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Shell-model computed cross sections for charged-current scattering of astrophysical neutrinos off ⁴⁰Ar

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Charged-current (anti)neutrino-40 Ar cross sections for astrophysical neutrinos have been calculated. The initial and final nuclear states were calculated using the nuclear shell model. The folded solar-neutrino scattering cross section was found to be $1.78(23) \times 10^{-42}$ cm², which is higher than what the previous papers have reported. The contributions from the 1⁻ and 2⁻ multipoles were found to be significant at supernova-neutrino energies, confirming the random-phase approximation (RPA) result of a previous study. The effects of neutrino flavor conversions in dense stellar matter (matter oscillations) were found to enhance the neutrino-scattering cross sections significantly for both the normal and inverted mass hierarchies. For the antineutrino scattering, only a small difference between the nonoscillating and inverted-hierarchy cross sections was found, while the normalhierarchy cross section was 2-3 times larger than that of the nonoscillating cross section, depending on the adopted parametrization of the Fermi-Dirac distribution. This property of the supernova-antineutrino signal could probably be used to distinguish between the two hierarchies in megaton LAr detectors.

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I. INTRODUCTION

The standard model of particle physics is considered not to be the final theory of the Universe and its constituents. It does not provide a good candidate for dark matter and also the tiny asymmetry between matter and antimatter in the Universe is not understood, not to mention the origin of dark energy. The first point, dark matter, is massively tackled experimentally, as it is expected that such a dark-matter particle will collide with a nucleus, resulting in a measurable recoil energy of a few keV of the hit nucleus. As is known, cross sections are very small because they have not been observed yet; hence, large detectors with very little radioactive contamination (low background) have to be installed underground to provide the necessary sensitivity. One approach, among others, are large-scale noble gas detectors. One material is argon, which has an abundance of 99.6% of ⁴⁰Ar and is currently used in the dark-matter experiments DEAP-3600 [1] and DarkSide-50 [2]. In addition, there are more applications of argon detectors in neutrino physics, one example being the 40-kiloton-scale LArTPC detector envisaged for the planned long-baseline experiment Deep Underground Neutrino Experiment (DUNE) [3]. Here, we would like to focus on cross-sectional determinations on ⁴⁰Ar for astrophysical neutrinos, which would include solar and supernova neutrinos, neutrinos from the diffuse supernovaneutrino background, low-energy atmospheric neutrinos, or general astrophysical neutrinos with energies below 60 MeV.

these investigations have been limited to Gamow-Teller (GT) and Fermi transitions. The shell-model calculations have been complicated by the large number of possible configurations for sd-pf nuclei. In Ref. [8], a new effective interaction was presented for the $1s-0d_{3/2}-0f_{7/2}-1p_{3/2}$ model space. This interaction was created to explain the isomeric shift in ³⁸K^m. The model space for which the interaction is designed is significantly smaller than the entire sd-pf model space. This allows for calculations without extra $n\hbar\omega$ type truncations used in the previous shell-model calculations. In the present paper, we have managed to perform shell-model calculations for the neutrino and antineutrino scatterings off ⁴⁰Ar for multipoles up to 3^{\pm} . We give the averaged cross sections folded with both solar- and supernova-neutrino energy spectra, which are

The focus is on v_e and \bar{v}_e reactions. Starting with the electron neutrinos from the sun, the reaction (1) (see the following

section) is possible. Given the fact that the reaction threshold

between the mother nucleus ⁴⁰Ar and the daughter nucleus ⁴⁰K

is 1.5044 MeV, only a fraction of the CNO neutrinos and the

⁸B neutrinos can be captured. The neutrino and antineutrino

scatterings off 40Ar have previously been studied using the

random-phase approximation (RPA) [4,5]. In Ref. [5], the

importance of the scattering to the 1- and 2- final nuclear

states was highlighted. The neutrino scattering $^{40}{\rm Ar}(\nu,e^-)^{40}{\rm K}$

has been studied also using the nuclear shell model [6,7] but

This article is organized as follows. In Sec. II, we give the theoretical background behind neutrino-nucleus scattering. In

conversions in the dense stellar matter.

of interest from an experimental point of view. In the present paper, we also take into account the effects of neutrino flavor

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Sec. III, we present our results for the total and averaged cross sections, and in Sec. IV, we draw the conclusions.

II. THEORETICAL FORMALISM

In this work, we consider charged-current neutrino and antineutrino scattering off the nucleus ⁴⁰Ar, i.e., the reactions

$$\nu_e + {}^{40}\text{Ar}(0^+)_{\text{g.s.}} \rightarrow {}^{40}\text{K} + e^-$$
 (1)

and

$$\bar{\nu}_e + {}^{40}\text{Ar}(0^+)_{\text{g.s.}} \rightarrow {}^{40}\text{Cl} + e^+,$$
 (2)

where the daughter nucleus can be in an excited state. At the energies considered in this work, the creation of the heavier lepton flavors, μ and τ , is not energetically possible.

For the solar and core-collapse supernova neutrinos, the four-momentum transfer is small compared to the mass of the exchanged gauge boson W^\pm , i.e., $Q^2 = -q_\mu q^\mu \ll M_{W^\pm}^2$, where the transferred four-momentum is the difference in the momenta of the outgoing and incoming leptons (due to energy conservation also the difference of the momenta of the mother and daughter nuclei is small). Therefore, to a good approximation the scattering can be considered in the lowest order as a single effective vertex with a coupling constant $G = G_F \cos(\theta_{\rm C})$, where G_F is the Fermi constant and $\theta_{\rm C} \approx 13^\circ$ is the Cabibbo angle. The matrix element of this effective Hamiltonian can be written as

$$\langle f | H_{\text{eff}} | i \rangle = \frac{G}{\sqrt{2}} \int d^3 \mathbf{r} l_{\mu} e^{-\mathbf{q} \cdot \mathbf{r}} \langle f | \mathcal{J}^{\mu}(\mathbf{r}) | i \rangle, \quad (3)$$

where \mathcal{J}^{μ} denotes the hadronic current and $l_{\mu} = e^{\mathbf{q} \cdot \mathbf{r}} \langle l | j_{\mu}(r) | \nu \rangle$ [9], where j_{μ} is the leptonic current.

The initial nuclear state in the scatterings of Eqs. (1) and (2) is the $J_i^{\pi_i} = 0^+$ ground state of ⁴⁰Ar. We assume that the final nuclear states in ⁴⁰K and ⁴⁰Cl also have well-defined spin parities $J_f^{\pi_f}$. The double differential cross section for the charged-current (CC) (anti)neutrino-nucleus scattering is given by [9–11]

$$\left[\frac{d^2 \sigma_{i \to f}}{d\Omega d E_{\text{exc}}}\right] = \frac{G^2 |\mathbf{k}_{l^{\mp}}| E_{l^{\mp}}}{\pi (2J_i + 1)} F(\pm Z_f, E_{\mathbf{k}_{l^{\mp}}}) \times \left(\sum_{J \geqslant 0} \sigma_{\text{CL}}^J + \sum_{J \geqslant 1} \sigma_{\text{T}}^J\right), \tag{4}$$

where $\mathbf{k}_{I^{\mp}}$ and $E_{I^{\mp}}$ are the three-momentum and energy of the outgoing lepton (e^{\mp}) , respectively, and $F(\pm Z_f, E_{\mathbf{k}_{I^{\mp}}})$ is the Fermi function which accounts roughly for the Coulomb interaction of the final-state lepton and nucleus. The Coulomb-longitudinal component σ_{CL}^J and the transverse component σ_{T}^J in Eq. (4) are defined as

$$\sigma_{\text{CL}}^{J} = (1 + a\cos\theta)|(J_f||\mathcal{M}_J(q)||J_i)|^2 + (1 + a\cos\theta - 2b\sin^2\theta)|(J_f||\mathcal{L}_J(q)||J_i)|^2 + \frac{E_k - E_{k'}}{q}(1 + a\cos\theta + c) \times 2\text{Re}[(J_f||\mathcal{M}_J(q)||J_i)^*(J_f||\mathcal{L}_J(q)||J_i)]$$
(5)

and

$$\sigma_{\mathrm{T}}^{J} = (1 - a\cos\theta + b\sin^{2}\theta)$$

$$\times \left[\left| \left(J_{f} \right| \left| \mathcal{T}_{J}^{\mathrm{mag}}(q) \right| \left| J_{i} \right) \right|^{2} + \left| \left(J_{f} \right| \left| \mathcal{T}_{J}^{\mathrm{el}}(q) \right| \left| J_{i} \right) \right|^{2} \right]$$

$$\mp \frac{E_{\mathbf{k}} - E_{\mathbf{k}'}}{q} (1 - a\cos\theta - c)$$

$$\times 2\operatorname{Re}\left[\left(J_{f} \right| \left| \mathcal{T}_{J}^{\mathrm{mag}}(q) \right| \left| J_{i} \right) \left(J_{f} \right| \left| \mathcal{T}_{J}^{\mathrm{el}}(q) \right| \left| J_{i} \right)^{*} \right]. \quad (6)$$

Here $E_{\bf k}$ and $E_{\bf k'}$ refer to the energies of the incoming and outgoing leptons. The minus sign is used for the neutrino scattering and the plus sign is for the antineutrino scattering. The quantities a, b, and c in Eqs. (5) and (6) are

$$a = \sqrt{1 - \frac{m_f^2}{E_{\nu'}^2}},\tag{7}$$

$$b = \frac{a^2 E_{\mathbf{k}} E_{\mathbf{k'}}}{q^2},\tag{8}$$

$$c = \frac{n_f^2}{aE_{\mathbf{k}'}},\tag{9}$$

where the magnitude of three-momentum transfer q is given by

$$q = |\mathbf{q}| = \sqrt{(E_{\mathbf{k}} - aE_{\mathbf{k}'})^2 + 2aE_{\mathbf{k}}E_{\mathbf{k}'}(1 - \cos\theta)}.$$
 (10)

The final-state interactions are treated in the modified effective-momentum approximation (MEMA) of Ref. [12]. There the effective momentum inside the nucleus is given by

$$k_{\rm eff} = \sqrt{E_{\rm eff} - m_e^2},\tag{11}$$

where m_e is the electron mass and E_{eff} is defined as

$$E_{\rm eff} = E_{\mathbf{k}'} - V_{\rm C}(0).$$
 (12)

The quantity $V_{\rm C}(0)$ is the value of the Coulomb potential produced by the final-state nucleus at the origin. According to MEMA, we use for small values of $k_{\rm eff}$ the Fermi function, whereas for the larger values of $k_{\rm eff}$ we omit the Fermi function in Eq. (4) and replace the energy and three-momentum of the outgoing lepton by the effective values $k_{\rm eff}$ and $E_{\rm eff}$.

III. RESULTS AND DISCUSSION

A. Nuclear-structure calculations

The wave functions of the initial and final nuclear states, and the one-body transition densities (OBTDs), related to the transitions, were calculated using the nuclear shell model. The calculations were done using the shell-model code NUSHELLX@MSU [14] in the $1s-0d_{3/2}-0f_{7/2}-1p_{3/2}$ valence space using the Hamiltonian ZBM2M [8]. In Ref. [8], the proton and neutron excitations across the N, Z = 20 shell gap were found to be significant in the 40 Ca region. Excitations across the shell gap are needed to produce the positive-parity states in 40 Cl and 40 K with J = 0, 1, which are the final nuclear states for the Fermi and Gamow-Teller type transitions. The contributions from these multipolarities dominate the (anti)neutrino-scattering cross sections at energies up to few tens of MeVs. In this work, we limit the considered final nuclear

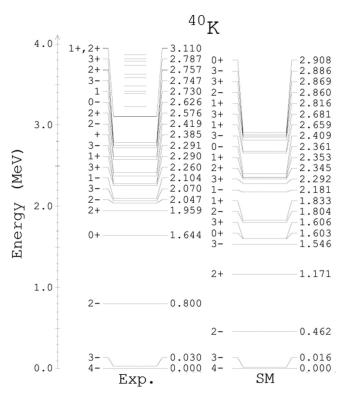


FIG. 1. Experimental and shell-model excitation spectra of ⁴⁰K. The observed states with uncertain spin parities or angular momenta above 4 are not shown. The experimental spectrum is from Ref. [13].

states to the 100 lowest states for each spin parity up to J=3(800 states). For 40 K, this includes states up to \approx 9 MeV and for 40 Cl up to \approx 7 MeV. For the calculation of excited states with higher energies, a larger valence space would be needed. The computational burden of such shell-model calculations is, however, too large for modern computers. In addition, the effective interactions used in shell-model calculations are designed only for low energies. The final nuclear states included here are enough for solar-neutrino energies, but for supernova energies higher excited states can probably contribute. In Ref. [5], the importance of excited states with energies 10-20 MeV for supernova neutrinos was pointed out. The previous randomphase approximation calculations have found the contributions from $0^+ \rightarrow 4^{\pm}$ scatterings to be very small for energies below 80 MeV [5], and thus the higher multipole contributions can be neglected. As in many previous neutrino-nucleus scattering studies (see, e.g., Refs. [9,15]), in this work we use the quenched, nuclear-matter value $g_A = 1.0$ for the axial-vector coupling constant. This is also consistent with the quenching used in Refs. [6,7]. However, there are indications that for higher neutrino energies the free-nucleon value $g_A = 1.27$ might be more appropriate [16]. The uncertainties related to g_A are discussed and estimated in Sec. IIIE.

The experimental and shell-model excitation spectra of ⁴⁰K are shown in Fig. 1. The shell model correctly predicts the spin and parity of the ground state and first two excited states. The first 1⁺ state is predicted to be 450 keV lower than the experimental value. While this increases the contribution of the state, the effect to the averaged cross section is minuscule, since

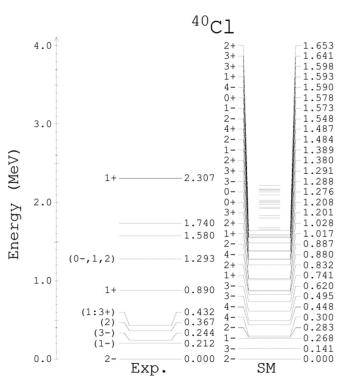


FIG. 2. Experimental and shell-model excitation spectra of ⁴⁰Cl. The observed states with uncertain spin parities or angular momenta above 4 are not shown. The experimental spectrum is from Ref. [13].

the contribution of this state is two magnitudes lower than the dominant contributions (see Fig. 5). The positive-parity state at 2385 keV and the J=1 state at 2730 keV are predicted to be 1^+ states. For the 0_2^+ Isobaric Analog State (IAS) state, the experimental value 4384 keV was adopted.

For ⁴⁰Cl, the excitation spectra are presented in Fig. 2. For this nucleus, the excitation spectrum is not well known experimentally. The shell model is able to predict the spin and parity of the ground state correctly but gets the order of the first 1⁻ and 3⁻ states wrong. However, this kind of small deviation from the experimental energies has only small effects on the total folded cross section.

B. Total cross sections

The total unfolded cross sections as functions of the energy of the incident neutrino for the 40 Ar(v,e^-) 40 K scattering and its decomposition to different multipole contributions is shown in Fig. 3 and Table I. The total cross section grows quadratically for energies below 35 MeV and linearly for energies between 35 and 60 MeV. Below 25 MeV, the total cross section is completely dominated by Gamow-Teller and Fermi transitions. These transitions contribute the most for energies up to 60 MeV, but the 2^- transitions become significant for the higher energies. Contributions from other multipoles begin to play a role above 50 MeV, but contribute still only a few percent. It is to be expected that the numbers of Table I are realistic up to 40 MeV (see the discussion in Sec. III E 2). The RPA calculation of Ref. [5] predicted the scatterings to the 1^- states to contribute approximately as much as the scatterings to the 2^- states for

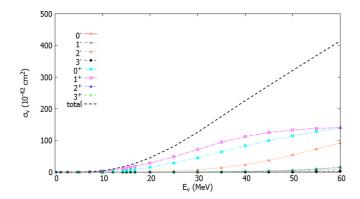


FIG. 3. Unfolded cross sections for the charged-current 40 Ar(ν , e^-) 40 K scattering as functions of the energy of the incident neutrino.

energies below 60 MeV. The present shell-model calculation, however, predicts the 1⁻ contributions to be much lower.

For the antineutrino scattering 40 Ar($\bar{\nu}, e^{-}$) 40 Cl, the unfolded cross sections are presented in Fig. 4 and Table II as functions of the antineutrino energy. The total cross section grows quadratically for energies up to 60 MeV. The total cross section for the antineutrino scattering is only 5% of the neutrino-scattering cross section for high energies and even less for the lower energies. This is partially explained by the 6-MeV-higher Q value for the β^- decay of 40 Cl [17]. The GT transitions dominate for energies below 40 MeV but for higher energies the spin-dipole states (1 $^-$ and 2 $^-$) are the major contributors. The Fermi transitions do not play a role since there is no isobaric analog state of 40 Ar in 40 Cl.

C. Averaged solar-neutrino cross sections

From the experimental point of view, the interesting quantity is the averaged cross section $\langle \sigma \rangle$ which is found by folding the total cross section with the appropriate neutrino energy profile, taking into account the reaction threshold 1.5044 MeV. For the solar neutrinos, we adopt a ⁸B profile. The differential cross section for the solar-neutrino reaction ⁴⁰Ar(ν , e^-)⁴⁰K as a function of excitation energy is presented in Fig. 5(a). The largest contribution in the shell-model calculation comes from the scattering to the third 1⁺ state at 2659 keV. This corresponds to the experimentally observed J=1 state at 2730 keV. The

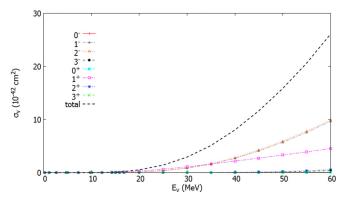


FIG. 4. Unfolded cross sections for the charged-current 40 Ar $(\bar{\nu}, e^+)^{40}$ Cl scattering as functions of the energy of the incident neutrino.

transition to the IAS state contributes only 40% of this. The other significant contributions come from the transition to the 1_6^+ , 1_{10}^+ , 1_{15}^+ , and 1_{17}^+ states.

For the solar neutrinos, the total computed cross section is 1.777×10^{-42} cm², which is higher than the averaged cross sections $1.15(7) \times 10^{-42}$ cm² of Ref. [6] and 1.405×10^{-42} cm² of Ref. [7]. The folded cross sections of the previous papers have considered only the GT and IAS transitions. Furthermore, in the previous shell-model calculations, the model space has been chosen as sd-pf with only the $(sd)^{-2}(pf)^2$ type of two-particle–two-hole excitations allowed.

D. Averaged supernova-neutrino cross sections

1. Averaged cross sections without neutrino flavor conversions

The averaged cross section $\langle \sigma \rangle$ for the supernova neutrinos we find by folding the total cross section with a Fermi-Dirac distribution

$$F_{\rm FD}(E_{\bf k}) = \frac{1}{F_2(\alpha_{\nu})T_{\nu}} \frac{(E_{\bf k}/T_{\nu})^2}{1 + \exp(E_{\bf k}/T_{\nu} - \alpha_{\nu})},$$
 (13)

where T_{ν} is the effective neutrino temperature and α_{ν} is the pinching parameter. If the temperature T_{ν} and the value of the parameter α_{ν} are known, the average neutrino energy is given

TABLE I. Total unfolded cross sections for the neutrino-nucleus scattering 40 Ar(ν , e^-) 40 K for different neutrino energies, decomposed into the contributing multipolarities. The cross sections are in the units 10^{-42} cm² and the exponents are shown in parentheses.

E_{ν} [MeV]	Total	0+	0-	1+	1-	2+	2-	3+	3-
5.0	1.01(-1)	9.27(-9)	3.02(-5)	1.01(-1)	5.56(-7)	1.37(-7)	3.41(-4)	1.51(-7)	8.96(-11)
10.0	4.56(0)	8.45(-1)	3.25(-3)	3.68(0)	1.55(-3)	9.62(-5)	3.08(-2)	1.19(-4)	1.03(-7)
15.0	1.99(1)	5.85(0)	1.99(-2)	1.37(1)	2.12(-2)	2.34(-3)	2.29(-1)	2.70(-3)	6.93(-6)
20.0	4.68(1)	1.55(1)	5.29(-2)	2.98(1)	1.14(-1)	1.90(-2)	1.27(0)	2.09(-2)	1.36(-4)
25.0	8.43(1)	2.90(1)	1.01(-1)	5.10(1)	3.79(-1)	8.84(-2)	3.64(0)	9.50(-2)	1.24(-3)
30.0	1.31(2)	4.55(1)	1.66(-1)	7.55(1)	9.32(-1)	2.95(-1)	8.22(0)	3.12(-1)	6.99(-3)
40.0	2.38(2)	8.28(1)	3.41(-1)	1.20(2)	3.29(0)	1.78(-0)	2.71(1)	1.85(0)	9.37(-2)
50.0	3.42(2)	1.15(2)	5.72(-1)	1.43(2)	7.25(0)	6.46(0)	6.19(1)	6.57(0)	6.19(-1)
60.0	4.45(2)	1.39(2)	8.50(-1)	1.51(2)	1.13(1)	1.68(1)	1.05(2)	1.67(1)	2.62(0)

TABLE II. Total unfolded cross sections for the antineutrino-nucleus scattering 40 Ar $(\bar{\nu}, e^+)^{40}$ Cl for different antineutrino energies, decomposed into the contributing multipolarities. The cross sections are in the units 10^{-42} cm² and the exponents are shown in parentheses.

E_{ν} [MeV]	Total	0+	0-	1+	1-	2+	2-	3+	3-
5.0									
10.0	1.29(-3)	6.58(-12)	2.73(-5)	8.31(-4)	1.96(-6)	1.10(-8)	4.25(-4)	1.01(-10)	2.52(-9)
15.0	1.17(-1)	3.80(-7)	3.02(-3)	8.05(-2)	1.42(-2)	1.64(-5)	1.90(-2)	4.74(-6)	1.44(-6)
20.0	6.10(-1)	1.11(-5)	1.13(-2)	3.76(-1)	1.07(-1)	3.25(-4)	1.15(-1)	9.19(-5)	3.55(-5)
25.0	1.61(0)	8.94(-5)	2.51(-2)	8.54(-1)	3.58(-1)	2.22(-3)	3.74(-1)	6.12(-4)	3.25(-4)
30.0	3.24(0)	4.02(-4)	4.44(-2)	1.46(0)	8.48(-1)	9.07(-3)	8.81(-1)	2.43(-3)	1.75(-3)
40.0	8.64(0)	3.32(-3)	9.93(-2)	2.82(0)	2.75(0)	6.61(-2)	2.86(0)	1.66(-2)	2.05(-2)
50.0	1.67(1)	1.42(-2)	1.76(-1)	4.17(0)	5.87(0)	2.58(-1)	6.06(0)	5.89(-2)	1.17(-1)
60.0	2.72(1)	4.14(-2)	2.72(-1)	5.56(0)	9.94(0)	6.93(-1)	1.01(1)	1.41(-1)	4.32(-1)

by the relation

$$\langle E_{\nu} \rangle / T_{\nu} = \frac{F_3(\alpha_{\nu})}{F_2(\alpha_{\nu})}, \tag{14}$$

where

$$F_k(\alpha_{\nu}) = \int \frac{x^k dx}{1 + \exp(x - \alpha_{\nu})}.$$
 (15)

The normalized differential cross sections for the reaction $^{40}{\rm Ar}(\nu,e^-)^{40}{\rm K}$ as function of the excitation energy are presented in Figs. 5(b) and 5(c). The largest contribution comes from the scattering to the third 1^+ state and the transition to the IAS state, both contributing some 50% of the total. The other significant contributions come from the transition to the 1_6^+ , 1_{10}^+ , 1_{15}^+ , and 1_{17}^+ states, as in the case of the solar neutrinos. The differential cross sections for the reaction $^{40}{\rm Ar}(\bar{\nu},e^+)^{40}{\rm Cl}$ as function of the excitation energy are presented in Fig. 6. The largest contributors are the transitions to 1_6^+ , $2^-_{\rm g.s.}$, and 1_6^- states. There are significant contributions coming also from the $2_{2,4}^-$, 1_4^- , and $1_{1,2,8,12,19,28}^+$ states.

In Ref. [4], the ratio of the supernova neutrino and antineutrino cross sections was found to be approximately 12.5 with no flavor conversions included in a scenario with averaged energies $\langle E_{\nu} \rangle = 11$ MeV and $\langle E_{\bar{\nu}} \rangle = 16$ MeV respectively. Folding the cross sections of the present work using Fermi-Dirac distributions with these average energies and assuming $\alpha = 0.0$, we find that $\sigma_{\nu} = 14.6 \times 10^{-42}$ cm² and $\sigma_{\bar{\nu}} = 887 \times 10^{-45}$ cm² respectively. This gives a ratio of 16.5 for the neutrino and antineutrino cross sections, which is in good agreement with the RPA result of Ref. [4].

2. Effects of (anti)neutrino flavor conversions

Because of the large rest masses of both muon and τ lepton, only electron-flavor (anti)neutrinos are detected in charged-current solar- and supernova-neutrino detection experiments. The energy profile of the (anti)neutrinos detected on Earth is, however, affected by (anti)neutrino flavor conversions (matter oscillations) which take place when the neutrinos propagate through the dense stellar matter [18]. We assume that the muon and τ -neutrino energy profiles are identical, reducing the problem into a two-neutrino one. In the two-neutrino problem, we consider flavor changes $\nu_x \rightarrow \nu_e$, where ν_x is a linear combination of muon and τ neutrinos [19,20]. The energy profiles of electron neutrinos and antineutrinos reaching Earth

can be written as

$$F_{\nu_e}(E_{\mathbf{k}}) = p(E_{\mathbf{k}})F_{\nu_e}^0(E_{\mathbf{k}}) + [1 - p(E_{\mathbf{k}})]F_{\nu_e}^0(E_{\mathbf{k}}), \quad (16)$$

$$F_{\bar{\nu}_e}(E_{\mathbf{k}}) = \bar{p}(E_{\mathbf{k}})F_{\bar{\nu}_e}^0(E_{\mathbf{k}}) + [1 - \bar{p}(E_{\mathbf{k}})]F_{\bar{\nu}_x}^0(E_{\mathbf{k}}), \quad (17)$$

where p and \bar{p} are the survival probabilities of the electron neutrinos and antineutrinos respectively, and the quantities $F^0_{\nu_{e/x}}(E_{\mathbf{k}})$ and $F^0_{\bar{\nu}_{e/x}}(E_{\mathbf{k}})$ are the initial energy profiles of the neutrinos and antineutrinos.

For the survival probabilities p and \bar{p} , we use the values from Refs. [21,22]. For the normal mass hierarchy, the values are

$$p(E_{\mathbf{k}}) = 0, (18)$$

$$\bar{p}(E_{\mathbf{k}}) = \begin{cases} \cos^2 \theta_{12}, & E_{\mathbf{k}} < \bar{E}_s, \\ 0, & E_{\mathbf{k}} > \bar{E}_s, \end{cases}$$
(19)

where $\bar{E}_s = 18$ MeV [22]. For the inverted mass hierarchy, we use the probabilities

$$p(E_{\mathbf{k}}) = \begin{cases} \sin^2 \theta_{12}, & E_{\mathbf{k}} < \bar{E}_s, \\ 0, & E_{\mathbf{k}} > \bar{E}_s, \end{cases}$$
(20)

$$\bar{p}(E_{\mathbf{k}}) = \cos^2 \theta_{12},\tag{21}$$

where $\bar{E}_s = 7$ MeV [19]. For the normal hierarchy $\sin^2 \theta_{12} = 0.306$ and for the inverted hierarchy $\sin^2 \theta_{12} = 0.312$ [23].

For the calculations, we used three sets of parameters $(\alpha, T, \langle E \rangle)$ taken from Ref. [24]. The values of the parameters for neutrinos and antineutrinos are presented in Table III.

The folded cross sections for supernova neutrinos are listed in Table IV. The neutrino-scattering cross section is increased roughly three-fold when the neutrino flavor conversions are taken into account. There is little difference between the cross sections with normal and inverted mass hierarchies. For the antineutrino scattering with parameter sets (I) and (II), the inverted-hierarchy cross section is enhanced by 30% while the normal-hierarchy cross section is enhanced by roughly 100% relative to the nonoscillating case. For the parameter set (III), the inverted-hierarchy cross section is 67% larger than the nonoscillating one, while the normal-hierarchy one is almost three times larger than the nonoscillating one.

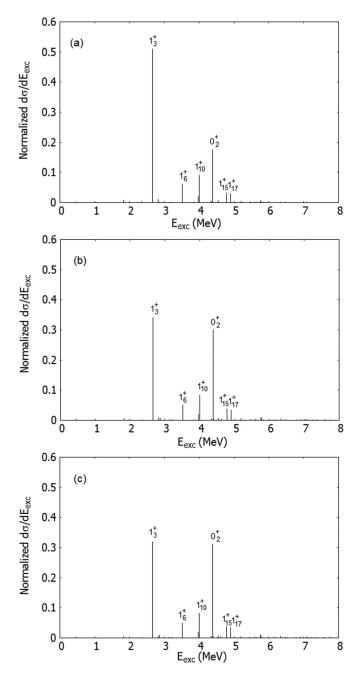


FIG. 5. Differential cross section for the CC supernova-neutrino scattering to final nuclear states at excitation energies $E_{\rm exc}$. The total cross section is normalized to unity. Panel (a) is folded with the solar neutrino spectrum, panel (b) with Fermi-Dirac distribution with parametrization (I), and panel (c) with parametrization (II) (see Table III). Here the effects of flavor conversions are not included.

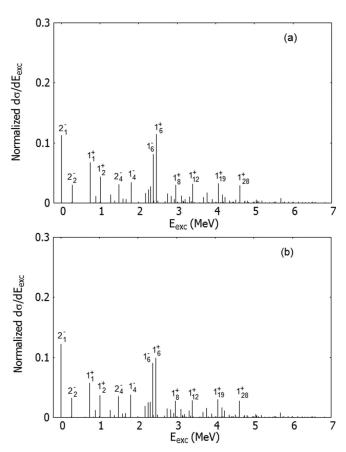


FIG. 6. Differential cross section for the CC supernovaantineutrino scattering to final nuclear states at excitation energies $E_{\rm exc}$. The total cross section is normalized to unity. Panel (a) with Fermi-Dirac distribution with parametrization (I) and panel (b) with parametrization (II) (see Table III). Here the effects of flavor conversions are not included.

E. Uncertainties

There are many sources of uncertainties for theoretical estimations of (anti)neutrino-nucleus scattering cross sections, which makes the estimation of the overall uncertainty difficult. In a previous shell-model study [6], the uncertainty was estimated by assuming that each GT strength has a statistical uncertainty of 10% since generally the uncertainties in the B(GT) values are of the order 5–10% [25]. Because of the large number of states in the present study, such statistical uncertainties amount to less than 3%. For the supernova (anti)neutrinos, there are also uncertainties related to the distribution of neutrino energies, which cannot be accurately estimated. The actual supernova-neutrino spectrum is complex, and the details

TABLE III. Values of parameters α , T, and the average neutrino energy $\langle E_{\nu_{e/x}} \rangle$ in MeV used for the supernova-neutrino calculations. The values are adopted from Ref. [24]. The index e refers to electron neutrinos and $x = \mu, \tau$ to the nonelectron flavors.

	$(\alpha_{v_e},T_{v_e},\langle E_{v_e}\rangle)$	$(lpha_{ar{v}_e},T_{ar{v}_e},\langle E_{ar{v}_e} angle)$	$(\alpha_{\nu_x}, T_{\nu_x}, \langle E_{\nu_x} \rangle)$	$(lpha_{ar{ u}_{\scriptscriptstyle X}},T_{ar{ u}_{\scriptscriptstyle X}},\langle E_{ar{ u}_{\scriptscriptstyle X}} angle)$
(I)	(3.0, 2.88, 11.5)	(3.0, 3.41, 13.6)	(3.0, 4.08, 16.3)	(3.0, 4.08, 16.3)
(II)	(0.0, 3.65, 11.5)	(0.0, 4.32, 13.6)	(0.0, 5.17, 16.3)	(0.0, 5.17, 16.3)
(III)	(3.0, 2.88, 11.5)	(3.0, 3.41, 13.6)	(0.0, 5.17, 16.3)	(0.0, 5.17, 16.3)

TABLE IV. Folded cross sections in units of cm² for supernova neutrinos with the quenched value $g_A = 1.00$. The first column refers to the parameters of the Fermi-Dirac distribution given in Table III. In the second (ν_e) and fifth columns ($\bar{\nu}_e$), cross sections for nonoscillating neutrinos are given, while the third, fourth, sixth, and seventh columns give the cross sections with matter oscillations included in the normal mass hierarchy (NH) and in the inverted mass hierarchy (IH).

Parameters	ν_e	$v_{ex}^{ m NH}$	$v_{ex}^{ m IH}$	$ar{ u}_e$	$ar{ u}_{ex}^{ m NH}$	$ar{ u}_{ex}^{ ext{IH}}$
(I)	13.90×10^{-42}	37.08×10^{-42}	37.09×10^{-42}	322.8×10^{-45}	678.1×10^{-45}	436.2×10^{-45}
(II)	16.63×10^{-42}	41.70×10^{-42}	42.08×10^{-42}	477.7×10^{-45}	947.3×10^{-45}	624.9×10^{-45}
(III)	13.90×10^{-42}	41.70×10^{-42}	42.06×10^{-42}	322.8×10^{-45}	948.5×10^{-45}	518.3×10^{-45}

of the spectrum are not well known. However, there are two potentially large sources of uncertainty which we can address. The first one is related to the value of the axial-vector coupling constant g_A , for which the correct effective value is not well understood. For the sd and pf shells half-life comparisons of GT transitions suggest a quenched value $g_A \approx 1.00$ [26,27]. However, there are indications that for high-energy neutrinos the free-nucleon value $g_A = 1.27$ should be used [16]. The effects of g_A are discussed in Sec. IIIE 1. The other potentially large source of systematic uncertainty is related to the limited valence space used in the calculations. Neutrinos with high energies excite states which are out of reach for valence spaces used in the shell-model calculations. The effect of the higher energy states on the folded cross sections are discussed in Sec. IIIE 2.

1. Value of gA

Adopting the free-nucleon value $g_A = 1.27$ instead of the quenched value increases the folded cross section for the solar-neutrino-nucleus scattering 40 Ar(ν,e^-) 40 K to $\sigma_{\nu} = 2.642 \times 10^{-42}$ cm². However, for the solar neutrinos the quenched value $g_A = 1.0$ is more appropriate, since the neutrino energies are lower. We assume the uncertainty related to this choice to be 5% (i.e., $g_A = 1.00(5)$), which includes most effective values obtained in previous shell-model studies in the sd and pf shells [26,28]. The 3% error related to the nuclear structure can be assumed to be uncorrelated with the error of g_A . With these assumptions, we end up with a cross section of $1.78(23) \times 10^{-42}$ cm² for the solar-neutrino-nucleus scattering.

For the supernova (anti)neutrinos, the results are listed in Table V. Since the energies are several MeV higher than for the solar neutrinos, the appropriate effective value to be used for g_A is not so clear. It is best to consider the results of Table IV as lower limits and those of Table V as upper limits for the cross section. Since the GT transitions dominate the folded cross sections, the cross sections scale roughly $\propto g_A^2$. Because of this scaling, the ratios between the folded cross sections corresponding to the nonoscillating case, inverted mass hierarchy, and normal mass hierarchy are similar for both the free-nucleon and quenched values of g_A .

2. High-energy neutrinos

The shell-model computed supernova-neutrino-nucleus cross section for the reaction $^{40}{\rm Ar}(\nu,e^-)^{40}{\rm K}$ is roughly proportional to E_{ν}^2 up to 35 MeV, as can be seen from Fig. 7. Beyond that, the shell model predicts roughly a linear energy dependence for the cross section. However, the QRPA result of Ref. [5] predicts larger cross sections and a rough proportionality to E_v^2 for neutrino energies between 40 and 80 MeV. Since we expect the QRPA results be more reliable than the shell model ones for higher energies, we need to correct for the missing cross section for the high-energy neutrinos. The small cross sections for high-energy neutrinos stem from the use of a too limited valence space for neutrino scattering at these energies. However, the effects of this on the folded cross sections are expected to be rather modest, since the tail of the supernova-neutrino energy distribution above 35 MeV is quite small and dies out exponentially. The missing strength can be approximated by assuming that the cross section keeps growing proportional to E_{ν}^2 also for energies above 35 MeV in a way which reproduces the QRPA cross sections at the higher energies. In Fig. 7, the total cross section is plotted together with a quadratic fit function which intersects the origin and tangents the shell-model cross section at 35 MeV. The resulting fit function agrees with the QRPA results of Ref. [5] at high energies, giving roughly $\sigma = 5 \times 10^{-40}$ cm² for 60 MeV and $\sigma = 8 \times 10^{-40} \text{ cm}^2$ for 80 MeV. It should be stressed that the energy dependence of the neutrino cross section is not as trivial as E_{ν}^2 , but the fitted function can be used to estimate the effect of the missing high-energy states, since it reproduces the 60to 80-MeV QRPA results well, as well as agreeing with the shell-model results for the 35- to 40-MeV energies. For the lower energies, the shell-model cross section should of course be used and not that of the fit.

One can estimate the effect of the missing total cross section beyond 40 MeV (this is where the quadratic fit function and the shell-model cross section start to depart from each other) on the folded cross sections. For this, we look at the proportion of neutrinos with energies above 40 MeV in the neutrino-energy profile. The proportion of these neutrinos is the largest for the

TABLE V. Same as Table IV but with the free nucleon value $g_A = 1.27$ adopted for the axial-vector coupling constant.

Parameters	ν_e	$ u_{ex}^{\mathrm{NH}}$	$v_{ex}^{ m IH}$	$ar{ u}_e$	$ar{ u}_{ex}^{ m NH}$	$ar{ u}_{ex}^{ ext{IH}}$
(I) (II) (III)	19.15×10^{-42} 23.03×10^{-42} 19.15×10^{-42}	50.80×10^{-42} 56.83×10^{-42} 56.83×10^{-42}	50.81×10^{-42} 56.87×10^{-42} 56.87×10^{-42}	512.8×10^{-45} 759.1×10^{-45} 512.8×10^{-45}	1077×10^{-45} 1501×10^{-45} 1506×10^{-45}	693.1×10^{-45} 993.2×10^{-45} 823.7×10^{-45}

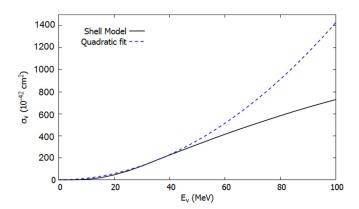


FIG. 7. The total shell-model cross section and a quadratic fit.

parameters ($\alpha = 0, T = 5.17$) and it is 1.87%. It then turns out that calculating the folded cross section with the quadratic fit function above 35 MeV, instead of the shell-model one, actually increases the folded cross section by about 0.9%. For parameter sets with lower average energies, the effect is significantly reduced from this. For example, for $(\alpha = 3, T = 2.88)$ the increase is only about 0.01%. Therefore, the lack of computed strength beyond 35 MeV has no practical effect on the folded cross sections calculated in the present paper. However, the numbers of Table I are expected to be realistic only up to 40 MeV. As seen in Fig. 4, the roughly quadratic behavior of the total antineutrino cross section continues up to 60 MeV and thus the numbers in Table II should be reliable. Furthermore, one should point out that the most contribution to the folded cross sections, both for the solar as well as for the supernova neutrinos, comes from nuclear excitations at energies that are best described by the nuclear shell model. In this sense, the present results for the folded cross sections should be considered as the best on the market.

IV. CONCLUSIONS

In the present paper, we have calculated cross sections for the charged-current neutrino and antineutrino scatterings $^{40}{\rm Ar}(\nu,e^-)^{40}{\rm K}$ and $^{40}{\rm Ar}(\bar{\nu},e^+)^{40}{\rm Cl}$ for astrophysical neutrinos with energies below 60 MeV, especially relevant for both solar and supernova neutrinos. The initial and final nuclear wave functions were calculated using the nuclear shell model. The effects of (anti)neutrino flavor conversions in dense stellar matter (matter oscillations) were also included.

While the previous shell-model calculations of cross sections have considered only Gamow-Teller and Fermi types of transitions, in the present paper we consider also transitions to the first $100~0^{\pm},~1^{\pm},~2^{\pm},~$ and 3^{\pm} states. Contributions from the spin-dipole states (1⁻ and 2⁻) dominate the total unfolded antineutrino-scattering cross section for antineutrino energies above 40 MeV. Especially the lowest two 2⁻ states and the

 6^{th} 1^- state give significant contributions to the cross section. For the total unfolded neutrino cross section, the transitions to 2^- states in 40 K becomes significant above 30 MeV of neutrino energy. It is therefore clear that the 1^- and 2^- multipolarities should not be omitted in the cross-sectional calculations.

For solar neutrinos, with a 8B distribution, the folded cross section was found to be $\sigma_{\nu} = 1.78(23) \times 10^{-42} \text{ cm}^2$. This cross section is higher than the folded cross sections $1.15(7) \times 10^{-42} \text{ cm}^2$ [6] and $1.405 \times 10^{-42} \text{ cm}^2$ [7] of previous theoretical papers, where only Fermi and Gamow-Teller transitions were taken into account.

We also computed the folded scattering cross sections for supernova (anti)neutrinos. To test the scope of our calculations, the cross sections were also folded with the supernova-neutrino spectra used in the RPA-based calculation of Ref. [4] with no matter oscillations included. The neutrino-antineutrino crosssectional ratio was found to be 16.5, which is in a reasonable agreement with the ratio 12.5 reported in Ref. [4]. Though the limited valence space considered in the present paper is unable to account for giant resonances, the systematic uncertainty related to this propagates to the folded cross sections at the level of 1% or less, as verified by our analysis of the previous RPA results. Since the folded cross sections for both the solar and supernova neutrinos gather the relevant contributions from nuclear excitations best described by the nuclear shell model, the present results for the folded cross sections can be considered as the most accurate ones available thus far.

For supernova-neutrino scattering, the cross section is increased roughly threefold when the neutrino flavor conversions are taken into account. The results for normal and inverted mass hierarchies agreed with 1% accuracy for all three adopted Fermi-Dirac distribution parameter sets (see Table III). For parametrizations (I) and (II), the antineutrino-scattering cross sections in the inverted-hierarchy scenario were enhanced by 30–35% with respect to the nonoscillating ones, while for the parameter set (III) the inverted-hierarchy cross section was 67% larger. The normal-hierarchy cross section was roughly twice as large as the nonoscillating cross section for the first two parameter sets and three times larger for the parameter set (III). One can then speculate that the strong effects of the neutrino mass hierarchy on the supernova-antineutrino signal could be used to distinguish between the two hierarchies in megaton LAr detectors. On the other hand, if the hierarchy was known, one could learn about the flavor-conversion processes inside the supernovae.

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