x^2 B_z^2 + B_y^2 B_z^2) \right] \right\}^{\frac{1}{2}} \quad (\text{C2})$$

where $E_{1,2}$ and $E_{3,4}$ give the heavy-hole and light-hole splitting energies, respectively. By setting the magnetic field direction using the notation $[xyz]$, referring to the crystal orientation, one can calculate the effective g factors along any direction. The heavy-hole and light-hole g factors that are observed at the high-field asymptote can be solved from

$$\frac{1}{2} \mu_0 g_{\text{LH}} \mathbf{B} = E_{3,4}, \quad (\text{C3})$$

$$\frac{3}{2} \mu_0 g_{\text{HH}} \mathbf{B} = E_{1,2}. \quad (\text{C4})$$

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