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β decay of ¹³³In: γ emission from neutron-unbound states in ¹³³Sn

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Excited states in 133 Sn were investigated through the β decay of 133 In at the ISOLDE facility. The ISOLDE Resonance Ionization Laser Ion Source (RILIS) provided isomer-selective ionization for 133 In, allowing us to study separately, and in detail, the β -decay branch of 133 In J $^{\pi} = (9/2^+)$ ground state and its J $^{\pi} = (1/2^-)$ isomer.

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Thanks to the large spin difference of the two β -decaying states of ¹³³In, it is possible to investigate separately the lower and higher spin states in the daughter, ¹³³Sn, and thus to probe independently different single-particle and single-hole levels. We report here new γ transitions observed in the decay of ¹³³In, including those assigned to the deexcitation of the neutron-unbound states.

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I. INTRODUCTION

Simple nuclear systems around doubly magic nuclei in exotic regions of the Segré chart are key to our understanding of nuclear structure. The observable evolution of the nuclear single-particle (s. p.) levels sequence far from stability has been postulated to arise from tensor and central forces [1,2], as the occupation of valence orbitals changes with the addition (or removal) of nucleons. Theoretical calculations predicting the evolution of shell structure require as an input complete information on s. p. states close to the core. In this context, the structure of 133 Sn, only one neutron above the doubly magic 132 Sn (Z=50, N=82), provides essential information on neutron s. p. energies, allowing us to predict properties of more complex nuclei in the 132 Sn region when moving further away from stability.

Moreover, nuclear astrophysics has a global interest in properties of neutron-rich nuclei, since they are used as input for modeling nucleosynthesis processes such as the r process. When no experimental data are available, theoretical predictions are used. So far, all calculations assume that when states above the neutron-separation energy (S_n) are populated in β decay, they deexcite through β -delayed neutron emission. Nonetheless this assumption is known to be not correct [3]. Recently, a strong competition between neutron and γ decay of levels above S_n was observed both in the ⁷⁸Ni and in the ¹³²Sn regions [4,5]. The fact that the γ deexcitation of neutron-unbound states can be observed and studied opens the

possibility to hunt for those s. p. as well as single-hole (s. h.) states that are neutron unbound and were so far unobserved.

The study of ¹³³Sn provides excellent conditions to investigate single-particle transitions relevant in the neutron-rich ¹³²Sn region due to the simplicity of its nuclear structure. The applicability of the shell-model approach to interpret its nuclear structure arises from the doubly magic nature of ¹³²Sn. Such nature is evident from the high energy of its first excited state, $E(2^+, {}^{132}\text{Sn}) = 4041 \text{ keV } [6,7]$, and the large spectroscopic factors determined for known states in ¹³³Sn $(S \approx 1)$, revealing the purity of single-neutron excitations [8]. Simple configurations corresponding to neutron s. p. orbitals were assigned to low-lying states in ¹³³Sn, which were found at excitation energies of 854 keV ($\nu p_{3/2}$), 1367 keV ($\nu p_{1/2}$), 1561 keV ($\nu h_{9/2}$), and 2005 keV ($\nu f_{5/2}$) relative to the ($\nu f_{7/2}$) ground state of ¹³³Sn [5,8–12]. In view of the importance of the s. p. energies for predicting the properties of more complex nuclei, when moving away from the N=82 and Z = 50 shell closures, different experimental techniques were adopted to confirm these values and find the last missing s. p. state corresponding to the $vi_{13/2}$ orbital. At higher excitation energies, states based on the two-particle single-hole (2p1h)configurations with respect to the ¹³²Sn core are expected. At present, information about them is limited to a tentatively deduced neutron-hole $vh_{11/2}^{-1}$ state [5,9]. β -decay studies seem to be a natural choice to investigate

 β -decay studies seem to be a natural choice to investigate the nature of neutron-unbound states in ¹³³Sn, since there is a large energy window for their population in the β de-

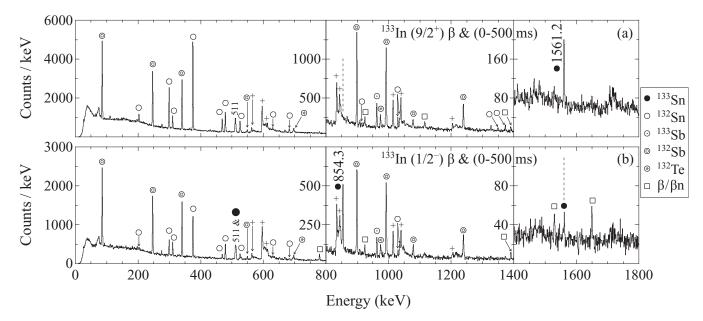


FIG. 1. Portions of β-gated γ-ray spectra within a time window of 500 ms after the proton impact, showing corresponding 854 keV and 1561 keV transitions in 133 Sn, which uniquely decay from the (a) $(9/2^+)$ ground state or (b) $(1/2^-)$ isomeric state of 133 In. Lines marked with a cross (+) arise from the neutron-induced activity.

cay of ¹³³In, determined by the high decay energy Q_{β} = 13.4(2) MeV (based on systematics) and the low neutronseparation energy S_n = 2.4 MeV [13]. Previous β -decay studies of ¹³³In provided information about the energy of delayed neutrons, E_n = 1.26 MeV, associated with decay of the (11/2⁻) neutron hole state, positioning it at an excitation energy of ~3.7 MeV in ¹³³Sn [9,10]. According to recent work, the decay of this state proceeds not only via neutron emission, but also, with significant contribution, via electromagnetic decay leading to the emission of 3570(50) keV γ rays [5].

The purpose of this work is to reexamine β decay of ¹³³In, taking advantage of recent experimental developments, which open new possibilities to study this β decay. Until recently, β decay studies of ¹³³In were limited by the inability to perform independent studies of β decay of the ¹³³In ground state (133g In), $I^{\pi} = (9/2^+)$, and isomeric state (133m In) with $I^{\pi}=(1/2^-)$ and $E_{\rm level}=330$ keV, both having similar half-lives. Only one half-life of $T_{1/2}=180(15)$ ms was observed in the experiment with beam containing both ^{133g}In and ^{133m}In [9]. Recent advances in resonance ionization laser ion sources for on-line isotope separators (ISOL) result not only in increased beam production yields, but also enhanced their purity. In the case of measurements using a ¹³³In beam produced at ISOL facilities, the delivery of a beam free from isobaric contamination is not the only requirement. In order to investigate specific s. p. and s. h. levels in ¹³³Sn populated in β decay of ¹³³In, the possibility to study separately the decay of the ground state and of the isomeric state is needed and was achieved via selective laser ionization in this work for the first time.

II. EXPERIMENTAL TECHNIQUE

The β decay of ¹³³In was studied at the Isotope Separator On-Line (ISOLDE) facility [14] at CERN. Indium ions were produced by fission induced in a UC_x target by fast neutrons. Those were generated by a proton-to-neutron converter [15], with a beam of 1.4-GeV protons from the Proton Synchrotron Booster (PSB) having an average beam intensity of 1.9 μ A. The fission products then diffuse from the target material to the hot ion source. The indium isotopes were ionized using a Resonance Ionization Laser Ion Source (RILIS) [16]. The application of isomer-selective ionization employing a titanium:sapphire (Ti:Sa) laser in narrow-band mode [17] allowed us to study separately the β decay of the groundor the isomeric-state of ¹³³In [18]. Following extraction and acceleration by an electrostatic potential of 40 kV, the beam of ¹³³In was separated using the High-Resolution Separator (HRS) [14] and then implanted on a movable aluminized mylar tape in the middle of the ISOLDE Decay Station (IDS) [19]. Pulses from the PSB were separated in time by multiples of 1.2 s, while the indium beam was implanted continuously for 200 ms after each proton pulse. To suppress the long-lived daughter activities, the tape was moved after every 34–35 proton pulses, matching the duration of the CERN PSB supercycle.

In order to measure the β -decay products of ¹³³In, the detection setup at IDS consisted of β and γ detectors arranged in a close geometry surrounding the beam-implantation po-

TABLE I. Relative γ -ray intensities (I_{rel}) following the β and βn decays of ¹³³In (9/2⁺) ground state and its (1/2⁻) isomeric level, normalized to the 4041-keV transition. It should be noted that, for the βn -decay channel, there might be some contribution coming from the beam impurity to the I_{rel} values presented below.

Decay channel	E_{γ} (keV)	I_{rel}^{a}	
		$133g$ In $(9/2^+)$	133m In $(1/2^-)$
β	513(1)	_	b
β	854.3(5)	_	33(2)
β	1561.2(5)	7.3(7)	_c
β	3181.1(5)	4.1(8)	_
β	3563.9(5)	38(4)	_c
β	6088(2)	4.8(7)	_c
βn	132(1)	d	
βn	203.0(5)	5.7(5)	2.9(5)
βn	299.4(5)	28(2)	13(1)
βn	310.4(5)	7.9(6)	11.0(9)
βn	375.1(5)	77(4)	43(2)
βn	469.0(5)	12.8(9)	5.8(7)
βn	478.9(5)	19(1)	18(1)
βn	526.0(5)	10.5(9)	6.9(7)
βn	630.1(5) ^e	<3	<3
βn	683.1(5)	5.6(5)	1.7(7)
βn	913.1(5)	1.6(3)	_
βn	1029.8(5)	3.9(8)	2.4(7)
βn	1035.8(5)	3.5(5)	6(1)
βn	1349.6(5)	1.3(4)	_
βn	1373.9(5)	2.3(5)	1.9(4)
βn	4041.1(5)	100(11)	100(11)
βn	4351.5(5)	54(6)	69(8)
βn	4416.2(5)	10(1)	8(1)
β and/or βn	779.4(5) ^f	2.4(8)	10(1)
β or βn	924.1(5)	4.0(6)	5(1)
β or βn	1115.6(5)	2.1(5)	_
β or βn	1390.6(5)	2.3(5)	4.7(7)
β or βn	1529.9(5)	_	2.9(9)
β or βn	1649.5(5)	_	6(1)
β or βn	3597(1)	3.5(9)	_
β or βn	5132(1)	_	6(1)
β or βn	5437(1)	_	9(1)
β or βn	5949(2)	-	7.7(9)
β or βn	6065(2)	_	5.5(8)

^aFor intensity per 100 decays of the parent, multiply by 0.122(15) and 0.109(13), for 133g In and 133m In, respectively.

sition. β particles were detected by a 3-mm thin plastic placed directly behind the ion collection point. For γ -rays detection we used four high-purity germanium Clovers ensuring high-resolution γ -ray spectroscopy up to 7.6 MeV

^bSeen in coincidence with 854 keV line.

^cBeam impurity. The observed intensity is compatible with the amount of the $(9/2^+)$ ground state component in the ¹³³In $(1/2^-)$ isomeric beam.

^dSeen in γ - γ coincidence spectra.

^eMost probably a doublet line.

^fMost probably a doublet line (780.8-keV transition reported in ¹³²Sn) [30].

and two LaBr₃(Ce) detectors, which were employed to measure lifetimes by applying the fast timing technique [20,21]. The Nutaq [22] digital data acquisition system (DAQ) was employed to read out the signals from the detectors and timing signals to correlate the activity with the proton impact on target. The fast plastic and LaBr₃(Ce) detector signals were preprocessed before being input into the digital DAQ [21]. Data were collected in triggerless mode. In the off-line analysis events were reconstructed, correlated with the time of arrival of the proton and coincidence gates as well as Clover add-back corrections were imposed.

Neutron-induced activity is a source of background that needs to be well understood for a consistent data analysis. Neutrons contributing to background activity can have two origins in this experiment: they may be produced by proton impact and emitted from the target area, or they may arise from the β decay of neutron-rich nuclei as delayed particles. The neutrons induce both (n, γ) and $(n, n'\gamma)$ reactions on the surrounding materials [23–25]. Particular attention was paid to the identification of γ transitions arising from these reactions. The neutron-induced peaks originating from interactions of neutrons from the target area are observed within the first 30 ms after the proton arrival. They were used to cross check the energy calibration at high energies. Their contribution can be removed by imposing a coincidence with the β detector and/or a time condition from the proton impact on target. The identification of γ rays following interactions of β -delayed neutrons is more complicated, since their time correlation is consistent with the half-life of ¹³³In, and they are also in coincidence with β particles.

III. EXPERIMENTAL RESULTS

In order to identify transitions following the β decay of 133 In, we studied β -gated γ -ray spectra within a time window from the proton impact on target, ranging from two to three half-lives of 133g In and 133m In. With such conditions, the contribution from daughters' activities, whose half-lives amount to 1.46(3) s for 133 Sn [26] and 39.7(8) s for 132 Sn [27], is significantly reduced.

In these spectra, we identified transitions corresponding to $^{133}{\rm In} \rightarrow ^{132}{\rm Sn} ~\beta n$ decay and subsequent $^{132}{\rm Sn} \rightarrow ^{132}{\rm Sb} ~\beta$ decay as the most intense ones. The quality of isomer selective laser ionization achieved in our experiment was demonstrated in Ref. [18], where we discussed the population of previously reported low-lying states in $^{133}{\rm Sn}$. An indication of the presence of the $(1/2^-)$ isomeric state of $^{133}{\rm In}$ in the implanted beam is the detection of the 854 keV γ ray emitted from $(3/2^-)$ state in $^{133}{\rm Sn}$, whereas the line at 1561 keV, corresponding to depopulation of the $(9/2^-)$ state in $^{133}{\rm Sn}$, is the signature of the $(9/2^+)$ ground-state content. In Fig. 1 we present portions of β -gated γ -ray spectra showing relevant known transitions uniquely decaying from the $(9/2^+)$ or $(1/2^-)$ state of $^{133}{\rm In}$.

Although the 133m In beam contained impurity originating from 133g In of the order of $\sim 30\%$, it is always possible to determine whether a new line is present in the spectrum due to the one or the other states of 133 In. It can be clarified by comparing relative γ -ray intensities, significantly influenced when the RILIS was set to provide 133g In versus 133m In beam. The relative intensities ($I_{\rm rel}$) of the γ rays assigned to β or

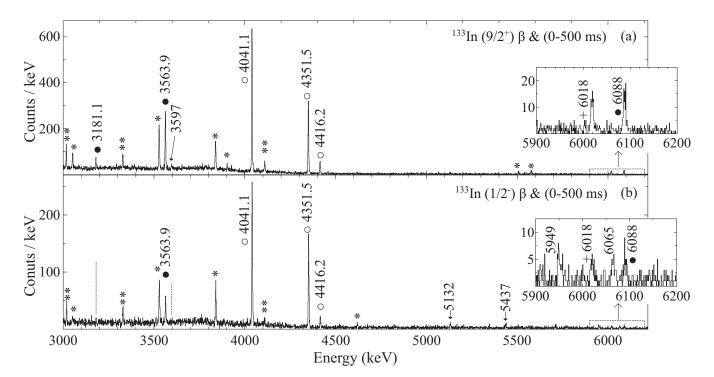


FIG. 2. Portions of the β -gated γ -ray spectra for the decay of the (a) ground and (b) isomeric state of ¹³³In recorded in the first 500 ms after the proton pulse occurrence. In the inserts, the zoom of the higher energy part is shown. Transitions in ¹³³Sn (\bullet) and ¹³²Sn (\circ) are labeled by their energies. Lines marked with star symbols correspond to escape peaks (" * " first or " ** " second escape peak, respectively). The line at 6018 keV (marked with "+") was identified as originating from a neutron-induced background.

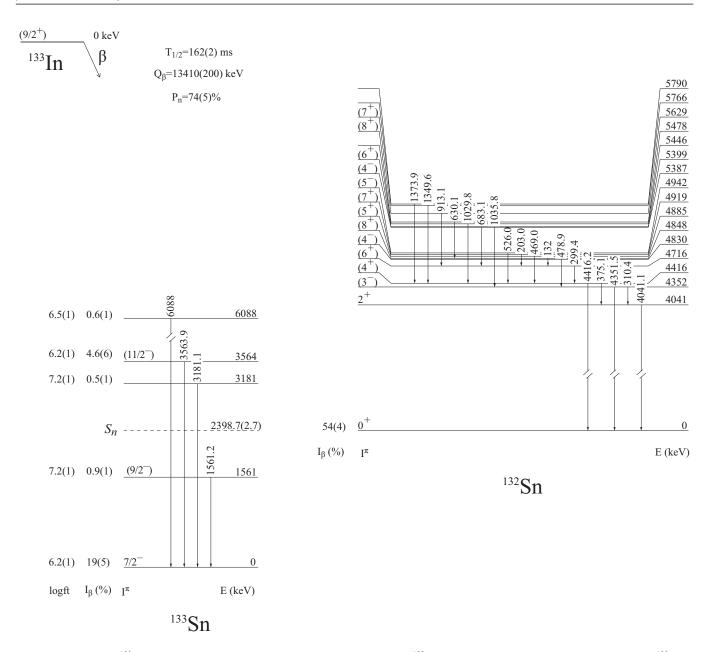


FIG. 3. Decay of 133g In, $I^{\pi} = (9/2^+)$, and apparent β feeding (I_{β}) to levels in 133 Sn. The β feeding to levels above S_n energy in 133 Sn is deduced only from γ transitions (see the text for more details). The spin-parity assignments of states in 132 Sn were adopted from Ref. [30]. The Q_{β} and S_n energies were taken from Ref. [13].

 βn -decay branches of the $(9/2^+)$ ground and $(1/2^-)$ isomeric state of 133 In are given in Table I. Transition de-populating the $(5/2^-)$ state in 133 Sn, 2004.6 keV [9,10], is not evident neither in the spectra of 133g In nor 133m In. We can estimate upper limits of its $I_{\rm rel}$, $I_{\rm rel} < 1$, and $I_{\rm rel} < 0.7$ for the β decay of 133g In and 133m In, respectively.

A. β decay of the ground state of ^{133g}In, $I^{\pi} = (9/2^{+})$

The most intense transitions following the decay of $(9/2^+)$ ground state of 133 In belong to its βn -decay channel (see Table I). Besides the known 1561.2-keV transition assigned to 133 Sn, we identified new transitions following the decay of the $(9/2^+)$ ground state at ener-

gies 924.1(5), 1029.8(5), 1115.6(5), 1349.6(5), 1373.9(5), 1390.6(5), 3181.1(5), 3563.9(5), 3597(1), and 6088(2) keV [see Figs. 1(a) and 2(a)]. Their assignment is justified by the analysis of their time dependences relative to the proton pulses. Their belonging to the neutron-induced background was excluded. Analysis of the β - γ - γ data allowed us to construct the decay scheme of 133g In. Three new transitions, 3181 keV, 3564 keV, and 6088 keV, could be placed in the level scheme of 133 Sn, see Figs. 2(a) and 3. Note that they deexcite levels above the neutron-separation energy. A half-life of $T_{1/2} = 167(7)$ ms was obtained for the 3564 keV transition (Fig. 4). In order to determine 133g In half-life value, three γ transitions were considered: the new γ transition at 3563.9 keV and known β -n- γ transitions at 375.1 keV and

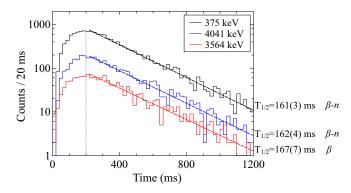


FIG. 4. Time distribution of the 375.1-, 4041.1-, and 3563.9-keV γ rays in coincidence with β particles with respect to the proton pulse. The fit of decay pattern is shown as a dashed line corresponding to the ^{133g}In decay. The vertical line indicates the end of the implantation.

4041.1 keV (see Fig. 4). We adopt the weighted average of 162(2) ms as the 133g In half-life. This value is consistent with two recent results known from the literature, 165(3) ms [28] and 163(7) ms [29]. For the 3181 keV and 6088 keV transitions, the time analysis gave low-precision results because of the limited statistics, but still in accordance with the half-life of 133g In. The analysis of the β - γ - γ coincident data allowed us to assign three new transitions, 1030 keV, 1350 keV, and 1374 keV, to 132 Sn since they are observed in coincidence with 375 keV and 4041 keV γ rays. Analysis of the β - γ - γ and γ - γ matrices does not indicate any coincidences for other new transitions.

B. β decay of the isomeric state of 133m In, $I^{\pi} = (1/2^{-})$

The analysis of the β - γ - γ data confirmed that the 854-keV and 513-keV transitions are in coincidence with each other and therefore follow the decay of the $I^{\pi} = (1/2^{-})$ isomer [18]. The observed $(1/2^-) \rightarrow 3/2^- \rightarrow 7/2^-$ cascade supports the low-spin assignment for the decaying state in the progenitor (see Fig. 5) [8]. Several new transitions at energies 924.1(5), 1029.8(5), 1373.9(5), 1390.6(5), 1529.9(5), 1649.5(5), 5132(1), 5437(1), 5949(2), and 6065(2) keV were observed in spectra [see Figs. 1(b) and 2(b)] and assigned to this decay. The low statistics did not allow us to measure the half-life of the individual new transitions, but we could confirm that they are consistent with the half-life of ^{133m}In, $T_{1/2} = 167(11)$ ms (Fig. 6), and therefore it is excluded that they belong to the decay of the granddaughter or any other nucleus in the isobaric mass chain. In the spectra collected with RILIS set on the $(1/2^-)$ isomeric state [Figs. 1(b) and 2(b)] weak transitions originating from the ground-state decay can be observed, due to a small ^{133g}In beam component.

C. Analysis of the apparent β feeding

The absolute intensities of the γ rays following the β decay of 133 In daughters, 132 Sn and 133 Sn, were used to calculate the number of 133 Sn and 132 Sn nuclei produced in the 133g In and 133m In decay. We adopted absolute γ -ray intensities of relevant transitions, $I_{abs}(962)$

keV, $^{133}Sn \rightarrow \,^{133}Sb) = 12(2)\% \,$ and $\,I_{abs}(340 \; keV, \,^{132}Sn \rightarrow \,$ 132 Sb) = 48.8(12)% from Refs. [31,32], respectively. Corrections to account for the tape movement and different halflives of ¹³²Sn and ¹³³Sn were included in the calculations. The determination of the number of nuclei produced both following the β and βn decays of ¹³³In allows us to calculate the βn emission probability, which was found to be $P_n =$ 74(5)% for the $(9/2^{+})$ ground state and $P_n = 80(5)\%$ for the $(1/2^{-})$ isomeric level. The apparent β feeding intensities (I_{β}) to levels in ¹³³Sn are summarized in Fig. 3. When no γ rays were detected the remaining intensity arising from both the β and βn decays was assigned to apparent ground-state feeding. Since some decays could proceed to states deexcited by weak, undetected γ -ray transitions, β feeding intensities should be taken as apparent. In particular, for levels located at excitation energies exceeding \hat{S}_n in ¹³³Sn, they should be considered only as a lower limit, since the population of neutron unbound states followed by neutron emission cannot be accounted for.

D. Lifetime measurement of 854 keV state in ¹³³Sn

The fast timing technique was applied in order to measure the half-life of the $3/2^-$ level at 854 keV in 133 Sn. Despite the fact that the 854 keV and 513 keV transitions are in coincidence, it was not possible to apply triple $(\beta-\gamma[HPGe detector]-\gamma[LaBr_3(Ce)])$ coincidences because of the limited statistics. Instead double $(\beta-\gamma[LaBr_3(Ce)])$ coincidences were employed, by means of the centroid-shift method [20,21], using as a reference point the centroid position of the time-delayed spectrum gated by the 1561 keV γ transition, which is assumed to be prompt. In this way, an upper limit on the lifetime was obtained, $T_{1/2}$ < 34 ps, which appears to be consistent with the value of 21(11) ps recently reported [5]. It was not possible to determine lifetimes of other states because of the high energy of the deexciting transitions and the low efficiency of the LaBr₃(Ce) detectors at these energies.

IV. DISCUSSION

The wave functions of states at low excitation energies in 133 Sn, a nucleus with only one valence neutron outside the 132 Sn core, should be dominated by s. p. neutron orbitals between N=82 and N=126 shells (Fig. 7). At higher excitation energies, states built on the neutron $(vf_{7/2}^2)v^{-1}$ or proton $v^1\pi^1\pi^{-1}$ two-particle one-hole configurations are expected. Due to the low neutron-separation energy of 133 Sn, the majority of those excited states are neutron unbound. Thanks to the large spin difference of the two β -decaying states of 133 In, it is possible to investigate separately the lower and higher spin states in 133 Sn and thus to probe independently different s. p. and $^{2}p1h$ levels relevant in the 132 Sn region.

The knowledge about neutron s. p. states above N=82 is almost complete. The only still unobserved s. p. state in this region, $13/2^+$ ($\nu i_{13/2}$), has been hypothesized to be neutron unbound in ¹³³Sn as it is expected at excitation energy about 2.5 MeV [33]. This state would be populated in the second-forbidden decay of the $(9/2^+)$ ^{133g}In, making it a rather hindered transition; it is not observed in this study. All

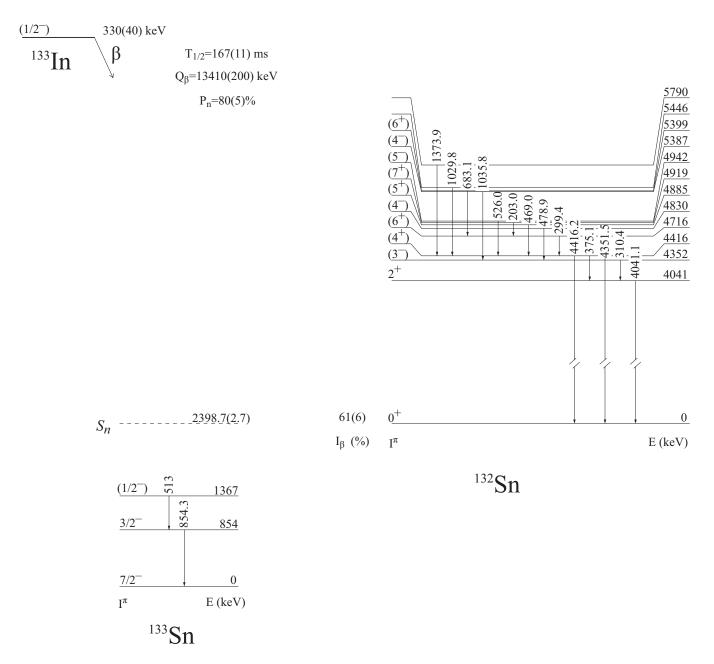


FIG. 5. Decay of 133m In, $I^{\pi}=(1/2^{-})$. The spin-parity assignments of states in 132 Sn adopted from Ref. [30]. The Q_{β} and S_{n} energies were taken from Ref. [13], the energy of the $I^{\pi}=(1/2^{-})$ isomeric state of 133 In was adopted from Ref. [26]. The determination of the apparent β feeding to the levels in 133 Sn was not possible due to unresolved contribution of the 511-keV annihilation γ -ray in the 513-keV photopeak.

known transitions depopulating excited states with $I^{\pi}=1/2^ (\nu p_{1/2})$, $3/2^ (\nu p_{3/2})$, and $I^{\pi}=9/2^ (\nu h_{9/2})$ assignments in ¹³³Sn were confirmed in this work. On the other hand, β feeding to the $(5/2^-)$ $(\nu f_{5/2})$ level was not evident neither in the decay of $(9/2^+)$ nor $(1/2^-)$ state of ¹³³In.

A. Neutron single-hole excited states in ¹³³Sn

The relevant s. p. levels in the 132 Sn region are depicted in Fig. 7. Strong population of the $11/2^-$ ($\nu h_{11/2}^{-1}$) and $7/2^+$ ($\nu g_{7/2}^{-1}$) neutron single-hole (2p1h) states in 133 Sn is expected

in the β decay of the $(9/2^+)$ ground state of 133 In. The β decay of its $(1/2^-)$ isomeric state would instead proceed by feeding the $1/2^+$ ($\nu s_{1/2}^{-1}$) and $3/2^+$ ($\nu d_{3/2}^{-1}$) states, which also have a neutron-hole nature. The spin-parity selection rules favor population of $7/2^+$ level via the $\nu g_{7/2} \to \pi g_{9/2}$ Gamow-Teller transition resulting in the $\nu f_{7/2}^2 g_{7/2}^{-1}$ daughter configuration (see Fig. 7). The corresponding $\nu g_{7/2}^{-1}$ hole state in 131 Sn was found at an excitation energy of 2434 keV with receiving the overwhelming majority of the β feeding, as demonstrated by the very low $\log ft = 4.4$ [34]. Only one level in 131 Sn located at lower excitation energy [$E_{\rm level} = 65.1(3)$ keV] than

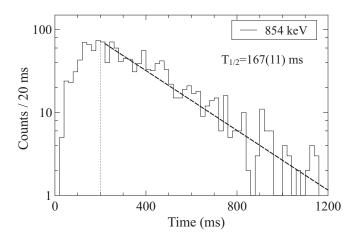


FIG. 6. Time distribution of the 854.3-keV γ -rays in coincidence with β particles with respect to the proton pulse. The fit of decay pattern is shown as a dashed line. The vertical line indicates the end of the implantation.

the $7/2^+$ state, which was assigned $I^{\pi} = 11/2^-$ spin-party, is fed in the decay of the $(9/2^+)^{131}$ In ground-state ($\log ft > 5.6$) [34]. The systematics of neutron hole states in the lighter odd $^{125-131}$ Sn isotopes follow a smooth trend, see Fig. 8. The excitation energies of the single-hole configurations increase

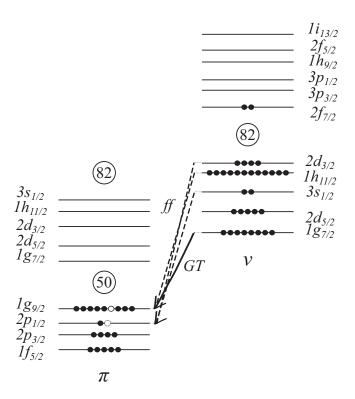


FIG. 7. Schematic view of single-particle states involved in Gamow-Teller (GT) and first forbidden (ff) decays resulting in the population of neutron hole states in 133 Sn. Configurations of 133 In are represented by circles corresponding to two neutron particles occupying the $\nu f_{7/2}$ orbital and the proton hole located on $\pi g_{9/2}$ (the ground state, solid stroke) or $\pi p_{1/2}$ orbital (isomeric state, dashed stroke).

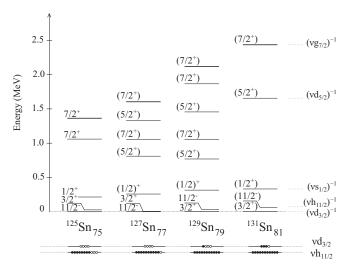


FIG. 8. Systematics of $1/2^+$, $3/2^+$, $5/2^+$, $7/2^+$, and $11/2^-$ states in odd $^{125-131}$ Sn isotopes observed in β -decay studies of $^{125-131}$ In isotopes [34–36]. Bold levels with $I^{\pi} = 7/2^+$ assignments have the biggest feedings following the β decays of $9/2^+$ states of indium isotopes.

with the addition of the next pair of neutrons. According to the systematics of the lowest-energy levels in odd $^{125-131}$ Sn nuclides, the two lowest-energy levels having s. h. nature in 133 Sn are expected to be the $3/2^+$ and $11/2^-$ states.

The identification of s. h. states in ¹³³Sn is more complicated than in lighter Sn isotopes, since the neutron-separation energy is drastically reduced just after crossing the N=82magic number. Consequently, β -delayed neutron emission is the main decay mode of ¹³³In, involving also s. h. states in ¹³³Sn, which are all expected to be neutron unbound. However, the high excitation energy of the first 2+ state in 132 Sn, $E(^{132}$ Sn, $2^+) = 4041$ keV [6,7], leads to favorable circumstances to observe γ emission from at least some of the neutron unbound states in ¹³³Sn. In the case of the decay of neutron unbound states in ¹³³Sn located at excitation energies up to \sim 6.4 MeV, the kinematics of β -delayed neutron emission $(E_i^* = S_n + E_f^* + E_n)$ would limit the final level that can be fed in ¹³²Sn to its ground state. If neutron unbound states of 133 Sn such as $7/2^+$ and $11/2^-$ are located below this energy threshold, their decay via neutron emission would have to proceed with $\ell = 4$ or $\ell = 5$, respectively. Due to centrifugal barrier hindering the neutron from leaving the nucleus, the contribution of electromagnetic decay of those unbound states would be significant. The observation of this phenomenon in the ¹³²Sn region was reported recently by Vaquero *et al.* [5] for the level found in ¹³³Sn at 3570(50) keV. This competition between neutron and γ decay of unbound states was attributed to a nuclear structure effect. In the case of lower spin states expected to be populated at excitation energies exceeding S_n of ¹³³Sn, such as $1/2^+$ ($\nu s_{1/2}^{-1}$) and $3/2^+$ ($\nu d_{3/2}^{-1}$), the aforementioned scenario would not be valid, since neutron emission with lower ℓ would not be hindered. Hence, the identification of lower spin states in ¹³³Sn is more complicated, since the γ -ray emission from them is not significant enough a decay mode to compete with neutron emission.

Owing to the isomer selectivity the observation of new transitions following only the decay of the $(9/2^+)$ ground state of ¹³³In gives the opportunity to connect them with missing higher spin states in ¹³³Sn, including those corresponding to the $vh_{11/2}^{-1}$ and $vg_{9/2}^{-1}$ configurations. We indicate here new transitions deexciting high spin states in ¹³³Sn at energies 3181, 3564, and 6088 keV.

The new γ -ray transition identified in this work at 6088 keV is assigned to the de-excitation of the 6088 keV level in ¹³³Sn. Other placement of this transition in the decay scheme of of ¹³³In is not supported by $\beta-\gamma-\gamma$ coincidences. For this level, we calculated β feeding resulting from γ -ray contribution and $\log ft = 6.5$ was obtained, see Fig. 3. It is worth noting that this level ($\sim 3.7 \text{ MeV}$ above S_n) may deexcite also by neutron emission to the ground state of ¹³²Sn. If we assumed that the I_{β} intensity determined for the ground state of ¹³²Sn (Fig. 3) was entirely due to the decay of this 6088 keV level, $\log ft = 4.5$ would be obtained. This suggests that the level is fed by a Gamow-Teller transition, and consequently $I^{\pi} = (7/2^{+})$ assignment is proposed for it. As a cross check the energy of the 7/2+ neutron-hole state in ¹³³Sn can be estimated using the energies of the 6⁻ and 7^- states in $^{132}{\rm Sn}$, which provide empirical information about the $vf_{7/2}\,g_{7/2}^{-1}$ interaction. These states were identified in β -decay studies of ¹³²In and their energies were deduced to be 7210 keV (6⁻) and \sim 7550 keV (7⁻) [7]. Using these values together with the known s. p. and s. h. energies from this region, the energy of $7/2^+$ state in ¹³³Sn was calculated to be about 6.1 MeV. This value, even if it is a rough estimate, led to the conclusion that the γ ray deexciting this state should

The next s. h. level in 133 Sn, which is expected to be populated in the β decay of the $(9/2^+)$ ground state of 133 In, is the I $^{\pi} = (11/2^-)$ state. Such a state was identified by Hoff *et al.* at an excitation energy of about 3700 keV [9]. Recently, a 3570(50) keV transition was assigned as the deexcitation of the same level [5]. In this work we provide improved accuracy of the energy of the $(11/2^-)$ state, 3563.9(5) keV. This level, located ~ 1.1 MeV above the S_n energy of 133 Sn, decays also through neutron emission. Hoff *et al.* observed 1.26 MeV neutrons following the decay of 133 In and related them to the decay of $(11/2^-)$ state populated in 133 Sn [9,10]. Since the contribution of neutrons in the decay of this state was clearly manifested in their spectra, real β feeding to the 3564 keV level is bigger than determined from our data, hence log ft = 6.2 should be treated as an upper limit.

Concerning the 3181 keV state, shell-model calculations predict a $11/2^-$ - $19/2^-$ multiplet corresponding to the configuration $vf_{7/2}^2\,h_{11/2}^{-1}$ between about 3.5 and 4.5 MeV and a $3/2^+$ - $15/2^+$ multiplet corresponding to $vf_{7/2}^2\,d_{3/2}^{-1}$ between 3.3 and 5 MeV [37]. The only states that can be expected below 3.5 MeV are those from the $3/2^+$ - $15/2^+$ multiplet. Taking into account that the 3181 keV level is populated in the decay of the $9/2^+$ ground state and that the calculated energies of the levels depend on monopole corrections, we propose a tentative spin-parity assignment of $I^{\pi}=(7/2^+,\,9/2^+,\,11/2^+)$ for 3181 keV level in 133 Sn. This β feeding transition from the $9/2^+$ ground state of 133 In is similar to the $9/2^+ \rightarrow (7/2^+)$

transition in the decay of ¹²⁹In feeding the 1047-keV state in ¹²⁹Sn [36].

B. Proton single-hole excited states in ¹³³Sn

Population of states having proton-hole nature, $vf_{7/2}\pi g_{7/2}g_{9/2}^{-1}$, should also be considered in studies of ¹³³In decay, since first forbidden $vf_{7/2} \rightarrow \pi g_{7/2}$ transition to orbitals above the Z=50 shell closure can also occur (see Fig. 7). On the basis of empirical calculations using the experimental interactions for $\pi g_{7/2}g_{9/2}^{-1}$, $vf_{7/2}\pi g_{7/2}$, and $vf_{7/2}\pi g_{9/2}^{-1}$ deduced from corresponding states in ¹³²Sn, ¹³⁴Sb, and ¹³²Sb [30], the excitation energy of such level is expected at about 4.8 MeV. Taking into account the value of $\log ft = 5.6$ for an analog state in ¹³²Sn, $\pi g_{7/2}g_{9/2}^{-1}$ at 5.6 MeV [30], the β feeding to the presumed 4.8 MeV state in ¹³³Sn was estimated to be about 2%. It is worth noting that this level would depopulate both by neutron and by γ decay. The nonobservation of candidates for the decay of such levels is compatible with the low branching.

Gamow-Teller decay from deeply bound neutrons in 133 In (e.g., $v2d_{5/2} \to \pi 2d_{5/2}$ and $v1g_{7/2} \to \pi 1g_{7/2}$) would lead to highly excited states for which γ deexcitation is not competing with neutron emission. The initial and final wave functions would have, e. g., configurations $vf_{7/2}^2\pi g_{9/2}^{-1}$ or $vf_{7/2}^2\pi g_{1/2}^{-1}$ A hint of the fact that this happens in the decay of both 133g In and 133m In is given by observation of almost the same transitions assigned to 132 Sn in both decays.

V. SUMMARY AND CONCLUSIONS

The structure of 133 Sn has been studied from the β decay of 133 In. By taking advantage of the isomer selectivity capabilities of the ISOLDE RILIS, independent investigation of the β decay of the 133 In $(9/2^+)$ ground state and the 133 In $(1/2^-)$ isomer could be performed.

Three states above the neutron-separation energy have been identified in the $^{133}{\rm Sn}$ nucleus, some of them for the first time. They all decay by electromagnetic radiation to the ground state. The high-lying γ -decaying states have predominant two-particle one-hole neutron configurations. The 6088-keV state is proposed to have $(7/2^+)$ spin-parity and be predominantly the neutron single-hole state based on the $\nu f_{7/2}^2\,g_{7/2}^{-1}$ configuration, while the 3564-keV state is proposed to be built on the $\nu f_{7/2}^2\,h_{11/2}^{-1}$ configuration, with assigned $(11/2^-)$ spin-parity. A spin-parity assignment of ${\rm I}^\pi=(7/2^+,9/2^+,11/2^+)$ is tentatively proposed for the 3181-keV level.

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