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Optimizing geometry of low-Q all-metal Fabry-Pérot microcavity for fluorescence spectroscopy

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Abstract

Fluorescence spectroscopy is commonly employed to study the excited-state photophysics of organic molecules. Planar Fabry-Pérot microcavities play an essential role in such studies and a strategic cavity design is necessary to attain an enhanced light-matter interaction. In this work, we computationally study different geometries for a planar metallic Fabry-Pérot microcavity tuned for the absorption of Sulforhodamine 101, a typical dye for fluorescence spectroscopy. The cavity consists of a polymer layer enclosed between two silver mirrors, where the thicknesses of all the three layers are varied to optimize the cavity. Our transfer-matrix and finite-difference time-domain simulations suggest that a cavity with 30 nm thin top mirror and 200 nm fully reflective thick bottom mirror, thus having only reflection and absorption and no transmission, is an optimal design for maximizing the Purcell factor and spectral overlap between the cavity and molecule, while still sustaining an efficient measurability of the fluorescence.

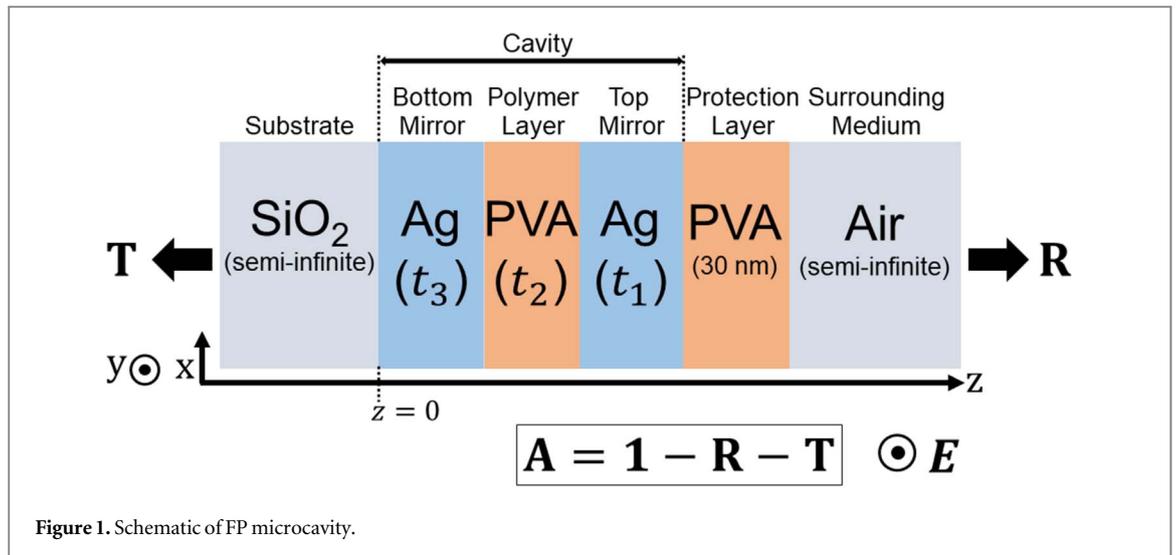
1. Introduction

Low-Q planar Fabry-Pérot (FP) microcavities, doped with photoactive organic molecules, are essential in exploring light-matter interactions under weak [1–4] and strong coupling limit [5, 6], and often employed in the studies of excited-state photochemistry [7, 8], photovoltaics [9], and cavity-quantum electrodynamics [10].

Planar metallic FP microcavities are popular in spectroscopy [3, 6] since they are simpler to fabricate and realize than dielectric cavities [11, 12]. However, implementing them in fluorescence spectroscopy is challenging, because usually one can tune the cavity resonance and thus the enhancement either for molecular absorption or emission, but not fully for both. The usual choice has been to do the excitation or detection via light leaking through a thin enough mirror, which, however, limits the quality factor (Q) of the microcavity to well below hundred. However, mode volumes (V_m) of the all-metallic microcavities are really small, which in the case of multimolecule coupling is enough to drive the system even to an ultrastrong coupling regime [13].

Performance of a FP cavity in fluorescence spectroscopy depends on its field-confinements in temporal (Q) and spatial (V_m) domains. Here $Q = \lambda_0 / \Delta\lambda$, where λ_0 is the wavelength of the cavity resonance and $\Delta\lambda$ is the full-width at half-maximum of the resonance peak [14]; and, $V_m = \left[\int \epsilon |\mathbf{E}|^2 dV \right] / [\max(\epsilon |\mathbf{E}|^2)]$, where ϵ is the dielectric function and \mathbf{E} is the electric-field amplitude inside the interaction volume V [15]. Purcell factor determines the fluorescence enhancement inside the cavity and it is $F_p = (3/4\pi^2)(\lambda_0/n)^3(Q/V_m)$, where n is the refractive index in V [16]. Increasing Q and decreasing V_m readily improves F_p . However, increasing Q often requires highly reflective mirrors, incurring a reduced cavity transmission, which further reduces the measurability of the fluorescence. Thus, an optimized compromise is needed.

In addition, the aforementioned F_p is ‘ideal’, assuming—perfect spectral overlap of the cavity mode with the fluorescence spectrum, and emitter location at the antinode of the cavity mode with its transition dipole aligned with the local electric field [17]. In reality, matching of the cavity mode of doped microcavities, with the emission spectrum of an ensemble of emitters spatially distributed within the cavity field with randomly oriented dipoles,



can be challenging [18]. Hence, only a fraction of the emission couples to the cavity leading to an effective F_p much lower than the ideal [4].

Improving the effective F_p can be done by spectral tuning between the cavity mode and the emitter responses. Increasing the spectral overlap between the molecular emission $PL(\lambda)$ and the cavity absorption $A_c(\lambda)$, i.e. emission overlap $\Phi_E = \int A_c(\lambda) \cap PL(\lambda) d\lambda$, will increase the fraction of the emission coupled to the cavity, resulting in more efficient fluorescence enhancement [19]. Similarly, excitation efficiency of the fluorescent molecules inside the cavity depends on the spectral overlap between $A_c(\lambda)$ and the molecular absorption $A_m(\lambda)$, i.e. absorption overlap $\Phi_A = \int A_c(\lambda) \cap A_m(\lambda) d\lambda$, which has to be high for an efficient cavity-molecular coupling [20].

Taking into account the above excitation efficiency ($\propto \Phi_A$) and considering that—only a fraction of the molecular emission coupled with the cavity absorption ($\propto \Phi_E$) is enhanced by a factor of F_p and collected through a cavity mirror possessing an average transmissivity T_{avg} , the total integrated fluorescence intensity measurable outside of the microcavity can be formulated as $I_{FL} = F_p T_{avg} \Phi_E \Phi_A$. I_{FL} is an estimation of the measurability of fluorescence, which is not necessarily optimal at optimal F_p . Therefore, a strategic cavity design is needed to attain an optimal F_p , Φ_E , Φ_A and T_{avg} to obtain the best I_{FL} , which we use as our main criteria for the cavity here.

In this work, we computationally study different geometries for a planar metallic FP microcavity. To calculate I_{FL} we have chosen sulforhodamine 101 (SR101) dye as our model molecule and tuned the cavities for its absorption maximum (576 nm). The cavity consists of a polymer layer enclosed between two silver mirrors, and the thicknesses of all the three layers are varied to optimize the cavity properties. Our transfer-matrix method (TMM) and finite-difference time-domain (FDTD) based simulations suggest that a reflective (non-transmitting) cavity is an optimal choice in maximizing F_p , Φ_A , Φ_E and especially I_{FL} . Our findings provide insights on designing low-Q all-metal FP microcavities for fluorescence spectroscopy.

2. Materials and methods

Planar metallic FP microcavities with different geometries were studied using TMM [21, 22] and FDTD [23, 24] simulations. The two silver (Ag) mirrors with thicknesses t_1 and t_3 , and a layer (thickness t_2) of poly-vinyl alcohol (PVA) embedded in between, form the cavity (see figure 1). PVA was chosen since it is a suitable polymer matrix for SR101 molecules. The cavity mode was always tuned to the absorption maximum of SR101 (576 nm) by varying t_2 . A thin PVA layer (30 nm) was also considered on top of the top Ag mirror as a protection layer, which prevents the oxidation of Ag in ambient condition in the case of real cavities. The glass (SiO_2) substrate and the surrounding medium (air, refractive index is 1.0) were considered as semi-infinite. The material models for Ag, PVA and SiO_2 were extracted from [25–27], respectively. The absorption and emission spectra of SR101 were taken from [28].

Reflection, transmission and absorption (R, T, A) of the modelled microcavities were calculated using TMM where $A = 1 - R - T$. The Q values were calculated from the cavity absorption. Electric field distribution and mode volume in each cavity were computed using 3D-FDTD simulations where normal incidence of linearly polarized light with polarization defined in figure 1 was considered as an excitation. The entire radiation zone of the cavity mode, as illustrated by the white dotted boundary in the field-distribution plot

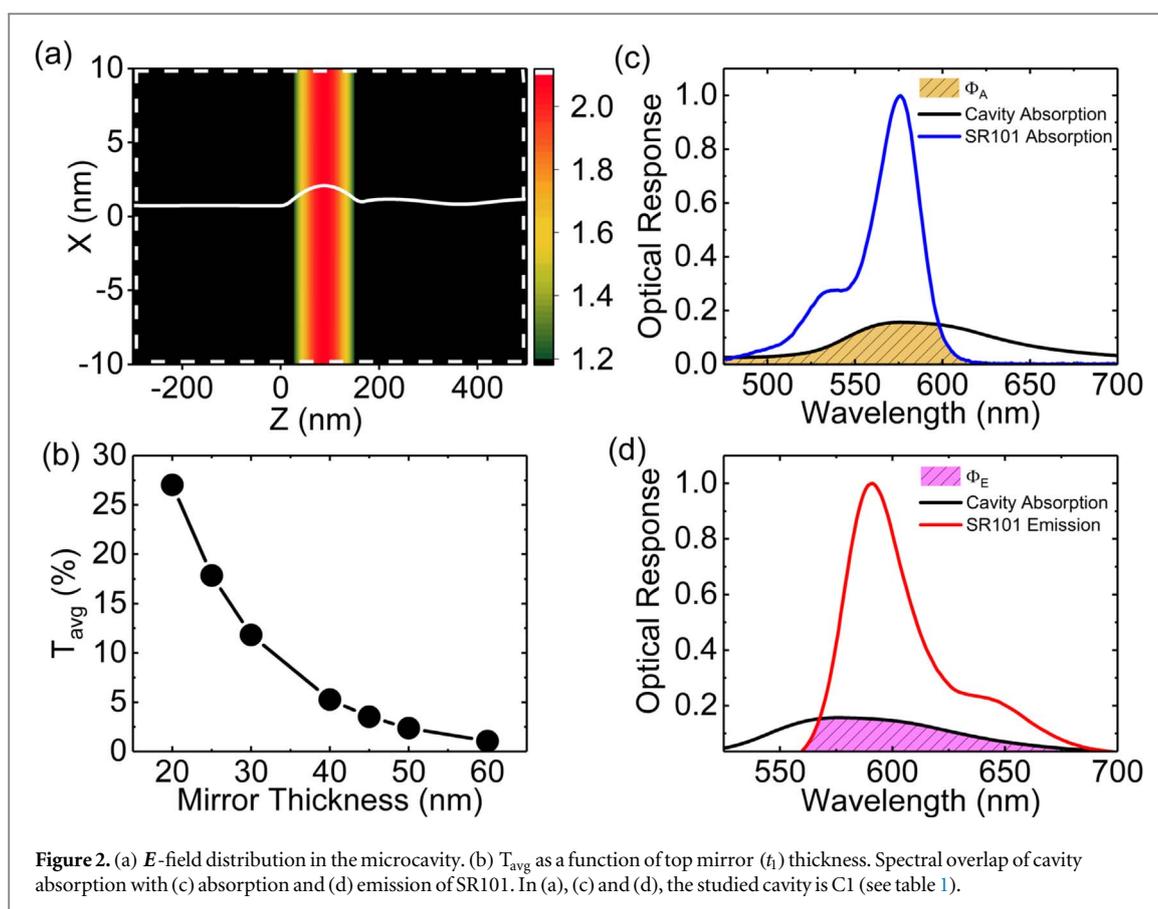


Table 1. Geometries for symmetric microcavities.

Cavity	$t_1/t_2/t_3$ (nm)
C1	20/132/20
C2	25/138/25
C3	30/142/30
C4	40/146/40
C5	50/148/50

shown in figure 2(a), was considered as V in V_m calculation. T_{avg} were calculated as the average transmission of the top mirrors (t_1) within the SR101 emission (560–700 nm) as reported in figure 2(b). Spectral overlaps (Φ_A and Φ_E) were calculated as an integral of the common area (shaded yellow/magenta regions) under the cavity absorption (black) and the molecular absorption/emission (blue/red) curves for each cavity, as shown in figures 2(c), (d).

3. Results and discussions

In our first approach, we designed symmetric cavities where both mirrors had equal thicknesses. Five cavities (C1–C5) with increasing mirror thicknesses were considered with their geometrical parameters reported in table 1, while figures 3(a)–(c) show their R, T, A analysis. From figures 3(c), (d), it is clear that an increment in cavity mirror thickness makes the cavity absorption linewidth narrower, resulting a drastic fall in Φ_A and Φ_E . However, it simultaneously improves cavity Q, V_m and F_p as shown in figures 3(e), (f). The cavity C5 (50 nm mirrors) provides highest F_p but it yields poorest spectral overlaps and T_{avg} (see figure 2(b)). Consequently, I_{FL} drops at the highest F_p .

To overcome this limitation we designed asymmetric cavities where we made one mirror thin (leaky) for fluorescence collection while keeping the other mirror thick. Five cavities (C6–C10) were considered with increasing Δt ($\Delta t = t_3/t_1$) with their geometrical parameters reported in table 2 and their R, T, A analysis shown in figures 4(a)–(c).

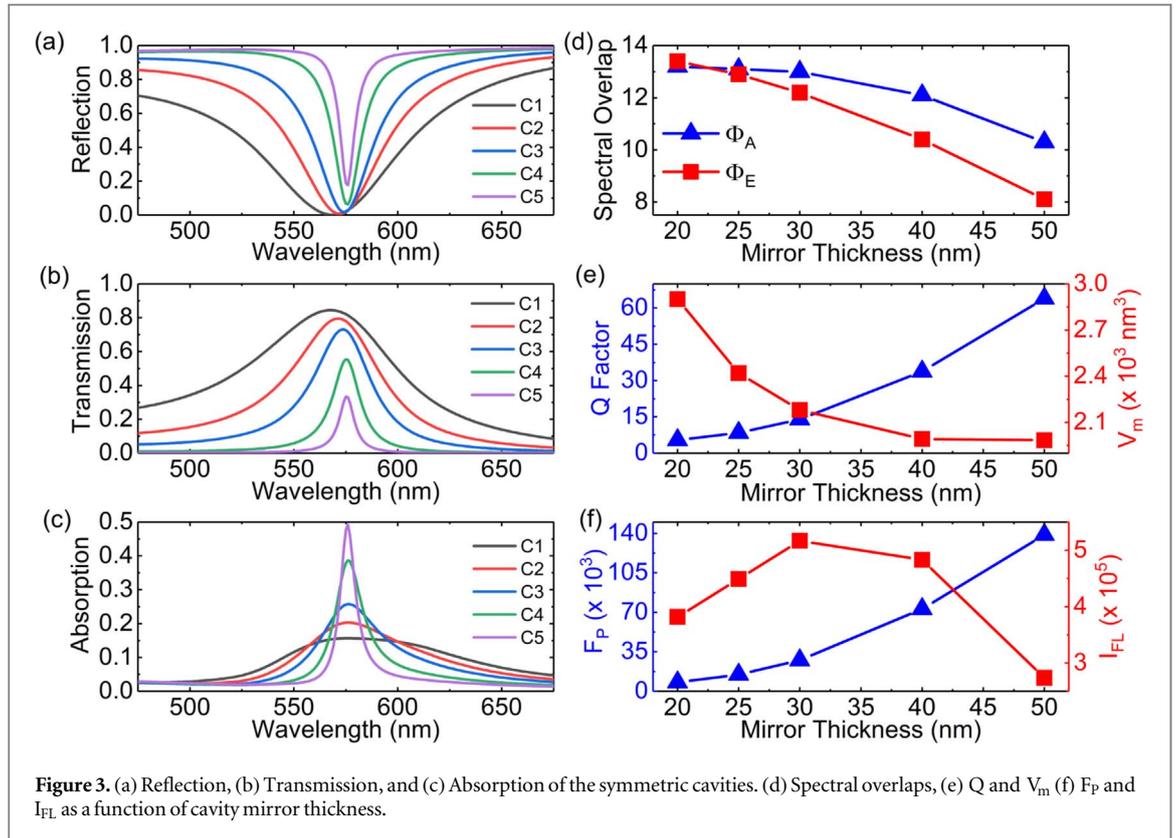


Table 2. Geometries for asymmetric microcavities.

Cavity	$t_1/t_2/t_3$ (nm)
C6	60/146/30
C7	45/145/30
C8	30/145/45
C9	30/145/60
C10	30/145/90

Figures 4(c), (d) show that the cavities with thin top and thick bottom mirrors ($\Delta t > 1$: C8-C10) yield higher cavity absorption and spectral overlaps than the cavities with thick top and leaky bottom mirrors ($\Delta t < 1$: C6-C7). An increment in Δt improves cavity Q, V_m , F_P and I_{FL} as shown in figures 4(e), (f). The cavity C10 ($\Delta t = 3$) provides highest I_{FL} , F_P , Φ_A and Φ_E . Moreover, the change in the cavity geometry from symmetric to asymmetric yields 7.54% drop in F_P with 223.33% rise in I_{FL} on average. Therefore, by making a very thick bottom mirror with a thin top mirror, one can ensure a healthy trade-off between F_P and I_{FL} .

Such findings motivated us to design a reflective (non-transmitting) cavity having a very thick bottom mirror and thin top mirror so that the cavity transmission becomes zero ($T \approx 0$) and the absorption becomes $A = 1 - R$. Five reflective cavities (C11–C15) with increasing top mirror thickness were considered while the bottom mirror thickness was kept constant. Figures 5(a), (b) present their R, A analysis with their geometries specified in table 3. Figure 5(c) depicts the leaky transmissivity of the top mirrors used for all the cavities. It was computed by considering an Ag layer between semi-infinite PVA and air. From C11 to C15, as the top mirror thickness is increased, the cavity absorption, Φ_A and Φ_E are increased with a significant drop in the transmissivity of the top mirrors, as shown in figures 5(b)–(d). However, a simultaneous improvement in cavity Q, V_m and F_P is also observed as depicted in figures 5(e), (f).

In a reflective cavity, due to the non-transmitting bottom mirror, the omnidirectional fluorescence emission can only exit through the thin top mirror. Therefore, a fall in the leaky mirror transmissivity, as shown in figure 5(c), directly results a drop in I_{FL} at highest F_P as shown in figure 5(f). Nevertheless, the change in the cavity geometry from symmetric to reflective results 98.55% rise in F_P alongwith 386.56% rise in I_{FL} on average and clearly outperformed the asymmetric cavities. Therefore, we can conclude that of the cavities studied here,

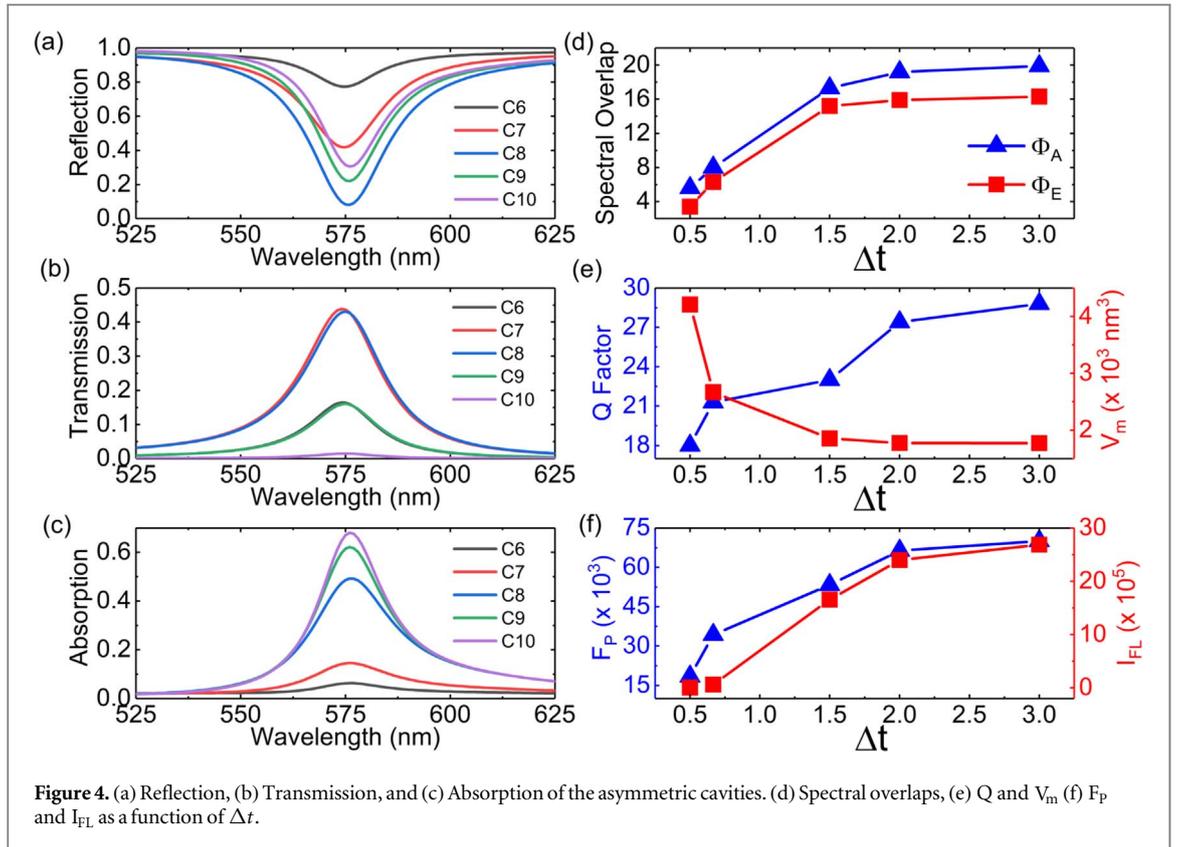


Figure 4. (a) Reflection, (b) Transmission, and (c) Absorption of the asymmetric cavities. (d) Spectral overlaps, (e) Q and V_m (f) F_P and I_{FL} as a function of Δt .

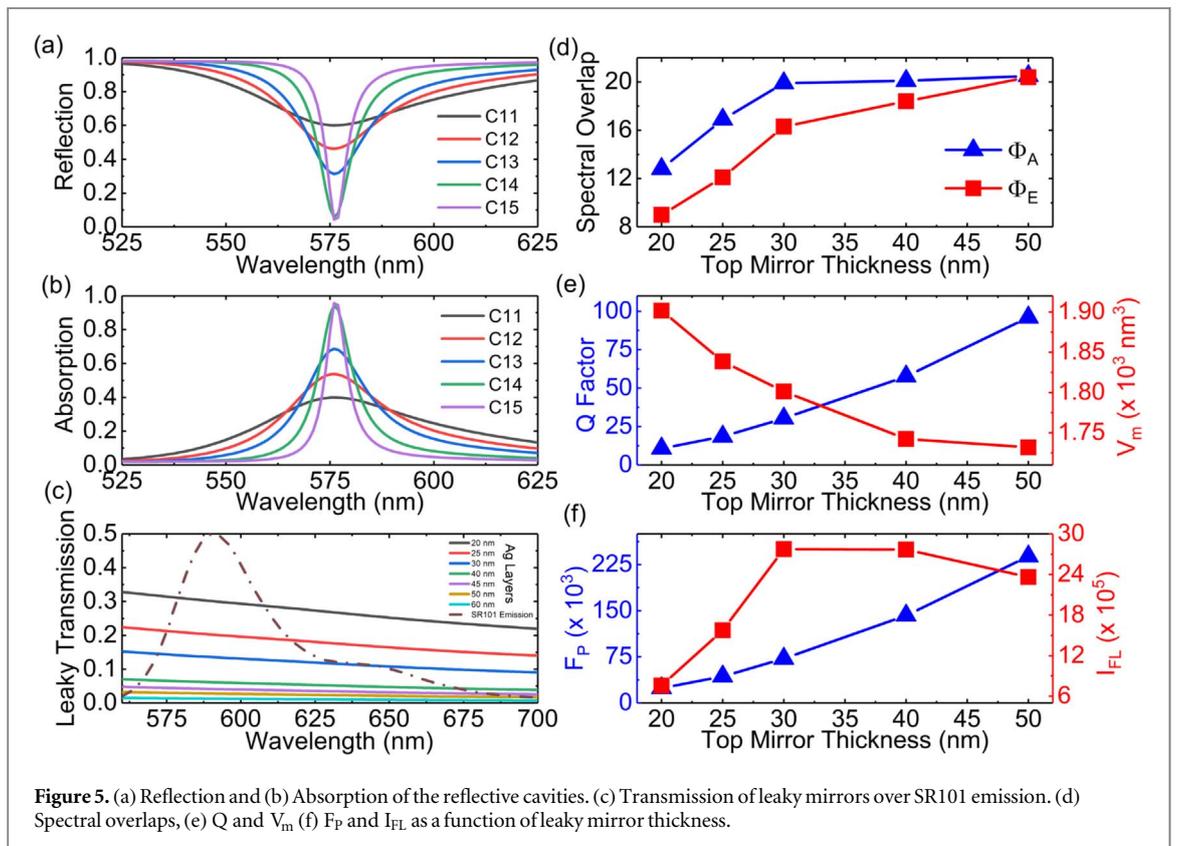


Figure 5. (a) Reflection and (b) Absorption of the reflective cavities. (c) Transmission of leaky mirrors over SR101 emission. (d) Spectral overlaps, (e) Q and V_m (f) F_P and I_{FL} as a function of leaky mirror thickness.

Table 3. Geometries for reflective microcavities.

Cavity	$t_1/t_2/t_3$ (nm)
C11	20/140/200
C12	25/143/200
C13	30/145/200
C14	40/148/200
C15	50/149/200

the reflective cavities, and more precisely C13 is the optimal choice for fluorescence spectroscopy of SR101, providing the best possible I_{FL} .

4. Conclusions

We computationally investigated different geometries of a planar metallic FP microcavity tuned for the absorption of SR101. The cavities were modelled using TMM and FDTD simulations to optimize the Purcell factor, the spectral overlap between the cavity mode and the molecular responses, and the measurability of fluorescence. To quantify the total fluorescence measurability, we defined $I_{FL} = F_P T_{avg} \Phi_E \Phi_A$, which takes into account all the above properties. However, we also analyzed the different properties separately since they can be important for other studies.

Our findings revealed that the symmetric cavities are limited in providing high Purcell enhancement along with an acceptable measurability of fluorescence. Asymmetric cavities can provide more efficient light-matter interaction while maintaining a pathway to collect the fluorescence through the leaky top mirror. Finally, we achieved an optimal design, i.e. a reflective cavity (C13) with 30 nm thin/leaky top mirror and 200 nm thick/non-transmitting bottom mirror, which provides high Purcell factor and spectral overlaps, and most importantly, the best I_{FL} for fluorescence spectroscopy of SR101.

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Data availability statement

The data that support the findings of this study are available upon reasonable request from the authors.

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References

- [1] Deppe D G and Lei C 1992 *Appl. Phys. Lett.* **60** 527–9
- [2] Pokhriyal A, Lu M, Chaudhery V, George S and Cunningham B T 2013 *Appl. Phys. Lett.* **102** 221114
- [3] Nyman M, Shevchenko A, Shavrin I, Ando Y, Lindfors K and Kaivola M 2019 *APL Photonics* **4** 076101
- [4] Kaupp H, Deutsch C, Chang H-C, Reichel J, Hänsch T W and Hunger D 2013 *Phys. Rev. A* **88** 053812
- [5] Agronovich V M and La Rocca G C 2005 *Solid State Commun.* **135** 544–53
- [6] Hobson P A, Barnes W L, Lidzey D G, Gehring G A, Whittaker D M, Skolnick M S and Walker S 2002 *Appl. Phys. Lett.* **81** 3519–21
- [7] Ribeiro R, Martinez-Martinez L, Du M, Campos-Gonzalez-Angulo J and Yuen-Zhou J 2018 *Chem. Sci.* **9** 6325–39
- [8] Sanvitto D and Kéna-Cohen S 2016 *Nat. Mater.* **15** 1061–73
- [9] Wang Y, Shen P, Liu J, Xue Y, Wang Y, Yao M and Shen L 2019 *Sol. RRL* **3** 1900181
- [10] Flick J, Ruggenthaler M, Appel H and Rubio A 2017 *Proc. Natl. Acad. Sci. USA* **114** 3026–34
- [11] Connolly L G, Lidzey D G, Butté R, Adawi A M, Whittaker D M, Skolnick M S and Airey R 2003 *Appl. Phys. Lett.* **83** 5377–9
- [12] Wang Z, Gogna R and Deng H 2017 *Appl. Phys. Lett.* **111** 061102
- [13] Suzuki M, Nishiyama K, Kani N, Yu X, Uzumi K, Funahashi M, Shimokawa F, Nakanishi S and Tsurumachi N 2019 *Appl. Phys. Lett.* **114** 191108
- [14] Bitarafan M H and DeCorby R G 2017 *Sensors* **17** 1748
- [15] Hu S, Khater M, Salas-Montiel R, Kratschmer E, Engelmann S, Green W M J and Weiss S M 2018 *Sci. Adv.* **4** eaat2355
- [16] Vahala K 2003 *Nature* **424** 839–46

- [17] Gerard J-M and Gayral B 1999 *J. Light. Technol.* **17** 2089–95
- [18] Gu Q and Fainman Y 2017 *Semiconductor Nanolasers* (Cambridge: Cambridge University Press)
- [19] Herrera F and Spano F C 2017 *Phys. Rev. A* **95** 053867
- [20] Groenhof G, Climent C, Feist J, Morozov D and Toppari J J 2019 *J. Phys. Chem. Lett.* **10** 5476–83
- [21] Mackay T G and Lakhtakia A 2020 *The Transfer-Matrix Method in Electromagnetics and Optics* (San Rafael: Morgan & Claypool Publishers)
- [22] Pascoe K J 2001 *Reflectivity and Transmissivity through Layered, Lossy Media: A User-Friendly Approach* (Ohio: Wright Patterson Air Force Base)
- [23] Gedney S 2011 *Introduction to the Finite-Difference Time-Domain (FDTD) Method for Electromagnetics* (San Rafael: Morgan & Claypool Publishers)
- [24] ANSYS Lumerical FDTD Solutions R2.4 2020
- [25] Johnson P and Christy R 1972 *Phys. Rev. B* **6** 4370–9
- [26] Schnepf M J *et al* 2017 *Nanoscale* **9** 9376–85
- [27] Palik E D 1997 *Handbook of Optical Constants of Solids* (Burlington: Academic)
- [28] Birge R R and Duarte F J 1990 *Kodak Optical Products* (Rochester: Kodak Publication)