Effects of triplet Higgs bosons in long baseline neutrino experiments

K. Huitu and T. J. Kärkäinen
Department of Physics, and Helsinki Institute of Physics, P. O. Box 64, FI-00014 University of Helsinki, Finland

J. Maalampi and S. Vihonen
University of Jyväskyla, Department of Physics, P. O. Box 35, FI-40014 University of Jyväskyla, Finland

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The triplet scalars \((\Delta = \Delta^{++}, \Delta^+, \Delta^0)\) utilized in the so-called type-II seesaw model to explain the lightness of neutrinos, would generate nonstandard interactions (NSI) for a neutrino propagating in matter. We investigate the prospects to probe these interactions in long baseline neutrino oscillation experiments. We analyze the upper bounds that the proposed DUNE experiment might set on the nonstandard parameters and numerically derive upper bounds, as a function of the lightest neutrino mass, on the ratio \(M_\Delta\) of the triplet scalars, and the strength \(|\lambda_\phi|\) of the coupling \(\phi\phi\Delta\) of the triplet \(\Delta\) and conventional Higgs doublet \(\phi\). We also discuss the possible misinterpretation of these effects as effects arising from a nonunitarity of the neutrino mixing matrix and compare the results with the bounds that arise from the charged lepton flavor violating processes.

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I. INTRODUCTION

The discovery of neutrino oscillations in atmospheric and solar neutrino measurements [1,2] proved that the SU(2)\(_L\) \(\times\) U(1)\(_Y\) Standard Model (SM) is not capable to fully explain the particle physics world. The existence of oscillations indicates that neutrinos are massive particles, in contrast with the prediction of the SM. One has to go beyond the SM in order to discover the origin of neutrino masses. At the same time, one has to find a convincing explanation for the lightness of neutrinos as compared with the other basic particles, i.e., quarks and charged leptons. The most popular answer to the latter question is the so-called seesaw mechanism [3–7], where the suppression of neutrino masses follows from the existence of a new mass scale much higher than the electroweak scale \(O(10^2)\) GeV. In the type-I seesaw mechanism, the new mass scale is set by sterile right-handed neutrinos by which the particle content of the SM is extended. The type-II seesaw mechanism is based on the existence of a set of new scalars \(\Delta = (\Delta^{++}, \Delta^+, \Delta^0)\) transforming as a triplet under the SU(2)\(_L\) gauge symmetry. The masses of neutrinos are proportional to the ratio \(\lambda_\phi v^2/M_\Delta^2\), where \(v \approx 174\) GeV is the vacuum expectation value of the SM Higgs field \(\phi\), \(M_\Delta\) is the mass of triplet scalar, and \(\lambda_\phi\) is the dimensionful strength of the \(\phi\phi\Delta\) coupling.

While the seesaw mechanism itself cannot be experimentally verified, the extension of the SM is based on generally leads to experimentally testable phenomena. For example, the doubly charged scalar \(\Delta^{++}\) would have clear experimental signatures, e.g., in high-energy proton-proton collision experiments [8–13]. One theoretical framework where a scalar triplet, as well as right-handed neutrinos, naturally appear is the left-right symmetric electroweak model based on the gauge symmetry SU(3)\(_C\) \(\times\) SU(2)\(_L\) \(\times\) SU(2)\(_R\) \(\times\) U(1)\(_{B-L}\) [14–18].

In this paper, we will concentrate on the type-II seesaw mechanism and investigate how the triplet scalar bosons \(\Delta\) would affect neutrino propagation in matter (for earlier studies, see, e.g., [19]) and how these effects could be probed in long baseline neutrino experiments, particularly in the planned DUNE. Applying the bounds derived for DUNE in Ref. [20], together with the constraints one has for the elements of the neutrino mass matrix from earlier oscillation experiments, we compute an upper limit of the ratio \(M_\Delta/|\lambda_\phi|\) as a function of the absolute neutrino mass scale (the mass \(m_1\) of the lightest neutrino). For comparison, we also compute the upper bound for this ratio using the existing constraints on the charged lepton flavor violation (CLFV) processes.

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II. NONSTANDARD INTERACTIONS AND NEUTRINO MASSES IN A TRIPLET MODEL

Our theoretical framework is the SU(2)_L × U(1)_Y electroweak model added with a scalar triplet field Δ = (Δ_1, Δ_2, Δ_3) ~ (3, 2), which can also be understood as a low-energy effective theory of the left-right symmetric SU(3)_C × SU(2)_L × SU(2)_R × U(1)_{B−L} theory, where all the other nonstandard degrees of freedom except the triplet scalar are so heavy that they do not have observable effects in the oscillation experiments. The interactions of the triplet Δ relevant for the neutrino oscillation are described with the following Lagrangian:

\[ \mathcal{L}_\Delta = Y_{\alpha\beta} L^T C_i \sigma_2 \Delta L_{\rho L} + \lambda_\phi \phi^\dagger i \sigma_2 \Delta^\dagger \phi + \text{H.c.}, \]  

(1)

where \( Y_{\alpha\beta} (\alpha, \beta = e, \mu, \tau) \) are Yukawa coupling constants, \( C \) is the charge conjugation operator, \( \phi \) is the SM Higgs doublet, and the triplet \( \Delta \) is presented in the 2 × 2 matrix form

\[ \Delta = \frac{1}{\sqrt{2}} \sigma_1 \Delta_1 = \begin{pmatrix} \Delta^+ \\
\Delta^0 \\
\Delta^+ 
\end{pmatrix}, \]

(2)

where \( \sigma_i \) are the Pauli matrices. When written in terms of component fields, Eq. (1) takes the form

\[ \mathcal{L}_Y = Y_{\alpha\beta} \left[ \Delta^0 \bar{\nu}_{\alpha R} \nu_{\beta L} - \frac{1}{\sqrt{2}} \Delta^+ (\bar{\nu}_{\alpha R} \nu_{\beta L} + \nu_{\alpha R} \bar{\nu}_{\beta L}) - \Delta^{++} \bar{\nu}_{\alpha R} \nu_{\beta L} \right] + \text{H.c.} \]  

(3)

These interactions lead in the second order of perturbation theory to the four-fermion interactions presented in the Fig. 1. The amplitude presented in Fig. 1(a) gives rise to Majorana mass terms for the neutrinos when the SU(2)_L × U(1)_Y symmetry is spontaneously broken, while the amplitudes in Figs. 1(b) and 1(c) correspond to new, nonstandard interactions among leptons. In the limit, where the mass of the triplet scalars \( M_\Delta \), assumed to be the same for all members of the triplet, is large compared with the momenta of the processes, the amplitudes are described by the following effective Lagrangians [19]:

\[ \mathcal{L}^{\text{eff}}_\nu = \frac{Y_{\alpha\beta} \lambda_\phi v^2}{M_\Delta} (\bar{\nu}_{\alpha R} \nu_{\beta L}) = -\frac{1}{2} (m_\nu)_{\alpha\beta} \bar{\nu}_{\alpha R} \nu_{\beta L}, \]  

(4)

\[ \mathcal{L}_{\text{NSI}} = \frac{Y_{\alpha\beta} Y_{\alpha\beta}^*}{M_\Delta} (\bar{\nu}_{\alpha L} \nu_{\beta L}) (\bar{\nu}_{\beta L} \nu_{\alpha L}), \]

(5)

where \( m_\nu \) is the neutrino mass matrix, \( M_\Delta \) is the degenerate mass of the \( \Delta \) particles, and \( v \) is the vacuum expectation value of the SM scalar Higgs field. The connection to the effective field theory can be derived by solving the Yukawa coupling \( Y_{\alpha\beta} \) from the Majorana mass term in Eq. (4) and inserting it to the neutrino matter NSI term in Eq. (5).

Comparing the result with the effective NSI Lagrangian

\[ \mathcal{L}_{\text{NSI}} = -2\sqrt{2} G_F Y_{\alpha\beta}^* (\bar{\nu}_{\alpha L} \nu_{\beta L}) (\bar{\nu}_{\beta L} \nu_{\alpha L}), \]  

(6)

where \( P_C \) is chiral projection operator (\( C = L, R \)), \( G_F \) is Fermi coupling constant, \( f, f' \) are any fermions, \( \alpha, \beta = e, \mu, \tau \), and allowing only left-handed lepton terms (since \( \Delta \) is leptophilic), one obtains the following expression for the nonstandard interaction parameters:

\[ \mathcal{L}_{\text{NSI}} = -2\sqrt{2} G_F Y_{\alpha\beta}^* (\bar{\nu}_{\alpha L} \nu_{\beta L}) (\bar{\nu}_{\beta L} \nu_{\alpha L}). \]  

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where $\alpha, \beta, \rho,$ and $\sigma$ are flavor indices. The expression (7) indicates the larger the ratio $M^2_\Delta/\lambda^2_{\phi}$, the stronger are the nonstandard interactions of light neutrinos. Conversely, stricter bounds on $\epsilon^{\sigma}_{\alpha\beta}$ also mean better constraints on $M^2_\Delta/\lambda^2_{\phi}$.

### III. NONSTANDARD INTERACTIONS AND NONUNITARY MIXING

In the context of long baseline experiments, neutrino oscillations are strongly influenced by matter effects, arising from the charged current (CC) and neutral current (NC) weak interactions of neutrinos with the medium they traverse. In the case of the SM, these interactions take place via an exchange of $W$ and $Z$ bosons. In the framework of our model, the matter effects are also contributed by the charged current interactions mediated by the scalar $\Delta$.

In the low energy limit, nonstandard interactions stem from the effective CC- and NC-like Lagrangians, which are given by (21),

$$L^{C/C}_{\text{NSI}} = -2\sqrt{2}G_F f^f_C \nu_\mu (\bar{\nu}_\mu P C f).$$

The CC Lagrangian $L^{C/C}_{\text{NSI}}$ in Eq. (8) is responsible for the NSI effects involved in the neutrino source and detector. The NC Lagrangian $L^{C/C}_{\text{NSI}}$, on the other hand, is relevant for neutrino propagation in matter. In the context of a triplet model, CC interactions arise from Fig. 1(b) at the low energy limit, when $f \neq f'$. The CC Lagrangian, where $f = f'$ is generated also, but such a case corresponds to a NC Lagrangian, and by definition $f^f_C \equiv f^{f'}_C$.

Most of the charged current NSI parameters have been studied comprehensively in lepton decay experiments resulting in strict constraints. The current bounds on the CC NSI parameters $\epsilon^{f^f}_\alpha$, as quoted in Ref. [19], are presented in Table I.

In the future long baseline experiments, the NSI effects become particularly relevant in the neutrino propagation in matter, where they are covered by the effective NC Lagrangian $L^{C/C}_{\text{NSI}}$. For previous studies, see [20,23–36]. The effective Hamiltonian takes the form

$$H = \frac{1}{2E_\nu} [U \text{diag}(m^2_1, m^2_2, m^2_3) U^\dagger + \text{diag}(A, 0, 0) + \Delta H],$$

where $E_\nu$ is the energy of the propagating neutrino, $U$ is the light neutrino mixing matrix, and $m_1$, $m_2$, and $m_3$ are the three masses of the active neutrinos.

### TABLE I. Constraints on the parameters $\epsilon^{\sigma}_{\alpha\beta}$ (updated from [19]) using [21] from the $\ell^\pm \to \ell^\pm \ell^\pm$, one-loop $\ell^\pm \to \ell^\pm \gamma$, and $\mu^\pm \to \mu^\pm e^\mp$ processes. All bounds are given at 90% confidence level.

<table>
<thead>
<tr>
<th>Decay</th>
<th>Constraint on</th>
<th>Bound</th>
</tr>
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<tbody>
<tr>
<td>$\mu^- \to e^- e^+ e^-$</td>
<td>$</td>
<td>\epsilon^{e}_{\mu\mu}</td>
</tr>
<tr>
<td>$\tau^- \to e^- e^+ e^-$</td>
<td>$</td>
<td>\epsilon^{e}_{\tau\mu}</td>
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<tr>
<td>$\tau^- \to \mu^- \mu^+ \mu^-$</td>
<td>$</td>
<td>\epsilon^{\mu}_{\tau\mu}</td>
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<tr>
<td>$\tau^- \to \mu^- \mu^+ e^-$</td>
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<td>\epsilon^{e}_{\tau\mu}</td>
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<tr>
<td>$\tau^- \to \mu^- \mu^+ \mu^-$</td>
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<td>\epsilon^{\mu}_{\tau\mu}</td>
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<tr>
<td>$\tau^- \to e^- e^+ \mu^-$</td>
<td>$</td>
<td>\epsilon^{\mu}_{\tau\mu}</td>
</tr>
<tr>
<td>$\tau^- \to e^- e^+ \mu^-$</td>
<td>$</td>
<td>\epsilon^{e}_{\tau\mu}</td>
</tr>
<tr>
<td>$\mu^+ e^- \to \mu^+ e^+$</td>
<td>$</td>
<td>\epsilon^{\mu}_{\mu\mu}</td>
</tr>
</tbody>
</table>

In this formalism, the so-called matter NSI effects are parametrized as

$$\epsilon^{m}_{\alpha\beta} = \sum_{f, C} f^{f}_C \frac{N_f}{N_e},$$

where $\epsilon^{f,C}_{\alpha\beta}$ are the NSI parameters from the low energy NC Lagrangian of Eq. (8) and $N_f/N_e$ is the fraction of fermions of flavor $f$ over electrons in the medium the neutrino traverses.

The effective matter potential is given by the matrix

$$V = A \left( \begin{array}{cccc} \pm 1 + \epsilon^{ee}_{m} & \epsilon^{e\mu}_{m} & \epsilon^{e\tau}_{m} \\ \epsilon^{e\mu}_{m} & \epsilon^{ee}_{m} & \epsilon^{e\tau}_{m} \\ \epsilon^{e\tau}_{m} & \epsilon^{e\mu}_{m} & \epsilon^{ee}_{m} \end{array} \right),$$

where $A = \sqrt{2}G_F N_e$, $G_F$ is the Fermi coupling constant and $N_e$ is the electron number density of the medium. Positive (negative) sign in (1,1) element of the matrix corresponds to matter potential for (anti)neutrinos. In this work, we consider only the former case. The matter NSI effects are incorporated in the SM matter effects via parameters $\epsilon^{m}_{\alpha\beta}$, $\alpha, \beta = e, \mu, \tau$. The effective Hamiltonian can therefore be written as

$$H = \frac{1}{2E_\nu} \left[ U \left( \begin{array}{ccc} 0 & 0 & 0 \\ 0 & \Delta m^2_{21} & 0 \\ 0 & 0 & \Delta m^2_{31} \end{array} \right) U^\dagger + V \right],$$

and the probability for the transition $\nu_\alpha \to \nu_\beta$ is given by

$$P_{\nu_\alpha \to \nu_\beta} = |\langle \nu_\beta | e^{-i\hat{H}t} | \nu_\alpha \rangle|^2$$,

where $|\nu_\alpha \rangle \equiv |\nu_\alpha \rangle + \epsilon^{\alpha}_{m}|\nu_\beta \rangle$ and $|\nu_\beta \rangle \equiv |\nu_\beta \rangle + \epsilon^{\beta}_{m}|\nu_\alpha \rangle$ refer to a neutrino that starts in the flavor $\alpha$ in the source and is
detected in the flavor $\beta$ in the detector after the traversing distance $L$. In long baseline experiments $L$ is set by the baseline of the experiment and $E_\nu$ by the energy of the neutrino beam. The matrices $e^i$ and $e^d$ contain dimensionless elements, which slightly alter the neutrino production and detection interactions in the source and detector, respectively. They originate from CC NSI parameters $\epsilon_{ab}^{ij, c}$ in Eq. (8), and their current experimental bounds are reported in Ref. [20].

It is possible that a part of the experimental signal presumed to originate from the matter NSI effects is actually caused by the nonunitarity of the light neutrino mixing matrix (see, e.g., [37,38]). We shall evaluate in our numerical analysis how large this contribution could possibly be in the triplet model, Eq. (1). In the case of nonunitarity, the light neutrino mixing matrix $U$ in Eq. (12) must be replaced with a nonunitary matrix, which we denote by $N$. The matrix $N$ can be parametrized as $N = N^{NP}U$, where the nonunitarity is contained in a specific $3 \times 3$ triangle matrix [24]

$$N^{NP} = \begin{pmatrix} 1 - \alpha_{ee} & 0 & 0 \\ -\alpha_{e\mu} & 1 - \alpha_{\mu\mu} & 0 \\ -\alpha_{e\tau} & -\alpha_{\mu\tau} & 1 - \alpha_{\tau\tau} \end{pmatrix}, \quad (14)$$

where $\alpha_{\ell\ell'} \ll 1, \ell, \ell' = e, \mu, \tau$. The current experimental bounds on nonunitarity parameters $\alpha_{\ell\ell'}$ are presented in Table II.¹

In the leading order, the matter NSI and nonunitarity parametrizations can be related through the equations [24],

$$\begin{align*}
\epsilon_{ee}^m &= -\alpha_{ee}, \\
\epsilon_{\mu\mu}^m &= \alpha_{\mu\mu}, \\
\epsilon_{\tau\tau}^m &= \alpha_{\tau\tau}, \\
\epsilon_{e\mu}^m &= \frac{1}{2} \alpha_{e\mu}^*, \\
\epsilon_{e\tau}^m &= \frac{1}{2} \alpha_{e\tau}^*, \\
\epsilon_{\mu\tau}^m &= \frac{1}{2} \alpha_{\mu\tau}^*,
\end{align*} \quad (15)$$

where $\alpha_{\ell\ell'}, \epsilon_{\ell\ell'}^m \ll 1$ for $\ell, \ell' = e, \mu, \tau$. One should note that the two low energy parametrizations are not equivalent, and Eq. (15) is only relevant in the context of neutrino oscillations at long baselines.

### IV. NUMERICAL STUDIES

We shall study what information DUNE could provide us on the parameters $M_\Delta$ and $\lambda_\phi$ through probing the NSI effects on neutrino propagation. Since $\Delta$ is leptonphobic, only electron-type matter participates in the NSI effects related to triplet Higgs bosons. In what follows, we will use the notation $\epsilon_{ab}^{m*} \equiv \epsilon_{ab}^\ell \lambda_{\phi}^{*}$. First, we remark that there are limits for both the individual NSI parameters and for their differences

$$\epsilon_{ab}^{m*} - \epsilon_{ab}^{m*} = \frac{M_\Delta^2}{8\sqrt{2} G_F v^4 \lambda_\phi^2} \left( (m_\nu)_{ab} (m_\nu)^*_{ab} - (m_\nu)_{a'b'} (m_\nu)^*_{a'b'} \right). \quad (16)$$

To continue, we consider only matter NSI and rewrite Eqs. (7) and (16) in the following forms:

$$\begin{align*}
M_\Delta^2 \lambda_\phi^2 &= -\frac{8\sqrt{2} G_F v^4 \epsilon_{ab}^{m}}{(m_\nu)_{ab} (m_\nu)^*_{ae} - (m_\nu)_{a'b'} (m_\nu)^*_{a'e}}, \\
M_\Delta^2 \lambda_\phi^2 &= -\frac{8\sqrt{2} G_F v^4 \epsilon_{ab}^{m* - m}}{(m_\nu)_{ab} (m_\nu)^*_{ae} - (m_\nu)_{a'b'} (m_\nu)^*_{a'e}}.
\end{align*} \quad (18)$$

From this expression, it is apparent that the upper limits for $|\epsilon_{ab}^{m}|$ and $|\epsilon_{ab}^{m* - m}|$ translate to upper limits of $M_\Delta^2 / \lambda_\phi^2$. The elements of the light neutrino mass matrix $m_\nu$ are obtained from the equation

$$\begin{align*}
(m_\nu)^2 &= U \begin{pmatrix} m_1^2 & 0 & 0 \\ 0 & m_2^2 & 0 \\ 0 & 0 & m_3^2 \end{pmatrix} U^\dagger \\
+ A \begin{pmatrix} 1 + \epsilon_{ee}^m & \epsilon_{e\mu}^m & \epsilon_{e\tau}^m \\ \epsilon_{e\mu}^m & 0 & \epsilon_{\mu\tau}^m \\ \epsilon_{e\tau}^m & \epsilon_{\mu\tau}^m & 0 \end{pmatrix}.
\end{align*} \quad (19)$$

Note that compared to Eq. (11), we have shifted the $e_{\mu\mu}^m$ element, akin to [20]. Next, we define a dimensionless quantity,

$$C_{ab}^\alpha \equiv \begin{cases} 
-8\sqrt{2} G_F v^4 \epsilon_{ab}^{m*} \\
\frac{(m_\nu)_{ab} (m_\nu)^*_{ae}}{(m_\nu)_{a'b'} (m_\nu)^*_{a'e}}, \quad \alpha \neq \beta, \\
-8\sqrt{2} G_F v^4 \epsilon_{ab}^{m} \\
\frac{(m_\nu)_{ab} (m_\nu)^*_{ae} - (m_\nu)_{a'b'} (m_\nu)^*_{a'e}}, \quad \alpha = \beta.
\end{cases} \quad (20)$$

This allows us to present the limits in a compact form.

### TABLE II

Current experimental limits of the nonunitarity of the light neutrino mixing matrix [38]. All limits are given at a 90% C.L.

<table>
<thead>
<tr>
<th>Constraint on</th>
<th>Current bound</th>
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<td>$\alpha_{ee}$</td>
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<tr>
<td>$\alpha_{\mu\mu}$</td>
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</tr>
<tr>
<td>$\alpha_{\tau\tau}$</td>
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</tr>
<tr>
<td>$</td>
<td>\alpha_{ee}</td>
</tr>
<tr>
<td>$</td>
<td>\alpha_{e\mu}</td>
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<td>$</td>
<td>\alpha_{e\tau}</td>
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</table>

¹The bounds reported in Table II are based on the neutrino oscillation data from CHORUS, NOMAD, and NuTeV to constrain the nonunitarity parameters. See, e.g., Ref. [39] for a detailed discussion on tighter bounds based on precision measurements of several SM observables.
Using Eq. (19), we maximize the denominators within their experimental bounds. In long baseline neutrino experiments, the electron number density $n_e$ depends on the matter density $\rho$, which is approximately 2700 kg/m$^3$. We take the average beam energy in DUNE to be $E_\nu \approx 2$ GeV. Assuming the normal neutrino mass hierarchy, the active neutrino masses $m_2$ and $m_3$ are given by $m_2 = \sqrt{m_1^2 + \Delta m_{31}^2}$ and $m_3 = \sqrt{m_1^2 + \Delta m_{31}^2}$, where $m_1 = 0\ldots0.2$ eV, $\Delta m_{31}^2 = 7.50^{+0.14}_{-0.13} \times 10^{-5}$ eV$^2$, and $\Delta m_{31}^2 = 2.524^{+0.039}_{-0.040} \times 10^{-3}$ eV$^2$ (for inverted hierarchy $\Delta m_{32}^2 = -2.514^{+0.038}_{-0.041} \times 10^{-3}$ eV$^2$). The standard oscillation parameters are varied within their 90% confidence level (C.L.) error limits (see [20] for the projected DUNE limits) to obtain the upper limits of the denominators of $C_{\alpha \beta}$. We then take the DUNE 90% C.L. upper bounds for the $e_{\alpha \beta}$ parameters and their differences, and insert the largest possible value of the denominator and the upper limit of $e_{\alpha \beta}$ into Eq. (17). This procedure is repeated for the current experimental 90% C.L. upper bounds for matter NSI. The current experimental bounds and the simulated DUNE bounds of these parameters are given in Table III. Comparing these bounds will elucidate the performance and feasibility of DUNE as a probe for the triplet Higgs model.

We calculated the expected upper bounds $|C_{ee}|$, $|C_{e\mu}|$, $|C_{e\tau}|$, $|C_{\mu\tau}|$, $|C_{\mu\mu}|$, and $|C_{\tau\tau}|$, for $M_\Delta^2/\lambda^2_\phi$ as function of $m_1$ using the 90% C.L. upper bounds for $|e_{ee}^m - e_{\mu\mu}^m|$, $|e_{e\mu}^m|$, $|e_{\mu\tau}^m|$, and $|e_{\tau\mu}^m - e_{\mu\tau}^m|$, respectively. Thus, we obtain five $M_\Delta^2/\lambda^2_\phi$ curves as a function of $m_1$ and construct the strictest possible upper limit for $M_\Delta^2/\lambda^2_\phi$, namely $C_{\text{min}}(m_1) \equiv \min(C_{ee}, C_{e\mu}, C_{e\tau}, C_{\mu\tau}, C_{\tau\tau})$. We present this piecewise combined curve in Fig. 2, which was found to be

$$C_{\text{min}}^{\text{NH}}(m_1) = \begin{cases} C_{e\tau}, & m_1 \gtrless 0.01 \text{ eV}, \\ C_{e\mu}, & m_1 \gtrless 0.01 \text{ eV} \end{cases}$$

\[\frac{M_\Delta^2}{\lambda^2_\phi} \leq C_{\alpha \beta} \]  

(21)

Considering the scales for $G_F$, $r$, and neutrino masses, we expect $C_{\alpha \beta} \gg 1$ and $\lambda_\phi \ll M_\Delta$.

The upper bounds for $M_\Delta/\lambda_\phi$ are calculated as follows. Using Eq. (19), we maximize the denominators in Eq. (20) by varying all relevant oscillation parameters within their experimental bounds. In long baseline neutrino experiments, the electron number density $n_e$ depends on the matter density $\rho$, which is approximately 2700 kg/m$^3$. We take the average beam energy in DUNE to be $E_\nu \approx 2$ GeV. Assuming the normal neutrino mass hierarchy, the active neutrino masses $m_2$ and $m_3$ are given by $m_2 = \sqrt{m_1^2 + \Delta m_{31}^2}$ and $m_3 = \sqrt{m_1^2 + \Delta m_{31}^2}$, where $m_1 = 0\ldots0.2$ eV, $\Delta m_{31}^2 = 7.50^{+0.14}_{-0.13} \times 10^{-5}$ eV$^2$, and $\Delta m_{31}^2 = 2.524^{+0.039}_{-0.040} \times 10^{-3}$ eV$^2$ (for inverted hierarchy $\Delta m_{32}^2 = -2.514^{+0.038}_{-0.041} \times 10^{-3}$ eV$^2$). The standard oscillation parameters are varied within their 90% confidence level (C.L.) error limits (see [20] for the projected DUNE limits) to obtain the upper limits of the denominators of $C_{\alpha \beta}$. We then take the DUNE 90% C.L. upper bounds for the $e_{\alpha \beta}$ parameters and their differences, and insert the largest possible value of the denominator and the upper limit of $e_{\alpha \beta}$ into Eq. (17). This procedure is repeated for the current experimental 90% C.L. upper bounds for matter NSI. The current experimental bounds and the simulated DUNE bounds of these parameters are given in Table III. Comparing these bounds will elucidate the performance and feasibility of DUNE as a probe for the triplet Higgs model.

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$$C_{\text{min}}^{\text{NH}}(m_1) = \begin{cases} C_{e\tau}, & m_1 \gtrless 0.01 \text{ eV}, \\ C_{e\mu}, & m_1 \gtrless 0.01 \text{ eV} \end{cases}$$

(22)
\[
C_{\text{min}}^{\text{IH}}(m_3) = \begin{cases} 
C_{\mu\tau}, & m_3 \lesssim 0.04 \text{ eV}, \\
C_{e\mu}, & m_3 \gtrsim 0.04 \text{ eV}.
\end{cases}
\] (23)

As was pointed out, the nonunitarity effects could be mistaken as matter NSI effects. To estimate how large a part these could constitute of the signal, we transpose the current experimental bounds for the nonunitarity parameters \(\alpha_{ll}\) given in Table II into bounds for the NSI parameters \(e^{\mu\phi}\) using the relations given in Eq. (15). From these bounds, we obtained the 90\% C.L. bound for \(M_\Delta/|\lambda_\phi|\) shown in Fig. 2.

Similarly, we derive the upper bounds for \(M_\Delta/|\lambda_\phi|\) using the CLFV bounds from Table I. The resulting curve for 90\% C.L. upper bound for \(M_\Delta/|\lambda_\phi|\) is shown in Fig. 3. One

FIG. 4. The allowed values of \(M_\Delta\) and \(\lambda_\phi\) in \((M_\Delta, \lambda_\phi)\) plane, considering both mass hierarchies and different masses for the lightest neutrino. The colors are chosen as in Fig. 2.
immediately notes that the CLFV constraints are much stricter than the bounds we obtained from the matter NSI presented in Fig. 2.

In addition, we present $\lambda_\phi$ as a function of $M_\Delta$ with the constant lightest neutrino mass. We solve (17) for $\lambda_\phi$ and determine the allowed parameter space in $(M_\Delta, \lambda_\phi)$ plane using the aforementioned bounds for matter NSI parameters, considering only bounds arising from current and future long baseline neutrino oscillation experiments. The bounds translate to the conditions

\[ \lambda_\phi \geq \frac{M_\Delta}{\sqrt{|C_{\alpha \beta}|}}, \]

where we again consider the bounds given by $|C_{ee}|$, $|C_{\mu \mu}|$, $|C_{\tau \tau}|$, $|C_{e \mu}|$, and $|C_{e \tau}|$. We pick the tightest constraint, given by $C_{\min}$ from Eqs. (22), and (23). The 90% C.L. bound is presented in Fig. 4.

Since there are known lower limits for $M_\Delta$ [40], we may use this information to calculate an experimental lower limit for $\lambda_\phi$. This is done by calculating $|e_{\alpha \beta}^m - e_{\alpha \beta}^p|$, $|e_{\alpha \beta}^m|$, and $|e_{\alpha \beta}^m - e_{\alpha \beta}^p|$ as a function of $\lambda_\phi$ from Eqs. (7) and (16). We consider $m_1 = 0, 0.1$, and 0.2 eV. The tightest lower bound for $\lambda_\phi$ is found using $|e_{\alpha \beta}^m|$. The result is illustrated in Fig. 5 and in Table IV. In all cases and results in this section, we have found that in the case of the inverted mass hierarchy, the bounds are similar as those presented here for the normal hierarchy, just slightly stricter in all cases. The results in the antineutrino matter potential case are also similar, just slightly less strict in all cases.

Finally, we conclude this section with remarks on perturbativity. By requiring all the Yukawa couplings to be $\sqrt{4\pi}$ at most, we find

\[ M_\Delta \lesssim \frac{617 \text{ GeV}}{\sqrt{|e_{\alpha \beta}^m|}}, \quad M_\Delta \lesssim \frac{872 \text{ GeV}}{\sqrt{|e_{\alpha \beta}^m - e_{\alpha \beta}^p|}}, \]

which are acquired by combining Eqs. (5) and (6). Taking into account the lower limits for $M_\Delta$, which we assume to be approximately 750 GeV [40,41], one can estimate the maximum possible contribution to NSI by the triplet scalar. We find $|e_{\alpha \beta}^m| \lesssim 0.677$ and $|e_{\alpha \beta}^m - e_{\alpha \beta}^p| \lesssim 1.355$. For CLFV experiments, these conditions are fulfilled (see Table I), but for $|e_{ee}^m|$ and $|e_{ee}^m - e_{ee}^p|$, the experimental limits are not restrictive enough (see Fig. 5). If DUNE confirms NSI with $|e_{ee}^m| \gtrsim 0.677$, all of it cannot be a manifestation of triplet scalar interactions, and there must be additional new physics contribution. In other words, in the case of the confirmation of the existence of triplet scalar and large $|e_{ee}^m|$, this would indicate additional NSI originating from other extensions of SM.

### Table IV. Current experimental and expected DUNE lower bounds with 90% C.L. for $\lambda_\phi$ inferred from current oscillation parameters, current bounds for NSI, and simulated DUNE bounds for NSI. NH and IH correspond to the normal and inverse neutrino mass hierarchy, respectively.

<table>
<thead>
<tr>
<th>$m_1 \text{ (eV)}$</th>
<th>Global $\lambda_\phi \text{ (eV)}$</th>
<th>DUNE $\lambda_\phi \text{ (eV)}$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>NH</td>
<td>IH</td>
</tr>
<tr>
<td>0.0</td>
<td>0.031</td>
<td>0.045</td>
</tr>
<tr>
<td>0.1</td>
<td>0.129</td>
<td>0.133</td>
</tr>
<tr>
<td>0.2</td>
<td>0.251</td>
<td>0.253</td>
</tr>
</tbody>
</table>
V. SUMMARY AND CONCLUSIONS

The triplet Higgs bosons ($\Delta = \Delta^+, \Delta^0, \Delta^0$) utilized in the type-II seesaw model will affect neutrino propagation in matter by mediating interactions not present in the Standard Model. We have studied in this work how the sensitivity of DUNE for NSI interactions can be utilized to derive a constraint for the quantity $M_\Delta/|\lambda_\phi|$, where $M_\Delta$ is the mass of the triplet bosons and $\lambda_\phi$, the strength of the coupling $\Delta\phi\phi$ between the triplet Higgs and the standard Higgs doublet. We found that a long baseline experiment with the specifications of the proposed DUNE can reach the upper bound $M_\Delta/|\lambda_\phi| \lesssim (2-4) \times 10^{12}$ at 90% C.L. If the ratio $M_\Delta/|\lambda_\phi|$ were above this value, the effects of the NSI neutrino-matter interactions caused by the triplet boson exchange would be seen in the DUNE oscillation data. We found the bound to be sensitive of the neutrino mass ordering (normal or inverted).

We found that in long baseline experiments the strictest bound on $M_\Delta/|\lambda_\phi|$ arises from the $|e_{\mu\mu}|$ and $|e_{\tau\tau}|$ constraints. DUNE would be able to improve the upper limits of these NSI parameters, as indicated in Table III. The sensitivity to the matter NSI parameters has been previously studied for the proposed HyperKamiokande and T2HK experiments, and the upper limit on $|e_{ee} - e_{\mu\mu}|$ achievable in these experiments is estimated to be improved, see [34].

In long baseline experiments, nonunitarity of the mixing matrix of the ordinary light neutrinos might give similar effects on the oscillation probabilities than the NSI due to the triplet Higgses, which might lead to a misinterpretation of the data. We found out that the effects caused by nonunitarity depend strongly on the lightest neutrino mass $m_1$ and are well below the sensitivity of DUNE. Only when $m_1 \ll 1$ eV, the signals interpreted as triplet-Higgs NSI effects could actually be caused by nonunitarity of the neutrino mixing.

We also showed that the existing constraints on the various NSI parameters obtained by studying low-energy charged lepton flavor violation (CLFV) processes, such as like $\mu^- \rightarrow e^- e^- e^-$, correspond, when interpreted in terms of the triplet Higgs model, to constraints on $M_\Delta/|\lambda_\phi|$, which are for all values of the lightest neutrino mass orders of magnitude more stringent than one would reach in DUNE.

To summarize, the study of NSI interactions in long-baseline neutrino-oscillation experiments considered in this work and at low-energy processes would give crucially central information on the triplet Higgs model and type-II seesaw model, in particular when combined with the information one can get in collider experiments for the lower limit of the triplet mass $M_\Delta$ (see, e.g., Ref. [40]). For a normal mass hierarchy and a triplet mass $M_\Delta = 750$ GeV, for example, the future DUNE data will indicate $|\lambda_\phi| \gtrsim 0.120$ eV, a clear improvement of the strictest current limit we calculated in Table IV, $|\lambda_\phi| \gtrsim 0.031$ eV.

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