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High-resolution laser spectroscopy of long-lived plutonium isotopesA. Voss,^{1,*} V. Sonnenschein,^{1,†} P. Campbell,² B. Cheal,³ T. Kron,⁴ I. D. Moore,^{1,‡} I. Pohjalainen,¹ S. Raeder,^{5,§} N. Trautmann,⁶ and K. Wendt⁴¹*University of Jyväskylä, Department of Physics, 40014 Jyväskylä, Finland*²*The University of Manchester, School of Physics and Astronomy, Manchester M13 9PL, England, United Kingdom*³*University of Liverpool, Oliver Lodge Laboratory, Liverpool L69 7ZE, England, United Kingdom*⁴*Johannes-Gutenberg Universität Mainz, Institut für Physik, 55128 Mainz, Germany*⁵*KU Leuven, Instituut voor Kern- en Stralingsfysica, 3001 Leuven, Belgium*⁶*Johannes-Gutenberg Universität Mainz, Institut für Kernchemie, 55128 Mainz, Germany*

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Long-lived isotopes of plutonium were studied using two complementary techniques, high-resolution resonance ionization spectroscopy (HR-RIS) and collinear laser spectroscopy (CLS). Isotope shifts have been measured on the $5f^67s^2\ ^7F_0 \rightarrow 5f^56d^27s\ (J = 1)$ and $5f^67s^2\ ^7F_1 \rightarrow 5f^67s7p\ (J = 2)$ atomic transitions using the HR-RIS method and the hyperfine factors have been extracted for the odd mass nuclei $^{239,241}\text{Pu}$. CLS was performed on the $5f^67s\ ^8F_{1/2} \rightarrow J = 1/2\ (27\,523.61\ \text{cm}^{-1})$ ionic transition with the hyperfine A factors measured for ^{239}Pu . Changes in mean-squared charge radii have been extracted and show a good agreement with previous nonoptical methods, with an uncertainty improvement by approximately one order of magnitude. Plutonium represents the heaviest element studied to date using collinear laser spectroscopy.

DOI: [10.1103/PhysRevA.95.032506](https://doi.org/10.1103/PhysRevA.95.032506)**I. INTRODUCTION**

Laser spectroscopy is an established technique at radioactive ion-beam (RIB) facilities for the study of nuclear shape, size, moments, and spins of short-lived radioactive nuclei [1,2]. Thus far, the heaviest isotopic chain for which nuclear moments and mean-squared charge radii have been extracted from on-line experiments is that of Ra ($Z = 88$) [3], above which lie the actinide elements covering a range from Ac ($Z = 89$) to Lr ($Z = 103$). Such elements are not available at on-line isotope separator facilities and can only be produced via fusion reactions in heavy-ion collisions or transfer reactions using radioactive targets or, for the study of long-lived isotopes of transuranium elements, bred in sufficient quantities in nuclear reactors and safely transported to facilities equipped for the study of nuclear structure. The combination of low production cross sections, the lack of stable isotopes, and correspondingly only a limited number of reliably determined optical transitions available from literature add to the challenge of performing laser spectroscopy on these heaviest elements. Due to the scarcity of ground-state nuclear structure information in this region of the nuclear chart, efforts are under way to develop suitable techniques which provide the required sensitivity to efficiently make use of the limited quantity of isotopes which can be produced [4–6].

Current studies at RIB facilities predominantly use two main techniques of optical spectroscopy. The first, collinear laser spectroscopy, has been applied in a number of variants to the majority of elements, possessing a high resolution

which routinely provides measurements of optical frequency splittings to 1–10-MHz precision, and a high sensitivity, with minimum fluxes of ~ 100 particles per second quoted for systems with hyperfine structure [7], even lower for even-even isotopes. The second, resonance ionization spectroscopy (RIS), has been successfully applied directly within the ion source [8] allowing the study of even more exotic nuclei, with minimum half-lives approaching ~ 1 ms and with spectroscopic information extracted from fluxes of below one ion per second [9].

The disadvantage of the in-source RIS method arises from the effect of the different broadening mechanisms which limits the resolution to typically a few GHz. It remains a challenge to analyze lower-resolution RIS spectra which exhibit either fully or partially overlapping hyperfine structures and to reliably assign systematic uncertainties to such measurements. Nevertheless, the complementarity of both spectroscopic methods has been demonstrated in recent studies of the nuclear structure of exotic Cu isotopes, where the lower-resolution in-source RIS method was often used to greatly reduce the scanning range for high-resolution collinear laser spectroscopy [10–15].

In recent years, in-source spectroscopy has improved with the development of advanced cavity designs for pulsed lasers. These new resonators combine the features of high output powers required for the saturation of atomic transitions in the resonant ionization process, as well as a reduction in the laser linewidth permitting a higher spectroscopic resolution for studies of isotope shifts and hyperfine structures. A ring design of a Ti:sapphire laser cavity developed at the University of Mainz resulted in output powers of up to 1 W in single-mode operation, with a laser linewidth of below 50 MHz [16]. Injection-locked systems on the basis of a similar ring cavity Ti:sapphire laser have demonstrated linewidths of pulsed high-repetition-rate radiation of below 20 MHz, while maintaining an impressive output power in the range of a few Watts [17,18].

In this work, a new programme of heavy element research at the IGISOL facility in the Accelerator Laboratory of the

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University of Jyväskylä was initiated in collaboration with the Institut für Physik, Johannes-Gutenberg Universität, Mainz, Germany. Plutonium ($Z = 94$) was chosen to be a suitable candidate having a number of long-lived isotopes, $^{238-244}\text{Pu}$, for which sufficiently large sample sizes (ng) have been supplied by the Institut für Kernchemie, Mainz, for studies both in Mainz and at Jyväskylä. Earlier optical emission studies of Pu include a measurement of the isotope shift for $^{239-240}\text{Pu}$ with modest resolution in a number of atomic levels and transition lines [19], whereas for a larger set of isotopes, $^{238-242}\text{Pu}$, the shift was determined with a precision of approximately 100 MHz in selected levels in neutral Pu [20]. Motivated by trace analysis applications [21,22], resonance ionization has been applied to quantify the plutonium amount in environmental samples. To enable isotope selectivity in these studies, RIS was used in combination with a time-of-flight mass spectrometer to resolve the isotope shifts in $^{238-242,244}\text{Pu}$ [23] to a precision of about 600 MHz, with later refinements using narrow linewidth continuous-wave lasers resulting in a precision of 15–30 MHz for $^{239,240,242,244}\text{Pu}$ [24].

The focus of the current paper is the comparison of the experimental techniques of collinear laser spectroscopy and high-resolution RIS in the actinide region. A measurement of optical isotope shifts in Pu has been performed on three transitions, two atomic transitions using an injection-locked pulsed laser system at Mainz and an ionic transition via collinear laser spectroscopy in Jyväskylä. The King plot method [25] is used to extract changes in mean-squared charge radii in order to assess the accuracy of both techniques. Establishing a good agreement is of importance such that either method can be used in the future to explore the properties of heavier actinides or lighter refractory elements which have thus far been challenging to access.

The paper is structured as follows. In Sec. II details of the two techniques are presented. The results and data analysis for the two experiments are presented in Sec. III, with the extraction of changes in mean-squared charge radii in Sec. IV. Section V contains a discussion of the systematic errors assigned to both techniques. The final conclusions are drawn in Sec. VI.

II. EXPERIMENTAL TECHNIQUE

As this work utilizes two very different laser spectroscopic techniques, resonance ionization spectroscopy using pulsed lasers and collinear laser spectroscopy using a continuous-wave laser, both techniques are described separately.

A. High-resolution resonance ionization spectroscopy

High-resolution resonance ionization spectroscopy (HR-RIS) was performed using a Ti:sapphire laser system composed of one conventional 10-kHz high-repetition-rate laser together with a dedicated injection-locked Ti:sapphire laser [18] which ensured a specifically narrow bandwidth. These were operated at the Mainz Atomic Beam Unit (MABU) which comprises a quadrupole mass filter (QMF), as schematically depicted in Fig. 1(a) [26]. A well-collimated atomic beam was formed by resistively heating a graphite oven to approximately 1300 K. In order to reduce the large Doppler broadening due

to the thermal velocity distribution of the atomic ensemble expected in co-/counter-propagating laser irradiation, the laser beam from the injection-locked Ti:sapphire laser was introduced in a perpendicular geometry to the effusing atomic beam and expanded to generate a uniform intensity distribution within the interaction volume. The ionization laser was introduced counterpropagating to the atomic beam and focused to a spot size comparable to the oven dimension with an inner diameter of 2 mm. Following resonant ionization, the ion beam was shaped and deflected by 90° in a quadrupole deflector to enter the QMF (mass resolving power $M/\Delta M \sim 200$) and subsequently detected using a channeltron electron multiplier operating in single-ion counting mode. Due to the pulsed nature of the lasers, a time-gating method was employed to minimize the background from surface ions.

The ring cavity Ti:sapphire laser was injection locked to an external cavity diode laser (ECDL) via a single-mode optical fiber providing 5–20-mW seed input. The spectral linewidth of the Ti:sapphire laser was analyzed with a commercial scanning Fabry-Pérot interferometer (FPI) with a free spectral range (FSR) of 300 MHz, resulting in a measured linewidth of 13.4(8) MHz. This may be compared with the measured linewidth of the master (ECDL) laser of 10.1(2) MHz. The ECDL was stabilized via a quadrature interferometer (ISCAN, TEM MESSTECHNIK) for fast frequency control in combination with fringe-offset locking for long-term stability [28]. By locking to a confocal FPI (FSR = 299.782(5) MHz) and using a frequency-stabilized HeNe laser as reference, a frequency calibration of better than 1 MHz could be attained. The frequency of the injection-locked laser was scanned in a stepwise manner by driving the ECDL to fixed setpoints. Data acquisition of the ion signal took place whenever the ECDL laser frequency was within a ± 5 -MHz locking interval of the setpoint.

Spectroscopy on neutral Pu was performed on two different atomic transitions illustrated in Fig. 1(b). The first transition at 385.210 nm proceeds from the atomic ground state ($J = 0$) to an excited state at $25\,959.849\text{ cm}^{-1}$ ($J = 1$), whereas the second transition at 387.965 nm proceeds from a thermally populated state at 2203.606 cm^{-1} ($J = 1$) to a level at $27\,929.161\text{ cm}^{-1}$ ($J = 2$). At an oven temperature of ~ 1300 K the metastable state is expected to have a 20% population with respect to the ground state. The wavelengths were obtained by single-pass frequency doubling of the laser radiation from the injection-locked Ti:sapphire laser using a β -barium borate (BBO) nonlinear crystal. The ionization step for both transitions proceeded via auto-ionizing states above the ionization potential (IP) and was provided by an intracavity frequency doubled broadband Ti:sapphire laser with a fundamental linewidth of approximately 4–5 GHz. Typical laser powers available for the ionization step were up to 1 W. Lower laser powers of the order of 2–10 mW were used for the spectroscopy step to minimize saturation broadening.

B. Collinear laser spectroscopy

Collinear laser spectroscopy (CLS) was performed at the IGISOL facility of the Accelerator Laboratory at the University of Jyväskylä. Samples containing Pu isotopes ($^{238-242,244}\text{Pu}$) were electrolytically deposited onto a tantalum substrate which

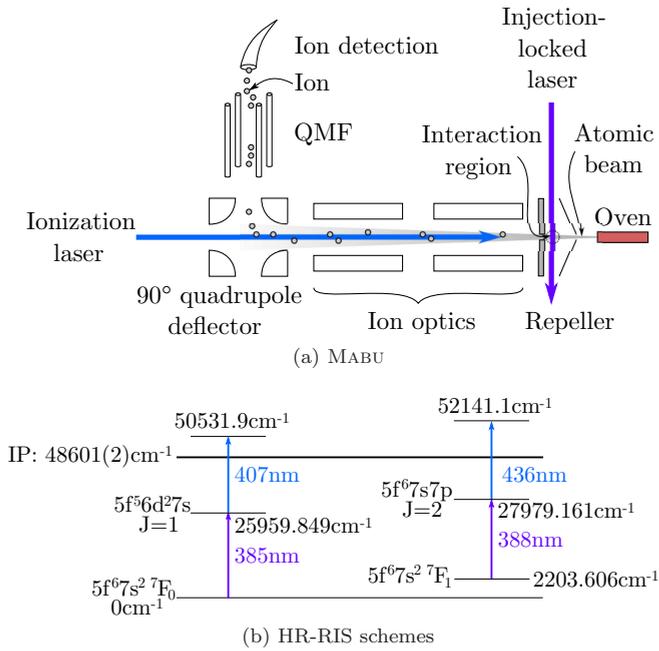


FIG. 1. Experimental setup at Mainz. (a) Schematic depiction of the MABU QMF system; see text for details. (b) Optical scheme used for HR-RIS. The wavelength of the first step was scanned. Data for level configurations and energies taken from [19,27].

was electrothermally heated inside a gas cell filled with helium. The Pu atoms were selectively ionized via two-step resonant laser ionization utilizing two intracavity frequency doubled, broadband Ti:sapphire lasers operating at a repetition rate of 10 kHz and a linewidth of ~ 100 GHz. Further details concerning the gas cell designed for such heavy element studies as well as the in-gas-cell resonant laser ionization process have been published elsewhere [29].

The ions were extracted from the gas cell via gas flow, guided through a sextupole ion guide [30] and accelerated to 30 keV towards a mass separator with a typical resolving power $M/\Delta M \sim 350$. Following mass separation, a continuous ion beam of a single A/q was injected into a gas-filled radio-frequency Paul trap (RFQ) for cooling and bunching [31]. The use of an RFQ in conjunction with collinear laser

spectroscopy was pioneered at the IGISOL facility in order to suppress the laser-scattered background by gating the data acquisition with respect to the arrival of an ion bunch at the light collection region [32]. The bunched ion beam was overlapped in a collinear geometry with a counterpropagating laser beam. A scanning voltage applied to the light collection region Doppler shifted the ions into resonance with the laser light and the resulting fluorescent photons were imaged and detected on a photomultiplier tube. A schematic diagram of the collinear laser spectroscopy beamline is given in Fig. 2. The tantalum filaments were heated to a temperature of approximately 1300–1500 K, depending on the abundance of the isotope of interest to be evaporated from the filament, such that a Pu⁺ ion yield of approximately 30 000/s were detected on a set of microchannel plates at the end of the collinear laser spectroscopy beamline.

Laser spectroscopy was performed from the PuII ionic ground state on the $5f^6 7s^8 F_{1/2} \rightarrow J=1/2$ ($27\,523.61\text{ cm}^{-1}$) transition [19] at 363.324 nm. The laser light was generated by a Spectra Physics 380D dye laser operating with Pyridine2 dye pumped by a Coherent Verdi V5 diode-pumped solid-state laser at 532 nm. Long-term frequency stabilization was achieved employing a “top-of-fringe” locking to an iodine absorption line with a 3-MHz accuracy. Intracavity frequency doubling using a BBO crystal allowed the generation of up to 0.35 mW UV light which was injected into the beamline through a Brewster window.

III. DATA ANALYSIS AND RESULTS

A. Resonance ionization spectroscopy

The resonance ionization spectra obtained using the two transitions on $^{238-242,244}\text{Pu}$ atoms are shown in Fig. 3. A frequency jitter of the ECDL of typically 5–10 MHz and the nature of the data acquisition selection (± 5 MHz around the setpoint for the fundamental light) led to small shifts of the resonance positions between the two scan directions. In order to consider this effect, the data from scans with increasing and decreasing frequency were summed for the analysis process. The fit results for the hyperfine coefficients and isotope shifts with respect to the reference isotope ^{240}Pu are given in Table I.

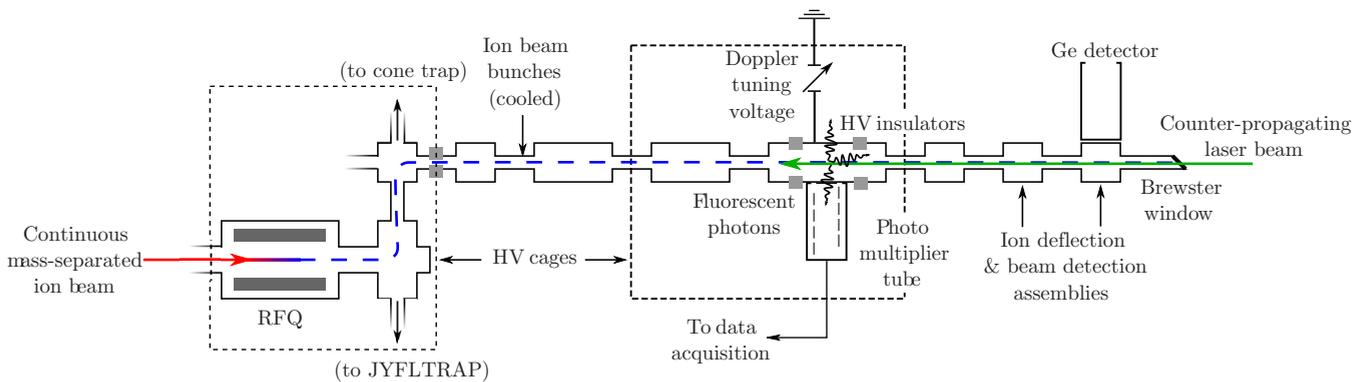


FIG. 2. Schematic diagram of the collinear laser spectroscopy beamline at JYFL. The bunched and cooled ion beam is overlapped with a counterpropagating, narrow linewidth laser beam. A Ge detector may be used for the detection of gamma rays emitted following the decay of a radioactive species and is often used for ion-beam identification during initial tuning.

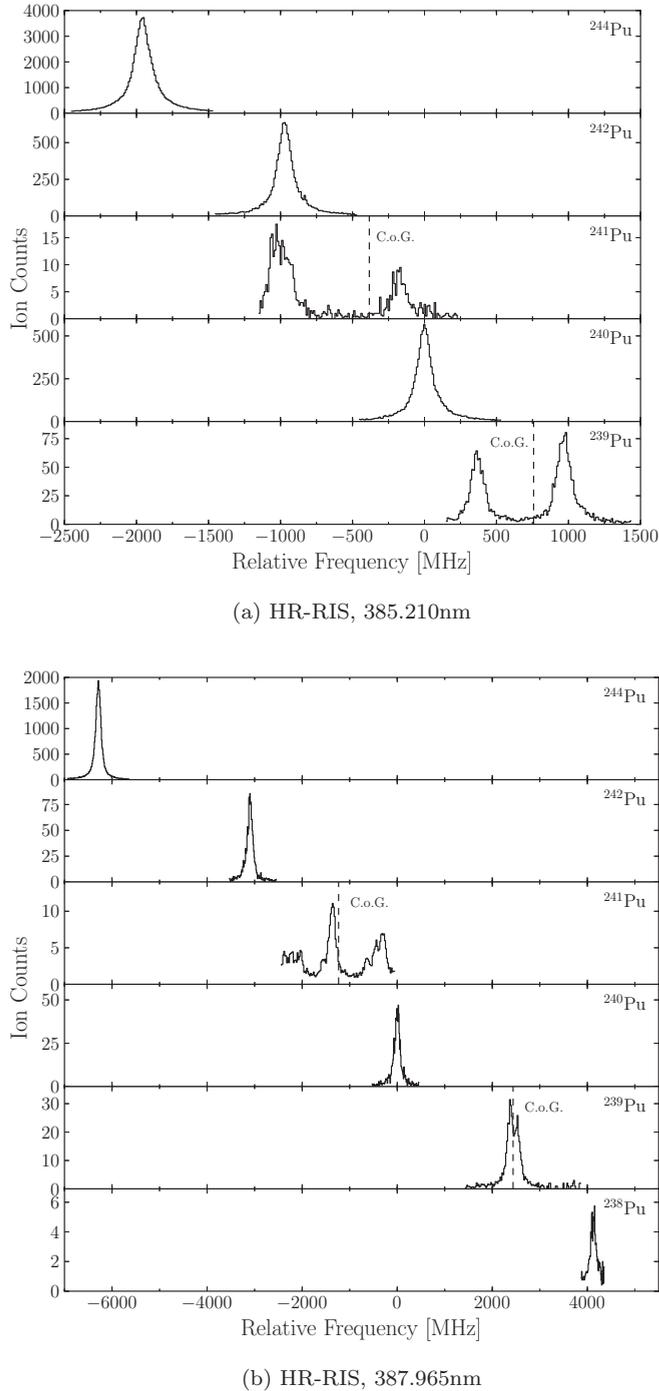


FIG. 3. High-resolution resonance ionization spectra using the injection-locked Ti:sapphire laser for the two transitions investigated.

The data were fitted with a Voigt line shape whereby the Gaussian component was considerably smaller than the Lorentzian component. The oven temperature was adjusted to optimize the release of the isotope of interest, which in turn may provide a different Gaussian contribution to the linewidth of each isotope. Free parameters in the fit were the background, the line shape [full width at half maximum (FWHM), Gaussian, and Lorentzian contributions], the peak intensities and its centroid, as well as hyperfine parameters where applicable. For each isotope, one line shape was

assumed for all resonances. The FWHM of the resonances varied from 100–150 MHz, of which approximately 20% was attributable to the Gaussian component. With respect to the hyperfine parameters, some additional constraints were included in the fitting procedure as outlined in the following. An example fit of the ^{241}Pu spectrum for the 387.965-nm atomic transition is given in Fig. 4(b) using free intensities to show the close correspondence of the fitted spectrum with regards to the experimental error bars.

In the metastable transition at 387.965 nm, the peaks for the $F = 7/2 \rightarrow F' = 7/2$ and $7/2 \rightarrow F' = 9/2$ hyperfine transitions [see Fig. 4(a) for an expanded level scheme] overlap closely in the ^{241}Pu hyperfine spectrum. The relative intensities for these peaks were therefore fixed to the theoretical value of the corresponding Racah coefficients in the fit. Since the hyperfine A coefficient of the lower state is close to and consistent with zero, as determined from the ^{241}Pu spectrum, it was kept fixed at zero for the evaluation of the collapsed hyperfine structure in ^{239}Pu .

The atomic ground state exhibits no splitting due to a spin $J = 0$. Additionally, ^{238}Pu was not observed using the 385.210-nm transition, which may indicate that despite a higher thermal population in the atomic ground state the ionization scheme starting from the metastable state was more efficient. As the MABU was optimized for high transmission, the obtained mass resolving power of the QMF was not sufficient to fully discriminate between the Pu isotopes and thus the more abundant ^{242}Pu was also present in scans of the hyperfine structure of ^{241}Pu . Since the hyperfine component of lowest frequency overlaps with the resonance of ^{242}Pu , the extraction of the isotope shift was more demanding. It was also noticed during the data analysis that the third component of the ^{241}Pu hyperfine spectrum of highest frequency was missed during the laser scans. By using the ratio of field shifts between the two transitions for the even isotopes, the hyperfine structure centroid of ^{241}Pu for the ground-state transition can be estimated as

$$\delta\nu_{385}^{240,241} = \frac{F_{385}}{F_{388}} \times \delta\nu_{388}^{240,241}, \quad (1)$$

where $F_{385}/F_{388} = 0.309(7)$ from a King plot. Included in the fitting of ^{241}Pu were the contributions from the abundant ^{242}Pu mass peak as well as a weaker ^{240}Pu component using the independently determined centroid positions.

B. Collinear laser spectroscopy

As the iodine absorption line at ~ 727 nm used to stabilize the dye laser is untabulated, the laser frequency had to be calculated from the resonance spectra of ^{240}Pu wherefore the transition frequency ν_{tran} is known [19]. This was accomplished by fitting the raw data of fluorescent photons versus DAQ channel number. The resonance channel number x and the nonrelativistic equation for a frequency offset $\Delta\nu$ for counterpropagating laser beams,

$$\Delta\nu = \nu_{\text{laser}} \left(1 + \frac{v}{c} \right) - \nu_{\text{tran}} \quad (2a)$$

$$= \nu_{\text{laser}} \left(1 + \sqrt{\frac{2[eV_{\text{RFQ}} - (mx + b)]}{m_{\text{ion}}c^2}} \right) - \nu_{\text{tran}}, \quad (2b)$$

TABLE I. Overview of the extracted hyperfine parameters and isotope shifts $\delta\nu^{240,A}$ (all in MHz) for the two HR-RIS transitions studied in this work. Empty fields indicate that the corresponding parameter cannot be determined due to the nuclear spin I . Statistical uncertainties arising from fits to the data are denoted by parentheses whereas systematic uncertainties are given in square brackets (see Sec. V A). The term {ref} for ^{240}Pu indicates the reference nature of this isotope. Uncertainties arising from the determination of its resonance centroid amount to 3.0 MHz and have been folded into the isotope shifts for the other isotopes.

Isotope	I	385.210 nm			387.965 nm				
		$\delta\nu^{240,A}$	A_{upper}	B_{upper}	$\delta\nu^{240,A}$	A_{lower}	A_{upper}	B_{lower}	B_{upper}
^{244}Pu	0	-1955.2(55)[80]			-6288.1(60)[80]				
^{242}Pu	0	-969.4(54)[80]			-3099.3(90)[80]				
^{241}Pu	5/2	-379.5(117)[80] ^a	-278.1(56)	+100.8(180)	-1228.3(120)[80]	-2.2(48)	+37.7(34)	+1058.6(82)	-175.4(143)
^{240}Pu	0	0.0{ref}			0.0{ref}				
^{239}Pu	1/2	+757.8(60)[80]	+402.3(32)		+2438.7(120)[80]	0 ^b	-62.6(33)		
^{238}Pu	0	Not studied using this transition			+4126.7(130)[80]				

^aNot an independent measurement. See text for details.

^bFixed parameter. See text for details.

where V_{RFQ} is the bias voltage of the RFQ and m and b are the slope and intercept calibration parameters of the scanning voltage, were used. For the reference isotope ^{240}Pu , $\Delta\nu = 0$ on resonance.

The collinear laser spectroscopic work was performed on singly ionized species and thus a correction to the atomic masses m_{atom} from [33] has been included to account for the

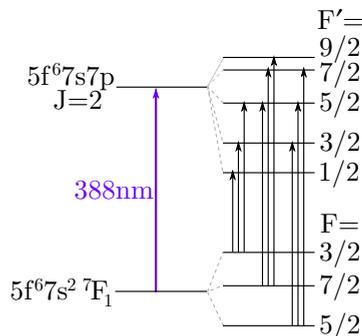
mass difference due to the missing electron. Here,

$$m_{\text{ion}} = m_{\text{atom}} - m_{\text{electron}} + m_{\text{IP}}, \quad (3)$$

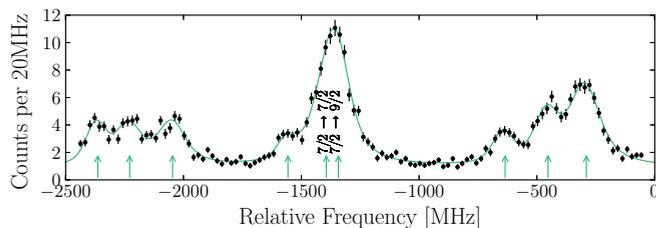
where m_{electron} was taken from [34] and m_{IP} represents the ionization potential converted into mass units from [27]. The effect of the latter is negligible, however, has been included in Eq. (3) for completeness. The calculated ionic masses used for evaluation of the optical spectra are tabulated in Table II.

The corresponding wave number of the ring dye laser was determined to be $\bar{\lambda}_{\text{laser}} = 13\,754.625\text{ cm}^{-1}$ from the weighted mean of all ^{240}Pu scans taking into account the frequency doubling. Any statistical errors related to the fits of the optical spectrum do not contribute at this scale. The fractional systematic uncertainty of the voltages due to the readback of the RFQ and scanning voltage of the light collection region corresponds to 0.1% [35]. The effect of a systematic uncertainty arising due to the voltage readback is considered to be $\sim 0.0035\text{ cm}^{-1}$. An uncertainty for the transition wave number $\bar{\lambda}_{\text{transition}}$ is not given in the literature [19]; however, it is assumed to be 0.01 cm^{-1} . The uncertainty of $\bar{\lambda}_{\text{laser}}$ is dominated by the uncertainty of $\bar{\lambda}_{\text{transition}}$. An overall systematic uncertainty of 0.01 cm^{-1} for $\bar{\lambda}_{\text{laser}}$ is therefore assumed.

The optical fluorescence spectra of singly charged $^{244,242,240,239}\text{Pu}$ ions measured in this work are shown in Fig. 5. A purely Lorentzian line shape was used in the data analysis reflecting a zero Gaussian contribution to the spectra. This can be expected when using cooled ion beams in which the energy spread is typically $< 0.6\text{ eV}$ [36]. The fit parameters included the background, the FWHM of the resonance, the



(a) Hyperfine level diagram



(b) Hyperfine spectrum

FIG. 4. Expanded hyperfine level diagram and example fit for the $5f^6 7s^2 \text{}^7F_1 \rightarrow 5f^6 7s \text{}^7P_2$ ($J = 2$) (387.965 nm) HR-RIS transition for ^{241}Pu ($I = 5/2$). Allowed transitions are indicated by arrows in the level diagram. A hyperfine structure fit with free intensities is included as the solid line to highlight the quality of the fit with respect to the small error bars on the data points. The locations of the hyperfine transitions are indicated by arrows with those labeled corresponding to the unresolved transitions.

TABLE II. Comparison of the atomic masses from [34] and the ionic masses used in this work.

A	m_{atom} (amu)	m_{ion} (amu)
244	244.064 205 26(557)	244.063 656 69(557)
242	242.058 742 81(196)	242.058 194 24(196)
240	240.053 813 75(192)	240.053 265 18(192)
239	239.052 163 59(192)	239.051 615 02(192)

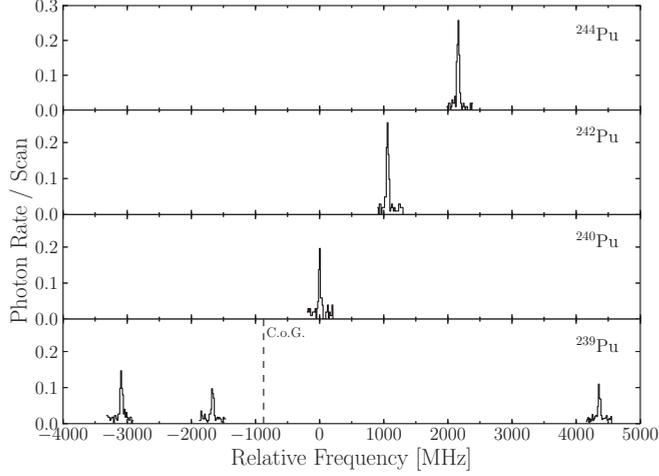


FIG. 5. Optical fluorescence spectra for $^{244,242,240,239}\text{Pu}^+$ isotopes determined by collinear laser spectroscopy on the $^8F_{1/2} \rightarrow J = 1/2$ (363.324 nm) ionic transition. The center of gravity (C.o.G.) in ^{239}Pu is marked as a vertical dashed line.

centroid, and the intensity of the resonance for the $I = 0$ isotopes. The FWHM of the resonances was ~ 30 MHz for all isotopes. For isotopes with a nonzero nuclear spin, the hyperfine A coefficients of the atomic ground and excited states were allowed to vary and the FWHM of all resonances was constrained to be common. An example of such a fit is shown in Fig. 6. The hyperfine structure of ^{239}Pu was fitted with free intensities with the relative intensities from the best-fit parameters corresponding to those from weak-field coupling estimates (“Racah intensities”). Due to the choice of optical transition, $J = 1/2 \rightarrow J' = 1/2$, there is no sensitivity

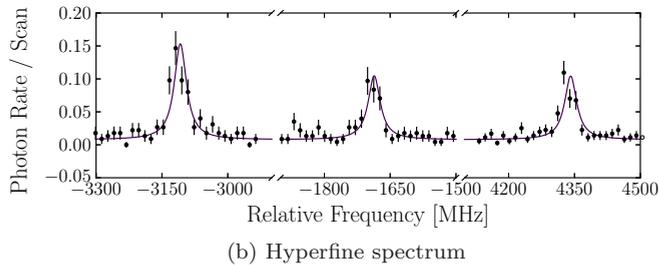
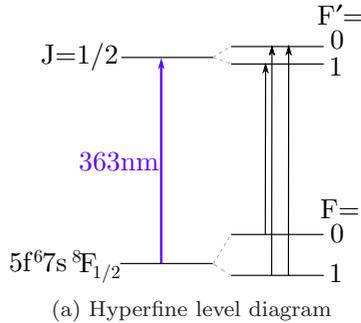


FIG. 6. Hyperfine level diagram and example fit for the $5f^6 7s \ ^8F_{1/2} \rightarrow J = 1/2$ (363.324 nm) CLS transition for $^{239}\text{Pu}^+$ ($I = 1/2$). A hyperfine structure fit with free intensities is shown as the solid line together with statistical error bars on the data points.

TABLE III. Summary of the extracted hyperfine A parameters and isotope shifts $\delta\nu^{240,A}$ (all in MHz) for the collinear laser spectroscopy work on the 363-nm ionic transition. Statistical uncertainties arising from hyperfine structure fits to the data are denoted by parentheses whereas systematic uncertainties (see Sec. VB) due to the conversion from scanning voltages into frequencies are given in square brackets.

Isotope	I	$\delta\nu^{240,A}$	A_{lower}	A_{upper}
^{244}Pu	0	+2160.6(48)[25]		
^{242}Pu	0	+1056.3(42)[12]		
^{240}Pu	0	0.0{ref}		
^{239}Pu	1/2	-872.7(55)[9]	+7445.5(32)	-1421.0(37)

to the electric quadrupole moments. The extracted parameters and isotope shifts with respect to ^{240}Pu are summarized in Table III.

IV. COMPARISON OF TECHNIQUES USING THE KING PLOT METHOD

Information on the changes in mean-squared charge radii between nuclei with atomic masses A and A' may be extracted from optical isotope shifts, $\delta\nu$, as

$$\delta\nu^{A',A} = \nu^A - \nu^{A'} \quad (4)$$

$$= \left(\frac{1}{m_{A'}} - \frac{1}{m_A} \right) M + F K(Z) \delta\langle r^2 \rangle^{A',A}. \quad (5)$$

Here, M and F are the transition-dependent atomic factors for the mass and field shift, respectively. $K(Z)$ is an element-dependent factor to correct for higher-order (Seltzer) moments which contribute a few percent in heavier nuclei [37,38]. The atomic factors are to be determined either theoretically or empirically through the King plot technique [25,39].

The King plot allows a direct determination of the atomic mass and field shift factors by examining optical isotope shifts either with respect to changes in mean-squared charge radii obtained from nonoptical methods, $\delta\langle r^2 \rangle$, or via a transfer of known atomic factor information from one transition to another provided that each isotope pair has been studied using at least two different transitions. Multiplying Eq. (5) with a modification factor κ ,

$$\kappa^{A,A'} = \frac{m_A m_{A'}}{m_A - m_{A'}} \times \frac{m_{A_{\text{ref}}} - m_{A'_{\text{ref}}}}{m_{A_{\text{ref}}} m_{A'_{\text{ref}}}}, \quad (6)$$

removes the dependence of nuclear masses and includes a standard reference pair $A_{\text{ref}} = 244$ and $A'_{\text{ref}} = 240$ for presentation purposes. The modified isotope shifts are then written as

$$\kappa^{A,A'} \delta\nu_i^{A',A} = \frac{m_{244} - m_{240}}{m_{244} m_{240}} \times M_i + F_i K(Z) \kappa^{A,A'} \delta\langle r^2 \rangle^{A',A}, \quad (7)$$

where i (and likewise for j) denotes the transition. The modified isotope shifts of two optical transitions i and j may be plotted against each other and should yield a straight line with the atomic factor information contained in the gradient

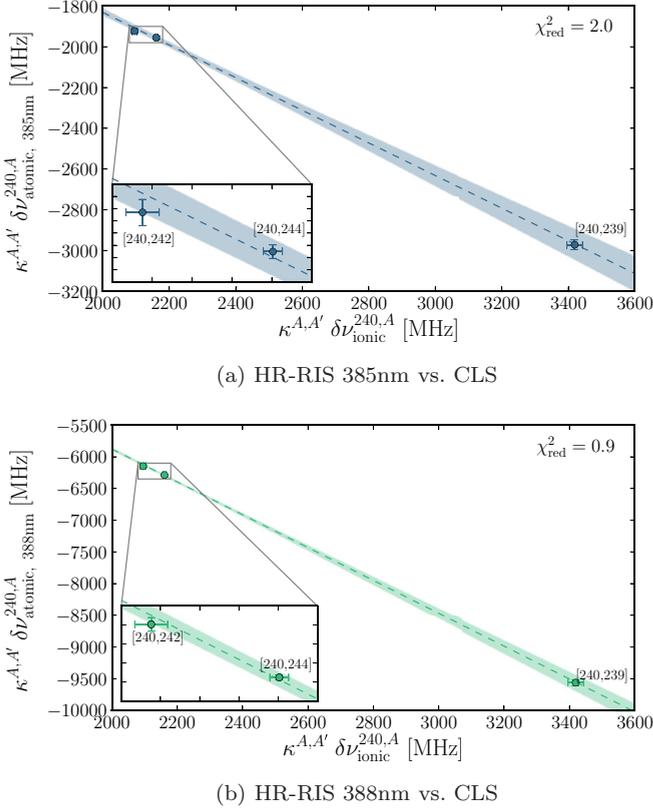


FIG. 7. King plots of the (a) 385.210-nm and (b) 387.965-nm HR-RIS atomic isotope shifts vs the ionic isotope shifts from CLS. The error bars are within the data points. The dashed lines denote the straight lines of best fit. The 68% (1σ) confidence bands are included as the shaded areas.

and intercept:

$$\kappa^{A,A'} \delta\nu_i^{A',A} = \frac{F_i}{F_j} \kappa^{A,A'} \delta\nu_j^{A',A} + \frac{m_{244} - m_{240}}{m_{244}m_{240}} \times \left(M_i - \frac{F_i}{F_j} M_j \right). \quad (8)$$

A plot of the atomic isotope shifts determined by the HR-RIS method compared with the ionic shifts from collinear laser spectroscopy is shown in Fig. 7. This serves as a consistency check of the measurements using the two techniques. The field shift ratio $F_{\text{atomic}}/F_{\text{ionic}}$ is $-0.799(39)$ for the ground-state atomic 385.210-nm transition and $-2.588(69)$ for the atomic metastable 387.965-nm transition. As expected for heavy elements, the y axis intercepts related to the mass shifts M are small, $-232(86)$ and $-701(151)$ MHz, respectively.

Absolute charge radii for $^{239,240,242}\text{Pu}$ have been determined from x-ray studies of muonic atoms [40]. Plotting the modified isotope shifts $\delta\nu^{240,A}$ against the changes in mean-squared charge radii $\delta\langle r^2 \rangle^{240,A}$ allows for a direct evaluation of the atomic factors (see Fig. 8 for all transitions in this work). As a fit curve a linear fit through the origin (assuming a negligible mass shift) was used to determine the effective field shift gradients $F_{\text{eff}} = F \times K(Z)$. The assumption of $M = 0$ is based on experimental work in Th [41] where the intercept was consistent with zero. Theoretical work carried out for

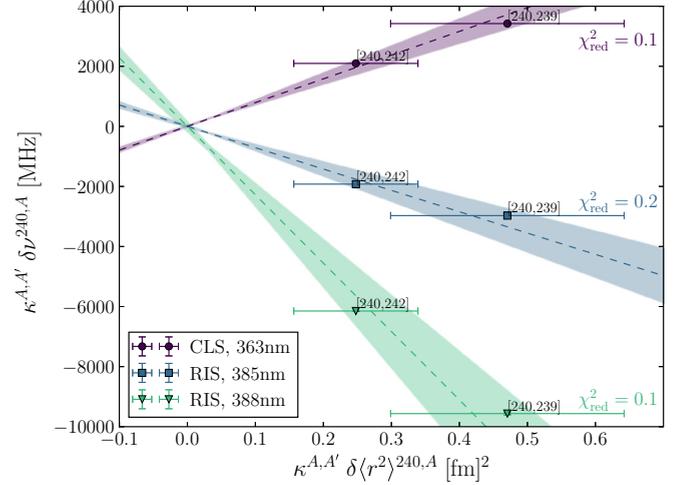


FIG. 8. King plots of the isotope shifts of all transitions in this work vs changes in mean-squared charge radii evaluated from muonic x-ray measurements [40]. The error bars for $\kappa^{A,A'} \delta\nu^{240,A}$ lie within the data points. The best fits are shown as the dashed lines with the 68% confidence bands included as the shaded areas.

Fr indicates that the absence of a mass shift contribution causes an uncertainty of $\sim 1\%$ in the extracted $\delta\langle r^2 \rangle$ [42]. The effective field shifts for the HR-RIS transitions were determined to be $F_{\text{eff}, 385\text{nm}} = -7.1(7)$ GHz/fm 2 and $F_{\text{eff}, 388\text{nm}} = -22.8(23)$ GHz/fm 2 from linear fits to the King Plot. The value for the effective field shift factor for the ionic collinear transition was extracted as $F_{\text{eff}, 363\text{nm}} = +7.9(6)$ GHz/fm 2 . The negative F factors reflect a decrease in s -electron density when promoting one electron from either the atomic ground state or metastable state to the excited state, as expected from the atomic configuration. In contrast, the positive F factor in the transition in Pu^+ indicates an increase of the electron density at the nucleus agreeing with the assumption of one f -electron being transferred to an orbital with lower angular momentum.

The extracted changes in mean-squared charge radii are presented in Table IV. Both spectroscopic techniques, collinear laser spectroscopy with fluorescence detection and high-resolution resonance ionization spectroscopy utilizing a narrow linewidth injection-locked laser, provide values for $\delta\langle r^2 \rangle^{240,A}$ with similar sized statistical uncertainties of $\sim 5 \times 10^{-4}$ fm 2 . Systematic uncertainties arising from the F_{eff} factors are of the order of 10% of $\delta\langle r^2 \rangle^{240,A}$ and therefore dominate any other uncertainties. A graphical comparison is given in Fig. 9. The extracted values for $\delta\langle r^2 \rangle^{240,A}$ from the optical isotope shifts in this work are consistent with those from muonic x-ray measurements [40]; however, they have uncertainties approximately one order of magnitude smaller when only comparing statistical uncertainties. A comparison of $\delta\langle r^2 \rangle^{240,A}$ with respect to the average change in mean-squared charge radius per isotope is provided in the bottom panel of Fig. 9. The relative change in relation to the average is defined as

$$\Delta = \frac{1}{N} \left(\sum_i^N \delta\langle r^2 \rangle_i^{240,A} \right) - \delta\langle r^2 \rangle_j^{240,A}, \quad (9)$$

TABLE IV. Changes in mean-squared charge radii $\delta\langle r^2 \rangle^{240,A}$ determined from optical work for all investigated transitions. The uncertainties in parentheses are statistical. Contributions from systematic uncertainties on the isotope shifts are denoted by square brackets; contributions arising from the effective field shift factors F_{eff} are given in curly brackets (see Sec. V for details). Literature values are included for comparison [40,43].

Transition	F_{eff} (GHz/fm ²)	$\delta\langle r^2 \rangle^{240,A}$ (fm ²)				
		238	239	241	242	244
385 nm Pu I	-7.1(7)		-0.1067(9)[11]{105}	+0.0538(14)[11]{52}	+0.1365(8)[11]{134}	+0.2754(8)[11]{271}
388 nm Pu I	-22.8(22)	-0.1810(5)[3]{174}	-0.1070(5)[3]{103}	+0.0565(4)[3]{51}	+0.1359(4)[3]{131}	+0.2758(2)[3]{266}
363 nm Pu II	+7.9(5)		-0.1105(7)[1]{69}		+0.1337(5)[1]{84}	+0.2735(6)[3]{173}
Muonic x rays [40]			-0.120(66)		+0.125(68)	
Literature [43]		-0.204(5)	-0.122(3)	+0.054(5)	+0.151(5)	+0.304(8)

where the summation runs over all transitions i studied in this work, N reflects the number of transitions studying a particular isotope, and j refers to the transition of interest.

A deviation in $\delta\langle r^2 \rangle^{240,A}$ values compared to [43] might partially be explained by different assumptions of the mass shift constant M . In this work, $M = 0$ was used for all three

investigated transitions. The arc discharge spectra of Pu [44] were evaluated in [43] against the muonic x-ray data from [40] using $M = +391$ GHz u assuming an alkali-like transition. For comparison, $\delta\langle r^2 \rangle^{240,A}$ from [43] were plotted against Δ obtained from the three optical transitions to highlight the influence of the atomic factors on $\delta\langle r^2 \rangle$ as indicated in the middle panel of Fig. 9.

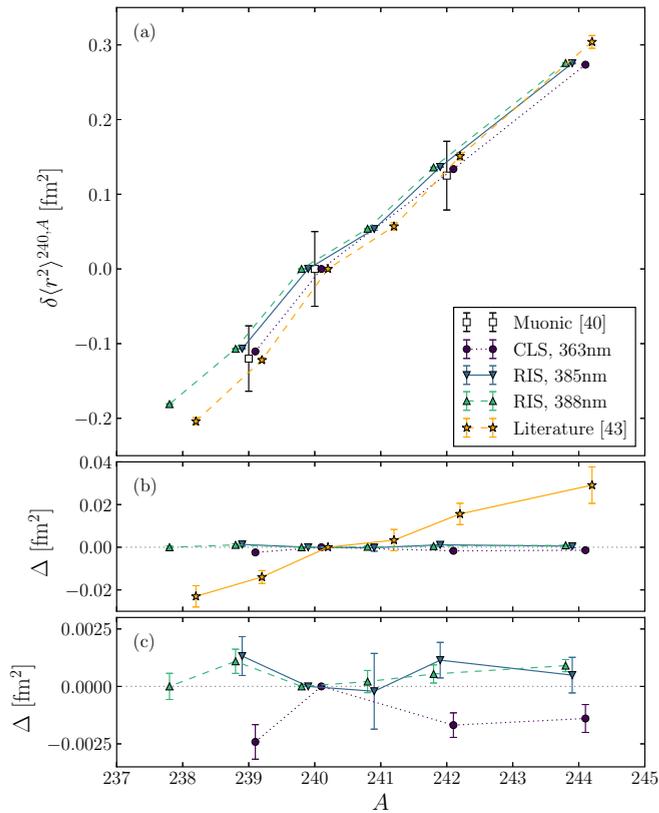


FIG. 9. (a) Changes in mean-squared charge radii extracted from optical isotope shifts in this work with respect to ^{240}Pu and compared with literature values from [40,43]. A small horizontal offset was included for display purposes. The error bars for this work lie within the data points. (b) The middle panel highlights the relative change in $\delta\langle r^2 \rangle$ for the optical work from Table IV with respect to the average change in mean-squared charge radius for each isotope as obtained from this work; see text for details. (c) In the lower panel, a zoom of the middle panel is provided without [43].

V. SYSTEMATIC ERROR BUDGET

As the statistical uncertainties on the isotope shifts (and therefore also for the extracted changes in mean-squared charge radii) are comparably small for both the HR-RIS and CLS techniques, a further investigation of systematic uncertainties was considered. These are of experimental nature and arise from the conversion of some detected variable to frequency changes. Naturally, the frequency conversion mechanisms differ for both methods but nevertheless can independently introduce uncertainties on the isotope shifts. These will directly affect the extracted $\delta\langle r^2 \rangle$; however, slight changes in the King plots are also expected. For the sake of the arguments presented in this section, the previously mentioned values for the atomic factors will be used.

In addition, the influence of atomic factors is also shortly discussed as those also directly affect the extraction of mean-squared charge radii.

A. Resonance ionization spectroscopy

For the resonance ionization studies, the master ECDL laser was stabilized against long-term drifts via a scanning Fabry-Pérot interferometer to a frequency stabilized HeNe laser. By sequentially changing the lockpoint of the master laser, the frequency of the injection-locked laser was scanned over a 10-GHz frequency range in total. The change in frequency of the master/slave laser was then determined to be $\Delta\nu = N \times \text{FSR}_{\text{FPI}} \times \lambda_{\text{HeNe}}/\lambda_{\text{master}}$ where N is the number of FSRs scanned over, a maximum of 41 for the 10-GHz scan range. Combining this with the uncertainty of the FSR, this results in a negligible effect of 0.1 MHz on the frequency scale.

The scanning of the laser and the setpoint interval of ± 5 MHz (thus ± 10 MHz for frequency-doubled laser light) has significantly more influence. Due to the data acquisition mode of recording data whenever the master laser frequency

had reached the set interval point, an offset in resonance centroids is observed between the two scanning directions of the master laser. This effect has been corrected for by summing the individual spectra together before analysis; however, bias effects may still be present. A systematic uncertainty of ~ 8 MHz is therefore attributed to the isotope shifts.

Accounting for a slight asymmetry in the HR-RIS resonances in the fitting process by implementing an asymmetric Lorentzian contribution in the Voigt profile, the effect on the centroids of the hyperfine structures is of the order of 0.5 MHz. In total, the isotope shifts are affected by less than 1 MHz, being much smaller compared to the contribution from other uncertainties.

$$\begin{aligned} \Delta_{\text{sys}}(\delta v^{240,A}) &= v_{\text{laser}} \sqrt{\frac{e V_{\text{RFQ}}}{2 m_{240} c^2}} \left[\frac{1}{2} \left(\frac{\delta V_{\text{LCR}}}{V_{\text{RFQ}}} + \frac{\delta m}{m_{240}} \right) \underbrace{\frac{\Delta V_{\text{RFQ}}}{V_{\text{RFQ}}}}_{\times 10^{-3}} + \frac{\delta V_{\text{LCR}}}{V_{\text{RFQ}}} \underbrace{\frac{\Delta \delta V_{\text{LCR}}}{\delta V_{\text{LCR}}}}_{\times 10^{-4}} + \frac{\Delta m_{240} + \Delta m_A}{m_{240}} \right] \\ &= v_{\text{laser}} \sqrt{\frac{e V_{\text{RFQ}}}{2 m_{240} c^2}} \left[\frac{1}{2} \left(\frac{\delta V_{\text{LCR}}}{V_{\text{RFQ}}} + \frac{\delta m}{m_{240}} \right) \times 10^{-3} + \frac{\delta V_{\text{LCR}}}{V_{\text{RFQ}}} \times 10^{-4} + \frac{\Delta m_{240} + \Delta m_A}{m_{240}} \right], \end{aligned} \quad (10)$$

with V_{RFQ} being the bias voltage of the RFQ, δV_{LCR} the difference in postacceleration voltage of the light collection region for $A = 240$ and $A = A'$ when on resonance, and $\delta m = |m_A - m_{240}|$ with all masses being the ionic masses and their uncertainties Δm according to Table II. According to [35,36], $\Delta V_{\text{RFQ}}/V_{\text{RFQ}} = 10^{-3}$ and $\Delta \delta V_{\text{LCR}}/\delta V_{\text{LCR}} = 10^{-4}$, respectively. The bias of the RFQ is read out on a scan-by-scan basis via a $1 : 10^4$ resistor stack [36] and its weighted mean is used. In order to obtain $\delta V_{\text{LCR}} = |V_{\text{LCR}}^{240} - V_{\text{LCR}}^A|$, the (hyperfine) spectra were fitted as a function of postacceleration voltage after calibration of the scanning power supply. The absolute errors on δV_{LCR} arising from the linear calibration fit were typically < 0.1 V and therefore consistent with [36]. The calculated systematic uncertainties for the isotope shifts are consistent with zero for the reference isotope ^{240}Pu and increase with increasing or decreasing neutron number, ΔN . The systematic uncertainties obtained for the isotope shifts are transferred to the changes in mean-squared charge radii and have been included in Table IV.

C. Influence of the atomic factors

Atomic factors play an important role in the extraction of changes in mean-squared charge radii such that slight changes in F and/or M can influence $\delta \langle r^2 \rangle$ dramatically. The effective field shift factors as extracted from the slopes of the King plots in Fig. 8 possess an uncertainty of approximately 10%, stemming from the large uncertainty of the muonic x-ray data [40]. As such, a systematic uncertainty of the order of 10% is introduced on the values of $\delta \langle r^2 \rangle$ in Table IV.

In the extraction of $\delta \langle r^2 \rangle^{240,A}$, a zero mass shift contribution was assumed. This leads to the assumption of the specific mass shift constant S being of identical value but opposite in sign to the normal mass shift constant N . In the absence of alkalilike transitions and theoretical work on this complex system, no predictions for S are available; N , however, may be calculated

Only the frequency of the ECDL laser was determined and recorded. In principle, the injection-locked laser should be lasing at a frequency very close to that; however, effects such as a nonoptimal lock, cavity mode pulling, and frequency chirps caused by the pump laser pulse may introduce inaccuracies [45,46]. The chirp effect, however, is a constant offset on the frequency axis and therefore valid for all isotopes. Any effect on the isotope shift is negligible.

B. Collinear laser spectroscopy

Systematic uncertainties to the measurement of isotope shifts may be introduced from the conversion of scanning voltages to frequencies and may be evaluated using [47]

using $N = \nu m_e / m_u$ where ν corresponds to the frequency of the transition, m_e to the mass of the electron, and m_u to the atomic mass unit. Incorporating $M = N$ and thus $S = 0$ as a fixed intercept into the King plot (as done in [43]) has no influence on the extracted F_{eff} values on the precision quoted in Table IV. The difference in the $\delta \langle r^2 \rangle^{240,A}$ compared to the values presented in Table IV is less than 2%.

D. Inclusion of systematic uncertainties

As the experimental effects discussed in this section are correlated, the total systematic uncertainty to be attributed to the isotope shifts is taken as a direct sum of the individual values. In case of HR-RIS this amounts to $\delta v_{\text{sys}}^{\text{HR-RIS}} = 8$ MHz and in case of CLS to $\delta v_{\text{sys}}^{\text{CLS}} \leq 2.5$ MHz. Ultimately, this yields an additional error to $\delta \langle r^2 \rangle_{\text{sys,exp}}^{\text{HR-RIS,385nm}} = 0.0011 \text{ fm}^2$ and $\delta \langle r^2 \rangle_{\text{sys,exp}}^{\text{HR-RIS,388nm}} = 0.0003 \text{ fm}^2$ for the high-resolution resonance ionization spectroscopy measurements as a result of the experimental technique. Similarly, a systematic error of $\delta \langle r^2 \rangle_{\text{sys,exp}}^{\text{CLS}} \approx 0.0004 \text{ fm}^2$ is attributed to the results from the collinear laser spectroscopy investigations. Relative systematic uncertainties originating from the experimental methods are $< 0.5\%$ for $\delta \langle r^2 \rangle_{\text{HR-RIS,385nm}}$ and $\delta \langle r^2 \rangle_{\text{CLS}}$, whereas they are of the order of 2% for $\delta \langle r^2 \rangle_{\text{HR-RIS,388nm}}$. The difference emerges from the different F_{eff} of the three transitions.

The relative uncertainties of the effective field shift factors are of the order of 10%, translating to systematic uncertainties $\delta \langle r^2 \rangle_{\text{sys,theo}}$ of up to 0.03 fm^2 on the changes in mean-squared charge radii for the isotopes investigated. Taking such uncertainties in F_{eff} into account leads to the conclusion that the two experimental methods are in agreement with one another.

VI. CONCLUSIONS

Long-lived Pu isotopes have been studied using two complementary laser spectroscopic methods, resonance ionization spectroscopy using the Mainz atomic beam unit and collinear

laser spectroscopy at the IGISOL facility of the University of Jyväskylä. The measurements using HR-RIS included the use of an injection-locked pulsed Ti:sapphire laser with an intrinsic linewidth of ~ 13 MHz affording a direct comparison of the two techniques.

Isotope shifts have been measured on the ground-state $5f^67s^2\ ^7F_0 \rightarrow 5f^56d^27s$ ($J = 1$) and metastable state $5f^67s^2\ ^7F_1 \rightarrow 5f^67s7p$ ($J = 2$) atomic transitions using the HR-RIS method and the hyperfine factors have been extracted for the odd mass nuclei $^{239,241}\text{Pu}$. Collinear laser spectroscopy was performed on the $5f^67s\ ^8F_{1/2} \rightarrow J = 1/2$ ($27\,523.61\text{ cm}^{-1}$) ionic transition with the hyperfine A factors measured for ^{239}Pu . The King plot method was used to perform a consistency check of the two techniques as well as providing an empirical extraction of the field shift factors for all three optical transitions. Changes in mean-squared charge radii are consistent with those determined by nonoptical muonic x-ray studies; however, they have a precision approximately one order of magnitude greater when only comparing statistical uncertainties.

A thorough analysis of experimental systematic uncertainties has been performed. Unforeseen systematic errors in either the wavelength determination, method of data acquisition, or possible perturbations to the excited state caused by the high laser power used in the ionization step may account for any discrepancy in absolute value between the two techniques. Within the dominating uncertainty of $\sim 10\%$ on $\delta\langle r^2 \rangle^{240,A}$ due to the effective field shift factors the changes in mean-squared charge radii extracted from the different transitions and techniques are consistent.

This work will hopefully stimulate future theoretical efforts in calculating the field shift and mass shift factors for actinide elements, where especially the specific mass shift constant is of importance. Such calculations would provide invaluable input for the current King plots. Furthermore, this work would benefit from additional measurements of absolute charge radii, e.g., through electronic K - or muonic x-ray isotope shifts, in order to provide constraints for future calculations. In addition, it is of high interest to probe the isotope shifts of a single transition which can be accessed by both experimental techniques.

To date, Pu is now the heaviest element studied using the collinear laser spectroscopic technique. In the immediate future, efforts are under way to expand the high-resolution studies to other actinide elements, notably thorium and uranium.

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