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Correlated Event-by-Event Fluctuations of Flow Harmonics in Pb-Pb Collisions at √s_{NN} = 2.76 TeV

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We report the measurements of correlations between event-by-event fluctuations of amplitudes of anisotropic flow harmonics in nucleus-nucleus collisions, obtained for the first time using a new analysis method based on multiparticle cumulants in mixed harmonics. This novel method is robust against systematic biases originating from nonflow effects and by construction any dependence on symmetry planes is eliminated. We demonstrate that correlations of flow harmonics exhibit a better sensitivity to medium properties than the individual flow harmonics. The new measurements are performed in Pb-Pb collisions at the center-of-mass energy per nucleon pair of √s_{NN} = 2.76 TeV by the ALICE experiment at the Large Hadron Collider. The centrality dependence of correlation between event-by-event fluctuations of the elliptic \( v_2 \) and quadrangular \( v_4 \) flow harmonics, as well as of anticorrelation between \( v_2 \) and triangular \( v_3 \) flow harmonics are presented. The results cover two different regimes of the initial state configurations: geometry dominated (in midcentral collisions) and fluctuation dominated (in the most central collisions). Comparisons are made to predictions from Monte Carlo Glauber, viscous hydrodynamics, AMPT, and HIJING models. Together with the existing measurements of the individual flow harmonics the presented results provide further constraints on the initial conditions and the transport properties of the system produced in heavy-ion collisions.

The properties of an extreme state of matter, the quark-gluon plasma (QGP), are studied by colliding heavy ions at BNL’s Relativistic Heavy Ion Collider (RHIC) and at CERN’s Large Hadron Collider (LHC). One of the most widely utilized physical phenomena in the exploration of QGP properties is collective anisotropic flow [1,2]. The large elliptic flow discovered at RHIC energies [3], which at the LHC energy of 2.76 TeV is 30% larger [4] and is recently reported in Ref. [5] to increase even further at 5.02 TeV, demonstrated that the QGP behaves like a strongly coupled liquid with a very small ratio of the shear viscosity to entropy density, \( \eta/s \), which is close to a universal lower bound of \( 1/4\pi \) [6].

Anisotropic flow is traditionally quantified with harmonics \( v_n \) and corresponding symmetry plane angles \( \psi_n \) in the Fourier series decomposition of the particle azimuthal distribution (parametrized with azimuthal angle \( \varphi \)) in the plane transverse to the beam direction [7]:

\[
\frac{dN}{d\varphi} \propto 1 + 2 \sum_{n=1}^{\infty} v_n \cos[n(\varphi - \psi_n)].
\]

The shape of the intersecting zone of two identical heavy ions in noncentral collisions is approximately ellipsoidal. This initial anisotropy is transferred via interactions among constituents and the pressure gradients developed in the QGP medium to an observable final-state anisotropic emission of particles with respect to the symmetry plane(s) of the intersecting zone. The resulting anisotropic flow for such an idealized ellipsoidal geometry is determined solely by even Fourier harmonics \( v_{2n} \), and only one symmetry plane (the reaction plane) exists. Recently, the importance of flow fluctuations and related additional observables has been identified. This has led to new concepts such as nonvanishing odd harmonics \( v_{2n-1} \) at midrapidity [8], nonidentical symmetry plane angles \( \psi_n \) and their intercorrelations [9–14], the stochastic nature of the harmonic \( v_n \) and its probability density function \( P(v_n) \) [15–20], and, finally, the importance of higher order flow moments \( \langle v_n^k \rangle \) (where the angular brackets denote an average over all events, and \( k \geq 2 \)) [21]. Two distinct regimes for anisotropic flow development are nowadays scrutinized separately: geometry dominated (in midcentral collisions) and fluctuation dominated (in the most central collisions) [11].

Anisotropic flow is generated by the initial anisotropic geometry and its fluctuations coupled with an expansion of the produced medium. The initial coordinate space anisotropy can be quantified in terms of the eccentricity coefficients \( \varepsilon_n \) and the corresponding symmetry plane angles \( \Phi_n \) [8,15,22]. A great deal of effort is being invested...
to understand the relations between the momentum space Fourier harmonics $v_n$ and the symmetry planes $\psi_n$ on one side, and their spatial counterparts $\varepsilon_n$ and $\Phi_n$ on the other side. These relations describe the response of the produced system to the initial coordinate space anisotropies, and therefore provide a rich repository of constraints for the system properties. In the early studies it was regularly assumed that, for small eccentricities, the harmonics $v_n$ respond linearly to the eccentricities $\varepsilon_n$ of the same order, $v_n \propto \varepsilon_n$, and that $\psi_n = \Phi_n$ [8,10,23,24]. However, for sizable eccentricities recent studies argue that the anisotropies in momentum and coordinate space are related instead with the matrix equation connecting a set of anisotropic flow harmonics $\{v_n\}$ and a set of eccentricity coefficients $\{\varepsilon_n\}$: it was demonstrated that the hydrodynamic response is both nondiagonal and nonlinear, and that in general $\psi_n \neq \Phi_n$ [9,11,25,26]. The first realization led to the conclusion that a relationship between event-by-event fluctuations of the amplitudes of two different flow harmonics $v_m$ and $v_n$ can exist. This is hardly surprising for even flow harmonics in noncentral collisions because the ellipsoidal shape generates nonvanishing values for all even harmonics $v_{2n}$ [27], not only for elliptic flow. However, this simple geometrical argument cannot explain the possible relation between the even and odd flow harmonics in noncentral collisions, and the argument is not applicable in the central collisions, where all initial shapes are equally probable since they originate solely from fluctuations. Recently a linear correlation coefficient $c(a, b)$ was defined in this context, which becomes $1 \left( -1 \right)$ if observables $a$ and $b$ are fully linearly (antilinearly) correlated and zero in the absence of correlation [25]. Model calculations of this new observable showed that neither $v_2$ and $v_3$ nor $v_2$ and $v_4$ are linearly correlated in noncentral collisions. Most importantly, it was demonstrated that $c(v_2, v_4)$ depends strongly both on $\eta/s$ of the QGP and on the value of $c(\varepsilon_2, \varepsilon_4)$, which quantifies the relationship between corresponding eccentricities in the initial state [25]. Therefore, it was concluded that new observables $c(v_n, v_m)$, depending on the choice of flow harmonics $v_n$ and $v_m$, are sensitive both to the fluctuations of the initial conditions and to the transport properties of the QGP, with the potential to discriminate between the two respective contributions when combined with a measurement of individual flow harmonics [25].

In this Letter we study the relationship between event-by-event fluctuations of magnitudes of two different flow harmonics of order $n$ and $m$ by using a recently proposed four-particle observable [28]:

$$
\langle \langle \cos(m\varphi_1 + n\varphi_2 - m\varphi_3 - n\varphi_4) \rangle \rangle_c = \langle \langle \cos(m\varphi_1 + n\varphi_2 - m\varphi_3 - n\varphi_4) \rangle \rangle_c
\quad - \langle \langle \cos(m(\varphi_1 - \varphi_2)) \rangle \langle \langle \cos(n(\varphi_1 - \varphi_2)) \rangle \rangle
\quad = \langle v_m^2 v_n^2 \rangle - \langle v_m^2 \rangle \langle v_n^2 \rangle \tag{2}
$$

with the condition $m \neq n$ for two positive integers $m$ and $n$. We refer to these new observables as the symmetric two-harmonic four-particle cumulant, and use the notation SC$(m, n)$, or just SC. The double angular brackets indicate that the averaging procedure has been performed in two steps—first, averaging over all distinct particle quadruplets in an event, and then in the second step weighting the single-event averages with the “number of combinations.” The latter for single-event average four-particle correlations is mathematically equivalent to a unit weight for each individual quadruplet when the multiplicity differs event by event [29]. In both two-particle correlators above all distinct particle pairs are considered in each case. The four-particle cumulant in Eq. (2) is less sensitive to nonflow correlations than any two- or four-particle correlator on the right-hand side taken individually [30,31]. The last equality is true only in the absence of nonflow effects [32]. The observable in Eq. (2) is zero in the absence of flow fluctuations, or if the magnitudes of the harmonics $v_m$ and $v_n$ are uncorrelated [28]. It is also unaffected by the relationship between the symmetry plane angles $\psi_m$ and $\psi_n$. The four-particle cumulant in Eq. (2) is proportional to the linear correlation coefficient $c(a, b)$ introduced in Ref. [25] and discussed above, with $a = v_m^2$ and $b = v_n^2$. Experimentally, it is more reliable to measure the higher order moments of the flow harmonics $v_k^N (k \geq 2)$ with two- and multiparticle correlation techniques [31,33,34], than to measure the first moments $v_n$ with the event plane method, due to the systematic uncertainties involved in the event-by-event estimation of the symmetry planes [35,36]. Therefore, we have used the new multiparticle observable in Eq. (2) as meant to be the least biased measure of the correlation between event-by-event fluctuations of magnitudes of the two different harmonics $v_m$ and $v_n$ [28].

The two- and four-particle correlators in Eq. (2) were evaluated in terms of $Q$ vectors [33]. The $Q$ vector (or flow vector) in harmonic $n$ for a set of $M$ particles, where throughout this Letter $M$ is the multiplicity of an event, is defined as $Q_n \equiv \sum_{k=1}^{M} e^{i n \varphi_k}$ [7,37]. We have used for a single-event average two-particle correlation $\langle \cos(n(\varphi_1 - \varphi_2)) \rangle$ the following definition and analytic result in terms of $Q$ vectors:

$$
\frac{1}{(\frac{M}{2})!} \sum_{(\varphi_j, \varphi_i)} e^{in(\varphi_i - \varphi_j)} = \frac{1}{(\frac{M}{2})!} \left| Q_n^2 - M \right| \tag{3}
$$
For four-particle correlation $\langle \cos(\eta q_1 + \eta q_2 - \eta q_3 - \eta q_4) \rangle$ we used

$$
\frac{1}{M^4 4!} \sum_{(a,b,c,d)} e^{i(m\eta_1 + n\eta_2 - m\eta_3 - n\eta_4)} = \frac{1}{M^4 4!} \{ |Q_m|^2 |Q_n|^2 - 2Re[Q_{m+n}Q_m^*Q_n^* - 2Re[Q_mQ_{m-n}Q_n^*] + |Q_{m+n}|^2 + |Q_{m-n}|^2 - (M - 4)(|Q_m|^2 + |Q_n|^2) + M(M - 6) \}.
$$

In order to obtain the all-event average correlations, denoted by $\langle \cdots \rangle$ in Eq. (2), we have weighted single-event expressions in Eqs. (3) and (4) with weights $M(M - 1) M(M - 1)(M - 2)(M - 3)$, respectively [29].

The data used in this analysis were obtained with the ALICE detector [38,39]. They consist of minimum-bias Pb-Pb collisions recorded during the 2010 LHC Pb-Pb run at $\sqrt{s_{NN}} = 2.76$ TeV. With the default event and track selection criteria described below, we have obtained in total about $1.8 \times 10^9$ events per 1% centrality bin width. All individual systematic variations were combined in quadrature to obtain the final uncertainty.

The centrality was determined with the V0 detector [40–42]. As a part of systematic checks the centrality was determined independently with the time projection chamber (TPC) [43] and the silicon pixel detector [44,45], which have slightly worse resolution [42]. A systematic difference of up to 3% was observed in the SC($m,n$) results when using different centrality estimations. Charged particles were reconstructed with the TPC and the inner tracking using different centrality estimations. Charged particles in the transverse momentum range $p_T < 100$ GeV/c, with a $p_T$ resolution of less than 6% for tracks below 20 GeV/c. Because of TPC dead zones between neighboring sectors, the track finding efficiency is about 75% for $p_T = 200$ MeV/c and then it saturates at about 85% for $p_T > 1$ GeV/c in Pb-Pb collisions. The TPC covers the full azimuth and has a pseudorapidity coverage of $|\eta| < 0.9$. Tracks reconstructed using the TPC and inner tracking system are referred to as global, while tracks reconstructed only with the TPC are referred to as TPC only.

For online triggering, the V0 and silicon pixel detectors were used [39]. The reconstructed primary vertex is required to lie within $\pm 10$ cm of the nominal interaction point in the longitudinal direction along the beam axis. The cut on the position of the primary vertex along the beam axis was varied from $\pm 12$ to $\pm 6$ cm; the resulting SC measurements are consistent with those obtained with the default cut.

The main analysis was performed with global tracks selected in the transverse momentum interval $0.2 < p_T < 5.0$ GeV/c and the pseudorapidity region $|\eta| < 0.8$. With this choice of a low $p_T$ cutoff we are reducing event-by-event biases from a smaller reconstruction efficiency at lower $p_T$, while the high $p_T$ cutoff was introduced to reduce the contribution to the anisotropies from the jets. Reconstructed tracks were required to have at least 70 TPC space points (out of a maximum of 159). Only tracks with a transverse distance of closest approach (DCA) to the primary vertex less than 3 mm are accepted to reduce the contamination from secondary tracks. Tracks with kinks (the tracks that appear to change direction due to multiple scattering, $K^\pm$ decays) were rejected.

An independent analysis was performed with TPC-only and hybrid tracks (see below). For TPC-only tracks, the DCA cut was relaxed to 3 cm, providing a different sensitivity to contamination from the secondary tracks. Both the azimuthal acceptance and the reconstruction efficiency as a function of transverse momentum differ between the TPC-only and global tracks. The resulting difference between independent analyses with global and TPC-only tracks was found to be 1%–5% in all the centrality ranges studied, both for SC(3,2) and SC(4,2).

In another independent analysis with hybrid tracks, three different types of tracks were combined, in order to overcome the nonuniform azimuthal acceptance due to dead zones in the silicon pixel detector, and to achieve the best transverse momentum resolution [39]. In this analysis the DCA cut was set to 3.2 cm in the longitudinal and to 2.4 cm in the transverse direction. The results between the global and hybrid tracks differ by 3% to 5%, depending on the observable considered.

One of the largest contributions to the systematic uncertainty originates from the nonuniform reconstruction efficiency as a function of transverse momentum. For the observables SC(3,2) and SC(4,2) the uncertainty is 7% and 8%, respectively. In order to correct the measurements of these azimuthal correlators for various detector inefficiencies, we have constructed the particle weights as a function of azimuthal angle $\varphi$ and transverse momentum $p_T$, and used the prescription outlined in Ref. [28]. In particular, $p_T$ weights were constructed as a ratio of the transverse momentum distribution obtained from Monte Carlo generated tracks and from tracks reconstructed after they have passed through the detector simulated with GEANT3 [46].

We have used four Monte Carlo models in this Letter. The HIJING model [47,48] was utilized to obtain the $p_T$ weights [28]. Second, the HIJING model was used to estimate the strength of the nonflow correlations (typically few-particle correlations insensitive to the collision geometry). We have evaluated the observables of interest in coordinate space by modeling the initial conditions with a Monte Carlo Glauber model [49]. We have compared the
centrality dependence of our observables with the theoretical model from Ref. [50], where the initial energy density profiles are calculated using a next-to-leading order perturbative-QCD+saturation model [51,52]. The subsequent spacetime evolution is described by relativistic dissipative fluid dynamics with different parametrizations for the temperature dependence of the shear viscosity to entropy density ratio $\eta/s(T)$. Each of the $\eta/s(T)$ parametrizations is adjusted to reproduce the measured $v_n$ from central to midperipheral collisions. Finally, we provide an independent estimate of the centrality dependence of our observables by utilizing the AMPT model [53].

The centrality dependence of SC(4,2) (red squares) and SC(3,2) (blue circles) is presented in Fig. 1. Positive values of SC(4,2) are observed for all centralities. This suggests a correlation between the event-by-event fluctuations of $v_2$ and $v_4$, which indicates that finding $v_2$ larger than $\langle v_2 \rangle$ in an event enhances the probability of finding $v_4$ larger than $\langle v_4 \rangle$ in that event. On the other hand, the negative results of SC(3,2) show the anticorrelation between the $v_2$ and $v_3$ magnitudes, which further imply that finding $v_2$ larger than $\langle v_2 \rangle$ enhances the probability of finding $v_3$ smaller than $\langle v_3 \rangle$. We have calculated the SC observables using HIJING, which does not include anisotropic collectivity but, e.g., azimuthal correlations due to jet production [47,48]. It is found that in HIJING both $\langle \cos(m \phi_1 + n \phi_2 - m \phi_3 - n \phi_4) \rangle$ and $\langle \cos(m \phi_1 - \phi_2) \rangle \langle \cos(n \phi_1 - \phi_2) \rangle$ are nonzero. However, the calculated SC observables from HIJING are compatible with zero for all centralities, which suggests that the SC measurements are nearly insensitive to nonflow correlations. We have also performed a study using the like-sign technique, which is another powerful approach to estimate the nonflow effects [4]. It was found that the difference between the correlations for like-sign and all charged combinations is within 10%. This demonstrates

![SC(3,2) and SC(4,2) observables](image)

FIG. 1. Centrality dependence of the observables SC(4,2) (red filled squares) and SC(3,2) (blue filled circles) in Pb-Pb collisions at 2.76 TeV. Systematic errors are represented with boxes. The results for the HIJING model are shown with hollow markers.

This demonstrates that nonzero values of SC measurements cannot be explained by nonflow effects.

A study based on the AMPT model showed that the observed (anti)correlations are also sensitive to the transport properties, e.g., the partonic and hadronic interactions [20,28]. Figure 2 shows the comparison of SC(3,2) and...
SC(4,2) to the AMPT calculations, which generally predict the correct sign but underestimate their magnitude. The comparison between experimental data and the theoretical calculations [50], which incorporate both the initial conditions and the system evolution, is shown in Fig. 2 (top). The model captures qualitatively the centrality dependence, but not quantitatively. Most notably, there is no single centrality for which a given $\eta/s(T)$ parametrization describes simultaneously both SC(4,2) and SC(3,2). On the other hand, the same theoretical model captures quantitatively the centrality dependence of the individual $v_2$, $v_3$, and $v_4$ harmonics with a precision better than 10% in the central and midcentral collisions [50]. We therefore conclude that the individual flow harmonics $v_n$ and new SC$(m,n)$ observables together provide a better handle on the initial conditions and $\eta/s(T)$ than each of them alone. This is emphasized in Fig. 2 (middle), where the SC(3,2) and SC(4,2) observables were divided with the products $\langle v_2^2 \rangle \langle v_3^2 \rangle$ and $\langle v_2^2 \rangle \langle v_4^2 \rangle$, respectively, in order to obtain the normalized SC observables (the result for 60%–70% is omitted due to the large statistical uncertainty). These products were obtained with two-particle correlations and using a pseudorapidity gap of $|\Delta \eta| > 1.0$ to suppress biases from few-particle nonflow correlations. We have found that the normalized SC(4,2) observable exhibits much better sensitivity to different $\eta/s(T)$ parametrizations than the normalized SC(3,2) observable, see Fig. 2 (middle), and than the individual flow harmonics [50]. These findings indicate that the normalized SC(3,2) observable is sensitive mainly to the initial conditions, while the normalized SC(4,2) observable is sensitive to both the initial conditions and the system properties, which is consistent with the prediction from Ref. [25].

It can be seen in Fig. 1 that SC(4,2) and SC(3,2) increase nonlinearly up to centrality 60%. Assuming only a linear response, $v_n \propto e_n$, we expect that the normalized SC$(m,n)$ evaluated in coordinate space can capture the measurement of the centrality dependence of the normalized SC$(m,n)$ in the momentum space. The correlations between the $n$th and $m$th order harmonics were estimated with calculations of $\langle (e_n^2 e_m^2) - \langle e_n^2 \rangle \langle e_m^2 \rangle \rangle / \langle e_n^2 \rangle \langle e_m^2 \rangle$, i.e., a normalized SC observable in the coordinate space, which we denote SC$(m,n)/\langle e_m^2 \rangle$. Here, $e_n$ ($e_m$) is the $n$th ($m$th) order coordinate space anisotropy, following the definition in Ref. [8]. Different scenarios of the Monte Carlo Glauber model, named the wounded nucleon and binary collision weights, have been used. An increasing trend from central to peripheral collisions with different sign has been observed in Fig. 2 (bottom) for SC(4,2) and SC(3,2). A dramatic deviation of SC(4,2) between data and the model calculation is observed for noncentral collisions. This deviation increases from midcentral to peripheral, which could be understood as the contribution of the nonlinear response ($e_2$ contributes to $v_4$) increasing as a function of centrality, which is consistent with that reported in Ref. [54]. Since the normalized SC(3,2) appears to be sensitive only to the initial conditions and not to $\eta/s(T)$, see Fig. 2 (middle), the Monte Carlo Glauber model captures better its centrality dependence than it does for the normalized SC(4,2) observable, see Fig. 2 (bottom).

The relationship between the flow harmonics $v_2$, $v_3$, $v_4$ has also been investigated by the ATLAS Collaboration using the event shape engineering technique [54–56]. For events with a larger $v_2$, the ATLAS Collaboration showed these have a smaller than average $v_3$, and a larger than average $v_4$. For events with a smaller $v_2$, the opposite trend occurred. These observations are consistent with the patterns observed via the SC measurements presented in this Letter. The SC observables, however, provide a compact quantitative measure of these correlations, without fitting correlations between $v_n$ and $v_m$. This simplifies the quantitative comparison of the SC observables with hydrodynamical calculations as shown in Fig. 2.

In the most central collisions the anisotropies originate mainly from fluctuations; i.e., the initial ellipsoidal...
geometry characteristic for midcentral collisions plays little role in this regime. Therefore, we have performed a separate analysis for the centrality range 0%–10% in centrality bins of 1%. The results are presented in Fig. 3. We observe that event-by-event fluctuations of \( v_2 \) and \( v_4 \) remain correlated, and of \( v_2 \) and \( v_3 \) anticorrelated, also in this regime. However, the strength of the (anti) correlations exhibits a different centrality dependence than for the wider centrality range shown in Fig. 1. As seen in Fig. 3 (top) the centrality dependence cannot be linearly extrapolated from the 0%–10% region to the full centrality range. Comparison with the two different parametrizations of the Monte Carlo Glauber initial conditions for the normalized SC observables presented in Fig. 3 (bottom) suggests that the binary collision parametrization (binary collision weights) is favored by the data in most central collisions. This agreement may suggest the scaling with the number of quark participants [57–61] in central collisions at the LHC energies.

In summary, we have measured for the first time the new multiparticle observables, the symmetric two-harmonic four-particle cumulants, which quantify the relationship between the event-by-event fluctuations of two different flow harmonics. We have found that the fluctuations of \( v_2 \) and \( v_3 \) are anticorrelated in all centralities; however, the details of the centrality dependence differ in the fluctuation-dominated (most central) and the geometry-dominated (midcentral) regimes. The fluctuations of \( v_2 \) and \( v_4 \) are correlated for all centralities. The SC observables were used to discriminate between the state-of-the-art hydro model calculations with different parametrizations of the temperature dependence of \( \eta/s \), for all of which the centrality dependence of elliptic, triangular, and quadrangular flow has a weaker sensitivity at the LHC. In particular, the centrality dependence of SC (4,2) cannot be captured with the constant \( \eta/s \). We have also used our results to discriminate between two different parametrizations of the initial conditions and have demonstrated that in the fluctuation-dominated regime (in central collisions) the Monte Carlo Glauber initial conditions with binary collision weights are favored over wounded nucleon weights.

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35 European Organization for Nuclear Research (CERN), Geneva, Switzerland
36 Excellence Cluster Universe, Technische Universität München, Munich, Germany
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38 Faculty of Mathematics, Physics and Informatics, Comenius University, Bratislava, Slovakia
39 Faculty of Nuclear Sciences and Physical Engineering, Czech Technical University in Prague, Prague, Czech Republic
40 Faculty of Science, P.J. Šafárik University, Košice, Slovakia
41 Faculty of Technology, Buskerud and Vestfold University College, Vestfold, Norway
42 Frankfurt Institute for Advanced Studies, Johann Wolfgang Goethe-Universität Frankfurt, Frankfurt, Germany
43 Gangneung-Wonju National University, Gangneung, South Korea
44 Gauhati University, Department of Physics, Guwahati, India
45 Helmholtz-Institut für Strahlen- und Kernphysik, Rheinische Friedrich-Wilhelms-Universität Bonn, Bonn, Germany
46 Helsinki Institute of Physics (HIP), Helsinki, Finland
47 Hiroshima University, Hiroshima, Japan
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49 Indian Institute of Technology Indore, Indore (IITI), India
50 Indonesian Institute of Sciences, Jakarta, Indonesia
51 Inha University, Incheon, South Korea
52 Institut de Physique Nucléaire d'Orsay (IPNO), Université Paris-Sud, CNRS-IN2P3, Orsay, France
53 Institute for Nuclear Research, Academy of Sciences, Moscow, Russia
54 Institute for Subatomic Physics of Utrecht University, Utrecht, The Netherlands
55 Institute for Theoretical and Experimental Physics, Moscow, Russia
56 Institute of Experimental Physics, Slovak Academy of Sciences, Košice, Slovakia
57 Institute of Physics, Academy of Sciences of the Czech Republic, Prague, Czech Republic
58 Institute of Physics, Bhubaneswar, India
59 Institute of Space Science (ISS), Bucharest, Romania
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61 Institut für Kernphysik, Johann Wolfgang Goethe-Universität Frankfurt, Frankfurt, Germany
62 Institut für Kernphysik, Westfälische Wilhelms-Universität Münster, Münster, Germany
63 Instituto de Ciencias Nucleares, Universidad Nacional Autónoma de México, Mexico City, Mexico
64 Instituto de Física, Universidad Nacional Autónoma de México, Mexico City, Mexico
65 Institut Pluridisciplinaire Hubert Curien (IPHC), Université de Strasbourg, CNRS-IN2P3, Strasbourg, France
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67 Joint Institute for Nuclear Research (JINR), Dubna, Russia
68 Konkuk University, Seoul, South Korea
69 Korea Institute of Science and Technology Information, Daejeon, South Korea
70 KTO Konya University, Konya, Turkey
71 Laboratoire de Physique Corpusculaire (LPC), Clermont Université, Université Blaise Pascal, CNRS-IN2P3, Clermont-Ferrand, France
72 Laboratoire de Physique Subatomique et de Cosmologie, Université Grenoble-Alpes, CNRS-IN2P3, Grenoble, France
73 Laboratori Nazionali di Frascati, INFN, Frascati, Italy
74 Laboratori Nazionali di Legnaro, INFN, Legnaro, Italy
75 Lawrence Berkeley National Laboratory, Berkeley, California, USA
76 Moscow Engineering Physics Institute, Moscow, Russia
77 Nagasaki Institute of Applied Science, Nagasaki, Japan
<table>
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<tr>
<th>Institution</th>
<th>City, Country</th>
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<td>National Centre for Nuclear Studies, Warsaw</td>
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<td>Research Division and ExtreMe Matter Institute EMMI, GSI Helmholtzzentrum für Schwerionenforschung</td>
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