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A search for neutrino–antineutrino mass inequality by means of sterile neutrino oscillometry

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Abstract

The investigation of the oscillation pattern induced by the sterile neutrinos might determine the oscillation parameters, and at the same time, allow to probe CPT symmetry in the leptonic sector through neutrino–antineutrino mass inequality. We propose to use a large scintillation detector like JUNO or LENA to detect electron neutrinos and electron antineutrinos from MCi electron capture or beta decay sources. Our calculations indicate that such an experiment is realistic and could be performed in parallel to the current research plans for JUNO and RENO. Requiring at least 5σ confidence level and assuming the values of the oscillation parameters indicated by the current global fit, we would be able to detect neutrino–antineutrino mass inequality of the order of 0.5% or larger, which would imply a signal of CPT anomalies.

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1. Introduction

The discovery of neutrino oscillations [1] provided undisputed evidence of incompleteness of the conventional Standard Model (SM) of particle physics [2] and gave a clear indication that
further neutrino studies may lead us towards phenomena Beyond the Standard Model (BSM). One of such possible manifestations would be violation of CPT invariance [3] in the process of neutrino oscillations.

CPT symmetry is considered a fundamental law of nature, to which we know no exceptions yet. One of the important implications of this symmetry law is the requirement that in all processes involving particles and their antiparticles the corresponding probabilities and other parameters governing the process should be exactly the same. Many experiments based on that principle have been conducted to probe the CPT conservation. For instance, in the leptonic sector, a measurement of g-factor for electron and positron performed at the University of Washington in Seattle [4] or, in the baryonic sector, a mass measurement of proton and antiproton implemented at CERN [5,6].

Neutrinos carry important information about weak interactions. Especially their interferometric nature makes them a very sensitive tool to search for unconventional physics, in particular CPT violation and Lorentz violation [3,7]. MINOS experiment has made an unsuccessful attempt to search for a possible dependence of the neutrino and antineutrino oscillation probability on the direction of propagation [8]. Perhaps one of the reasons why the issue of CPT violation in the leptonic sector remains unresolved is the shortage of experiments making a direct and simultaneous comparison of neutrino and antineutrino properties such as a possible mass inequality.

Obviously, the properties of neutrinos doom the attempts to verify CPT conservation through oscillation measurements to a likely failure or, at best, have a prohibitively high price tag. Very low interaction cross-sections, limited neutrino flux, and the size of the available detectors exclude such attempts on short time scales. However, if the active neutrinos like the well-known electron-, muon-, and tau neutrino and their antiparticles were not the only existing neutrino flavors, it might be possible to search for CPT violation already in the near future, as it is outlined in this paper.

One of the exciting new hypotheses is the existence of the light sterile neutrinos with unknown nature and properties [9]. The existence of one or more sterile flavors is indicated by the re-evaluation of reactor neutrino fluxes experiments [10], some of the beam experiments such as MiniBoone, LSND and the Gallium anomaly [9,11].

Although the direct observation of sterile neutrinos is not possible, their presence would be revealed by a distinct oscillation pattern, caused by the conversion from active to sterile flavor. If observed, the pattern would also give a hint of the number of sterile neutrino flavors. The simplest assumption is the scenario with one additional sterile flavor, so-called 3 + 1 scheme [12]. The current global fit to the oscillation data suggests that the additional mass-squared difference and mixing angle governing the active-to-sterile conversion should be of the order of $\Delta m^2_{41} \sim 1$ eV$^2$ and $\sin^2 2\theta_{ee} \sim 0.1$ respectively [13]. Assuming these parameter values and relying on the proportionality between the energy and oscillation length, we may choose the energy of neutrinos in a way that at least one full oscillation period will overlap with the active volume of a single detector, like it is proposed in the Borexino SOX experiment [14]. The realization of this neutrino oscillometry method [15] will open a unique opportunity to search not only for disappearance oscillations to sterile neutrinos but also to check the validity of CPT conservation in the leptonic sector if such a transition is observed.

2. Probing neutrino–antineutrino mass inequality

If CPT is strictly conserved the oscillation of neutrinos and antineutrinos would be described by identical probability functions with two main parameters: mixing angles and mass-squared
differences. For instance, in the case of 3 + 1 scenario, the survival probability of electron neutrino and electron antineutrino can be approximated with [15]:

\[
P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \sin^2(2\theta_{ee}) \cdot \sin^2(1.27 \cdot \Delta m_{41}^2 \cdot \frac{L}{E}).
\]

Note that the equation (1) is valid for short baseline experiment (SBL). Consequently, if CPT conservation holds, we should obtain in the classical case [16]:

\[
\frac{(\Delta m_{41}^2)_N}{(\Delta m_{41}^2)_A} = 1,
\]

where \(N\) stands for the value obtained from the measurement with neutrinos and \(A\), with antineutrinos. At the same time, if in the real experiment the mass inequality will be observed, then it would mean CPT violation and the estimation of this process should be done within the framework of the Standard Model Extension (SME) formalism with using coefficients of Lorentz- and CPT-violation [3]. In this paper, the comparison is made only for the ratio of the mass-squared differences, because \(\Delta m_{41}^2\) can be extracted from the experimental data with better precision than \(\Theta_{ee}\). For instance, it depends far less on the intensity normalization. The evaluation of \(\Theta_{ee}\) will be considerably less accurate, because of the systematic uncertainties in absolute values of neutrino flux and fiducial volume.

It should be noted, that \(P(\nu_e \rightarrow \nu_\mu) \neq P(\bar{\nu}_e \rightarrow \bar{\nu}_\mu)\) would mean both CPT and CP violation. However the latter cannot be probed in survival experiments if CPT is conserved.\(^1\)

3. Outline of the experiment

Successful application of neutrino oscillometry requires some degree of energy selection and well-defined source position. For these reasons the experiment cannot rely on natural neutrino sources such as the Sun, the Earth or cosmic neutrinos. Nuclear power reactors also are excluded, as they do not produce considerable amounts of electron neutrinos. The best alternatives are provided by man-made, high-intensity beta decaying radioactive sources emitting electron neutrinos and antineutrinos with the energy around 1 MeV. This choice is based on the outcome of the global fit predicting \(\Delta m_{31}^2\) of the order of 1 eV\(^2\). Precise measurement of that value both for electron neutrinos and antineutrinos will be the key outcome of the proposed experiment.

The mass-squared difference will be derived from the reconstructed oscillation probability curves. To measure the oscillation pattern the detector has to have sufficiently low energy threshold for the registration of both neutrinos and antineutrinos and have adequate position and energy resolution. Furthermore, to achieve the required statistics, the active volume of the detector should ideally extend over at least one oscillation period. The only devices that can currently fulfill these requirements are large liquid scintillator detectors.

3.1. Neutrino and antineutrino sources

The obvious first choice for a \(\nu_e\) source is \(^{51}\)Cr, well known from GALLEX [17,18] and GNO [19] experiments. The decay scheme of \(^{51}\)Cr is shown in Fig. 1. This nuclide has 27.7 days half-life and a neutrino spectrum dominated by mono-energetic lines at an energy of around \(~0.75\) MeV (90.1% total branching ratio), as shown in Fig. 1. Current estimations for the SOX

\(^1\) Suggested by E.Kh. Akhmedov.
Fig. 1. The decay scheme of $^{51}$Cr, with indicated energies of emitted neutrinos [23].

Fig. 2. The decay scheme of system $^{144}$Ce–$^{144}$Pr [20,21].

Table 1
Properties of sources proposed as neutrino- and antineutrino emitters for the oscillometry measurement.

<table>
<thead>
<tr>
<th>Source</th>
<th>Type</th>
<th>Spectrum</th>
<th>$E$, MeV</th>
<th>$A$, MCi</th>
<th>$T_{1/2}$, d</th>
<th>Exposition, d</th>
</tr>
</thead>
<tbody>
<tr>
<td>$^{51}$Cr</td>
<td>$\nu_e$</td>
<td>mono</td>
<td>0.75</td>
<td>8</td>
<td>27.7</td>
<td>55</td>
</tr>
<tr>
<td>$^{144}$Ce–$^{144}$Pr</td>
<td>$\bar{\nu}_e$</td>
<td>continuous</td>
<td>1.8–3.0</td>
<td>0.12</td>
<td>285</td>
<td>300</td>
</tr>
</tbody>
</table>

project [14] indicate that a 35 kg chromium oxide source enriched in $^{50}$Cr ($\sim$30%) placed in a nuclear reactor, can be activated up to 10 MCi. Accounting for the decay during extraction from the reactor, transport, and installation inside the detector, the realistic activity of the source at the start of the experiment would be around 8 MCi.

As the source of $\bar{\nu}_e$ we propose $^{144}$Ce–$^{144}$Pr chain [21]. The decay scheme is shown in Fig. 2. The antineutrino energy spectrum of $^{144}$Pr is continuous with the end point energy at about 3 MeV [22] and with the overall half-life of 285 days. About 48.5% of the emitted antineutrinos are at energies above the detection threshold for the IBD reaction (see Section 3.2) and can be used in the experiment. Current studies indicate that an activity of 100 kCi or more can be reached for the Ce–Pr source [24]. In our calculations we assume the initial activity of 120 kCi.

The both type of sources can be produced in nuclear reactor with high flux of neutrons. The properties of sources are summarized in Table 1.
3.2. Neutrino detection in a liquid scintillation detector

Elastic neutrino–electron scattering is the dominant interaction channel leading to the registration of $\nu_e$ events in a liquid scintillator detector. This reaction

$$\nu_e + e^- \rightarrow \nu_e + e^-$$

has similar characteristic to the Compton effect. While all three neutrino flavors interact with electrons by neutral current, electron neutrinos interact as well via charged current. The cross-section of this interaction may be approximated by a simple expression: $\sigma = 0.7 \times E_\nu \cdot 10^{-44}$ cm$^2$ [25]. The uncertainty of this estimation, including of radiation corrections, is about 2% [25].

The dominant detection channel of electron antineutrinos in liquid scintillator is the inverse beta decay reaction (IBD)

$$\bar{\nu}_e + p \rightarrow n + e^+$$

This reaction produces two distinct signals in the detector allowing for an unambiguous identification of a neutrino event. The kinetic energy and annihilation of the positron and the second, from neutron capture on hydrogen. The former is prompt and contains the information on the energy of the neutrino. The later 2.2 MeV gamma signal is delayed by about $\approx 200$ $\mu$s, it depends on the chemical composition of the scintillator. The threshold energy for IBD is 1.8 MeV and the cross section of the process can be approximated by the expression $\sigma = 9.5 \times (E_\nu - 1.29)^2 \cdot 10^{-44}$ cm$^2$ [26].

3.3. Proposed implementation and expected event rates

To evaluate the feasibility of the proposed experiment the event rates were calculated for two alternative shapes of liquid scintillator detector: spherical, with the source installed in the centre, and cylindrical, with the source mounted close to the center of the end cap of the tank.

The specifications of the spherical detector are those of JUNO [27], currently under construction in China. It will contain 20 ktons (fiducial) of liquid scintillator enclosed in a spherical volume with a diameter of 34.5 m. Spherical shape provides the optimal detection geometry when the source of $\nu_e$ or $\bar{\nu}_e$ is placed in the center, as shown in Fig. 3A. The expected exposition time is restricted by the half-life. For the Cr source we therefore assume 55 days and for the Ce–Pr source 300 days. Gamma-ray background from the source inside the detector can be reduced by using a radiation shielding, e.g. from tungsten [14].

To evaluate the case of a cylindrical detector, we have used LENA specifications [28]: 100 m high, 28 m diameter, 50 kton fiducial mass. The source of $\nu_e$ or $\bar{\nu}_e$ would be located close to the top of the detector, as it is shown in Fig. 3B. In this case only the hemispherical volume near the top would be considered for analysis. This is clearly a less favorable geometry as it uses only part of the fiducial volume and has to cope with non-optimal coverage by the photo sensors (PMTs). The only considerable advantage of this geometry is that it eliminates the need to immerse the source into the volume of the detector. For the purpose of this analysis the two detector geometries differ just by a factor of 4 (volume of a sphere vs. hemisphere) hence energy-and distance-dependent event rate in both cases can be expressed by the equation [21,29]:

$$N(L, E) = \int_{L - \frac{L}{2}}^{L + \frac{L}{2}} \int_{E_{\text{min}}}^{E_{\text{max}}} \frac{A_0}{\lambda} \cdot n \cdot \sigma(E) \cdot S(E) \cdot P(L, E) \cdot (1 - \exp[-\lambda \tau_e]) dE dL,$$

(3)
where $A_0$ is the source activity at the start of the measurement, $n$ the density of free protons (electrons) in the target, $\Delta$ the width of bin with the center $L$, $\sigma(E)$ the cross section for IBD or electron–neutrino scattering, $S(E)$ the spectral shape (delta-function for monoenergetic neutrinos), $P(L,E)$ the oscillation probability (1), $t_e$ the time of measurement and $\lambda$ the decay constant of the source.

The total exposure time needed to complete the measurement would be about 355 days assuming that both sources are used subsequently. The event rates were plotted as a function of the distance from the source and are shown in Fig. 4A and Fig. 4B for $\nu_e$ and $\bar{\nu}_e$ respectively. The presented calculations correspond to the spherical geometry.

Since the detection channels for $\nu_e$ and $\bar{\nu}_e$ are different and disentangled, it would be possible to make the measurement with both radioactive sources at the same time. Simultaneous measurements could be realized only in cylindrical geometry (LENA case) with one source on the top and another on the bottom of the detector. Our estimates indicate that NC (neutral current)
contamination of neutrino spectrum from antineutrino would be of the order of 1% only. This configuration would even have the advantage of reduced systematic error due to normalization. However, from the implementation point of view, that would be a major experimental challenge.

4. Results

The main outcome of the experiment will be the independent determination of the oscillation parameters for neutrinos and antineutrinos by fitting the spectra shown in Fig. 4. As it was explained earlier, the main parameter for testing CPT symmetry is $\Delta m^2_{41}$. The confidence level can be evaluated from equation (2),

$$\frac{(\Delta m^2_{41})_N \pm \sigma_N}{(\Delta m^2_{41})_A \pm \sigma_A} = 1 \pm \sigma,$$

(4)

where $\sigma_N$ is the uncertainty of measurement of $(\Delta m^2_{41})_N$, $\sigma_A$ is the uncertainty of measurement of $(\Delta m^2_{41})_A$, $\sigma$ is the total uncertainty of ratio. Since the starting assumption is that $(\Delta m^2_{41})_N$ and $(\Delta m^2_{41})_A$ are identical (although with different error bars), the relative uncertainty can be estimated as follows:

$$\sigma \leq \frac{\sigma_N}{(\Delta m^2_{41})_N} + \frac{\sigma_A}{(\Delta m^2_{41})_A}.$$

(5)

The event samples were generated by using Monte-Carlo approach. The basic steps which were used in analysis:

- The oscillation spectrum was generated with certain oscillation parameters ($\Delta m^2_{41}$ and $\sin^2 2\theta_{ee}$).
- The pattern of real oscillation spectrum was obtained with adding of basic uncertainties: statistical error, the error of position resolution, the error of source activity and the error of fiducial volume of detector. For antineutrino case the energy resolution was also used in analysis.
- The oscillation parameters were extracted from the pattern of real spectrum with using fit-function the same as probability function (1) taking energy and position resolution smearing into account.
- The fit-function was optimized by using the method of minimization $\chi^2$ from package Minuit2 ROOT.
- The gaussian distribution for uncertainties of oscillation parameters was assumed.

The example of such distribution of errors is shown in Fig. 5 and Fig. 6 for neutrino and antineutrino, respectively. As can be seen, the relative error for $\sin^2 2\theta_{ee}$ is larger at least by one order of magnitude than the relative error for $\Delta m^2_{41}$. It explains also our choice for $\Delta m^2_{41}$ as the key parameter of CPT test. The uncertainty of these measured values of $\Delta m^2_{41}$ was determined independently for both sources, and combined with the equation (5). However this approach allows also to determine $\theta_{ee}$ with high precision.

For detector-related uncertainties, the design parameters given by JUNO and LENA Collaborations were used. In the case of JUNO the energy resolution of $3\%/\sqrt{E} \,[\text{MeV}]$ and position resolution of $9\, \text{cm} (\nu_e)$ and $4.5\, \text{cm} (\bar{\nu}_e)$ were used. For LENA $6.1\%/\sqrt{E} \,[\text{MeV}]$, $10\, \text{cm} (\nu_e)$ and $4.5\, \text{cm} (\bar{\nu}_e)$ were used respectively.
Fig. 5. The distribution of difference between reconstructed value and true value for neutrino case in LENA detector geometry. A: the reconstructed parameter is $\Delta m^2_{41}$ with true value 1 eV$^2$. B: the reconstructed parameter is $\sin^2 2\theta_{ee}$ with true value 0.1.

Fig. 6. The distribution of difference between reconstructed value and true value for antineutrino case in LENA detector geometry. A: the reconstructed parameter is $\Delta m^2_{41}$ with true value 1 eV$^2$. B: the reconstructed parameter is $\sin^2 2\theta_{ee}$ with true value 0.1.

Table 2
Expected background and signal events for full time of the experiment. The mass of JUNO’s sphere is 20 kt, mass of semisphere in LENA is 5 kt.

<table>
<thead>
<tr>
<th>Type</th>
<th>Signal</th>
<th>Background</th>
<th>Signal</th>
<th>Background</th>
<th>Exposition time, d</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\nu_e$</td>
<td>1148860</td>
<td>348032</td>
<td>459234</td>
<td>87008</td>
<td>55</td>
</tr>
<tr>
<td>$\bar{\nu}_e$</td>
<td>466800</td>
<td>3090</td>
<td>193500</td>
<td>45</td>
<td>300</td>
</tr>
</tbody>
</table>

Neglecting background from radioactive decays, the main background in the energy region of interest for $\nu_e$ detection arises from the solar neutrinos ($^7$Be). It is shown in Table 2. The influence of this factor on the final result was also taken into account in our estimations. Nevertheless, direct measurements of the solar background are carried out automatically whenever the sources are removed so the correction may be done afterwards. In the case of antineutrinos, the highest
background comes from nuclear reactors and can be neglected, even in the case of JUNO detector, because the expected neutrino flux from $^{144}\text{Ce} - ^{144}\text{Pr}$ source located in the middle of the detector is considerably higher than that of 12 power reactors 53 km away. The estimated event rates from sources with the strength of 8 M Ci for $^{51}\text{Cr}$ and 0.12 M Ci for $^{144}\text{Ce} - ^{144}\text{Pr}$ as well as the corresponding backgrounds are presented in Table 2.

The main outcome of our simulations is shown in Fig. 7 (for LENA) and Fig. 8 (for JUNO). The figures show a 5σ sensitivity limit calculated for 3 different $\sin^2 2\theta_{ee}$ values and plotted as a function of $\Delta m^2_{41}$. For instance, if we check the performance for the parameters chosen by the global fit that is $\Delta m^2_{41} \geq 1 \text{ eV}^2$ and $\sin^2 2\theta_{ee} \approx 0.1$, we conclude from Fig. 7 that LENA will detect (at the 5σ level of measured events) a difference of $\Delta m^2_{41}$ neutrino/antineutrino and therefore CPT violation that exceeds 1%. For the same parameters JUNO would reach 0.5% sensitivity as it may be observed from Fig. 8. The slightly better sensitivity of the JUNO detector is a consequence of the spherical shape and better expected energy resolution.

5. Conclusions

We have outlined a scheme to probe the mass inequality by analyzing the neutrino and antineutrino oscillation patterns induced by the still hypothetical sterile neutrinos. If the “sterile” oscillation patterns are detected, the experiment will yield new fundamentally important oscillation parameters and will be sensitive to the mass inequality on the level of a few tenths of a percent at 5σ significance. This sensitivity can be achieved assuming the current best-fit values of the oscillation parameters indicated by the global fit.

The proposed experiment would utilize a large scintillator like future JUNO, LENA or RENO-50 experiments. Since JUNO is now approved and has just entered the first construction phase, the proposal is certainly feasible. The same concerns the use of M Ci sources. Since similar ones were already produced and used by GALLEX and GNO experiments, there is already the necessary knowhow and, in the case of Cr source, also enriched material in sufficient quantity.
Fig. 8. Sensitivity limits of JUNO for the detection of mass inequality at 5σ level of measured events calculated for 3 different mixing angles and plotted as a function of $\Delta m^2_{41}$.

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